

Mathematica 11.3 Integration Test Results

Test results for the 664 problems in "1.2.3.2 (d x)^m (a+b x^n+c x^(2 n))^p.m"

Problem 61: Result more than twice size of optimal antiderivative.

$$\int x^2 (a^2 + 2 a b x^3 + b^2 x^6)^{5/2} dx$$

Optimal (type 2, 36 leaves, 2 steps):

$$\frac{(a + b x^3) (a^2 + 2 a b x^3 + b^2 x^6)^{5/2}}{18 b}$$

Result (type 2, 82 leaves):

$$\frac{1}{18 (a + b x^3)} x^3 \sqrt{(a + b x^3)^2 (6 a^5 + 15 a^4 b x^3 + 20 a^3 b^2 x^6 + 15 a^2 b^3 x^9 + 6 a b^4 x^{12} + b^5 x^{15})}$$

Problem 132: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (a^2 + 2 a b x^3 + b^2 x^6)^p dx$$

Optimal (type 5, 53 leaves, 3 steps):

$$\frac{1}{a} x (a + b x^3) (a^2 + 2 a b x^3 + b^2 x^6)^p \text{Hypergeometric2F1}\left[1, \frac{4}{3} + 2 p, \frac{4}{3}, -\frac{b x^3}{a}\right]$$

Result (type 6, 204 leaves):

$$\frac{1}{b^{1/3} (1 + 2 p)} 4^{-p} \left((-1)^{2/3} a^{1/3} + b^{1/3} x \right) \left(\frac{a^{1/3} + (-1)^{2/3} b^{1/3} x}{(1 + (-1)^{1/3}) a^{1/3}} \right)^{-2 p} \left(\frac{i \left(1 + \frac{b^{1/3} x}{a^{1/3}} \right)}{3 i + \sqrt{3}} \right)^{-2 p} \left((a + b x^3)^2 \right)^p$$

$$\text{AppellF1}\left[1 + 2 p, -2 p, -2 p, 2 (1 + p), -\frac{i \left((-1)^{2/3} a^{1/3} + b^{1/3} x \right)}{\sqrt{3} a^{1/3}}, \frac{i + \sqrt{3} - \frac{2 i b^{1/3} x}{a^{1/3}}}{3 i + \sqrt{3}}\right]$$

Problem 141: Result is not expressed in closed-form.

$$\int \frac{1}{x (a + b x^3 + c x^6)} dx$$

Optimal (type 3, 69 leaves, 7 steps):

$$\frac{b \operatorname{ArcTanh}\left[\frac{b+2 c x^3}{\sqrt{b^2-4 a c}}\right]}{3 a \sqrt{b^2-4 a c}} + \frac{\operatorname{Log}[x]}{a} - \frac{\operatorname{Log}\left[a+b x^3+c x^6\right]}{6 a}$$

Result (type 7, 66 leaves):

$$\frac{\operatorname{Log}[x]}{a} - \frac{\operatorname{RootSum}\left[a+b \#1^3+c \#1^6 \&, \frac{b \operatorname{Log}[x-\#1]+c \operatorname{Log}[x-\#1] \#1^3}{b+2 c \#1^3} \&\right]}{3 a}$$

Problem 142: Result is not expressed in closed-form.

$$\int \frac{1}{x^4 (a+b x^3+c x^6)} dx$$

Optimal (type 3, 89 leaves, 8 steps):

$$-\frac{1}{3 a x^3} - \frac{(b^2-2 a c) \operatorname{ArcTanh}\left[\frac{b+2 c x^3}{\sqrt{b^2-4 a c}}\right]}{3 a^2 \sqrt{b^2-4 a c}} - \frac{b \operatorname{Log}[x]}{a^2} + \frac{b \operatorname{Log}\left[a+b x^3+c x^6\right]}{6 a^2}$$

Result (type 7, 92 leaves):

$$-\frac{1}{3 a x^3} - \frac{b \operatorname{Log}[x]}{a^2} + \frac{\operatorname{RootSum}\left[a+b \#1^3+c \#1^6 \&, \frac{b^2 \operatorname{Log}[x-\#1]-a c \operatorname{Log}[x-\#1]+b c \operatorname{Log}[x-\#1] \#1^3}{b+2 c \#1^3} \&\right]}{3 a^2}$$

Problem 143: Result is not expressed in closed-form.

$$\int \frac{x^7}{a+b x^3+c x^6} dx$$

Optimal (type 3, 636 leaves, 14 steps):

$$\begin{aligned}
 & \frac{x^2}{2 c} + \frac{\left(b - \frac{b^2 - 2 a c}{\sqrt{b^2 - 4 a c}}\right) \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{\left(b - \sqrt{b^2 - 4 a c}\right)^{1/3}}}{\sqrt{3}}\right]}{2^{2/3} \sqrt{3} c^{5/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{1/3}} + \frac{\left(b + \frac{b^2 - 2 a c}{\sqrt{b^2 - 4 a c}}\right) \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{\left(b + \sqrt{b^2 - 4 a c}\right)^{1/3}}}{\sqrt{3}}\right]}{2^{2/3} \sqrt{3} c^{5/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{1/3}} + \\
 & \frac{\left(b - \frac{b^2 - 2 a c}{\sqrt{b^2 - 4 a c}}\right) \operatorname{Log}\left[\left(b - \sqrt{b^2 - 4 a c}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{2/3} c^{5/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{1/3}} + \\
 & \frac{\left(b + \frac{b^2 - 2 a c}{\sqrt{b^2 - 4 a c}}\right) \operatorname{Log}\left[\left(b + \sqrt{b^2 - 4 a c}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{2/3} c^{5/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{1/3}} - \\
 & \left(\left(b - \frac{b^2 - 2 a c}{\sqrt{b^2 - 4 a c}}\right) \operatorname{Log}\left[\left(b - \sqrt{b^2 - 4 a c}\right)^{2/3} - 2^{1/3} c^{1/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) / \\
 & \left(6 \times 2^{2/3} c^{5/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{1/3}\right) - \\
 & \left(\left(b + \frac{b^2 - 2 a c}{\sqrt{b^2 - 4 a c}}\right) \operatorname{Log}\left[\left(b + \sqrt{b^2 - 4 a c}\right)^{2/3} - 2^{1/3} c^{1/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) / \\
 & \left(6 \times 2^{2/3} c^{5/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{1/3}\right)
 \end{aligned}$$

Result (type 7, 70 leaves):

$$\frac{3 x^2 - 2 \operatorname{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{a \operatorname{Log}[x - \#1] + b \operatorname{Log}[x - \#1] \#1^3}{b \#1 + 2 c \#1^4} \&\right]}{6 c}$$

Problem 144: Result is not expressed in closed-form.

$$\int \frac{x^6}{a + b x^3 + c x^6} dx$$

Optimal (type 3, 631 leaves, 14 steps):

$$\frac{x}{c} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b - \sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{4/3} (b - \sqrt{b^2-4ac})^{2/3}} + \frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b + \sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{4/3} (b + \sqrt{b^2-4ac})^{2/3}} -$$

$$\frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{Log}\left[\left(b - \sqrt{b^2-4ac}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{4/3} (b - \sqrt{b^2-4ac})^{2/3}} -$$

$$\frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{Log}\left[\left(b + \sqrt{b^2-4ac}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{4/3} (b + \sqrt{b^2-4ac})^{2/3}} +$$

$$\left(\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{Log}\left[\left(b - \sqrt{b^2-4ac}\right)^{2/3} - 2^{1/3} c^{1/3} (b - \sqrt{b^2-4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) /$$

$$\left(6 \times 2^{1/3} c^{4/3} (b - \sqrt{b^2-4ac})^{2/3}\right) +$$

$$\left(\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{Log}\left[\left(b + \sqrt{b^2-4ac}\right)^{2/3} - 2^{1/3} c^{1/3} (b + \sqrt{b^2-4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) /$$

$$\left(6 \times 2^{1/3} c^{4/3} (b + \sqrt{b^2-4ac})^{2/3}\right)$$

Result (type 7, 70 leaves):

$$\frac{x}{c} - \frac{\operatorname{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{a \operatorname{Log}[x-\#1] + b \operatorname{Log}[x-\#1] \#1^3}{b \#1^2 + 2c \#1^5} \&\right]}{3c}$$

Problem 145: Result is not expressed in closed-form.

$$\int \frac{x^4}{a + b x^3 + c x^6} dx$$

Optimal (type 3, 558 leaves, 13 steps):

$$\begin{aligned}
 & \frac{(b - \sqrt{b^2 - 4 a c})^{2/3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b - \sqrt{b^2 - 4 a c})^{1/3}}}{\sqrt{3}}\right]}{2^{2/3} \sqrt{3} c^{2/3} \sqrt{b^2 - 4 a c}} - \frac{(b + \sqrt{b^2 - 4 a c})^{2/3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b + \sqrt{b^2 - 4 a c})^{1/3}}}{\sqrt{3}}\right]}{2^{2/3} \sqrt{3} c^{2/3} \sqrt{b^2 - 4 a c}} + \\
 & \frac{(b - \sqrt{b^2 - 4 a c})^{2/3} \operatorname{Log}\left[(b - \sqrt{b^2 - 4 a c})^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{2/3} c^{2/3} \sqrt{b^2 - 4 a c}} - \\
 & \frac{(b + \sqrt{b^2 - 4 a c})^{2/3} \operatorname{Log}\left[(b + \sqrt{b^2 - 4 a c})^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{2/3} c^{2/3} \sqrt{b^2 - 4 a c}} - \\
 & \left((b - \sqrt{b^2 - 4 a c})^{2/3} \operatorname{Log}\left[(b - \sqrt{b^2 - 4 a c})^{2/3} - 2^{1/3} c^{1/3} (b - \sqrt{b^2 - 4 a c})^{1/3} x + 2^{2/3} c^{2/3} x^2 \right] \right) / \\
 & \left(6 \times 2^{2/3} c^{2/3} \sqrt{b^2 - 4 a c} \right) + \\
 & \left((b + \sqrt{b^2 - 4 a c})^{2/3} \operatorname{Log}\left[(b + \sqrt{b^2 - 4 a c})^{2/3} - 2^{1/3} c^{1/3} (b + \sqrt{b^2 - 4 a c})^{1/3} x + 2^{2/3} c^{2/3} x^2 \right] \right) / \\
 & \left(6 \times 2^{2/3} c^{2/3} \sqrt{b^2 - 4 a c} \right)
 \end{aligned}$$

Result (type 7, 44 leaves):

$$\frac{1}{3} \operatorname{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{\operatorname{Log}[x - \#1] \#1^2}{b + 2 c \#1^3} \& \right]$$

Problem 146: Result is not expressed in closed-form.

$$\int \frac{x^3}{a + b x^3 + c x^6} dx$$

Optimal (type 3, 558 leaves, 13 steps):

$$\frac{(b - \sqrt{b^2 - 4ac})^{1/3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b - \sqrt{b^2 - 4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{1/3} \sqrt{b^2 - 4ac}} - \frac{(b + \sqrt{b^2 - 4ac})^{1/3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b + \sqrt{b^2 - 4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{1/3} \sqrt{b^2 - 4ac}} -$$

$$\frac{(b - \sqrt{b^2 - 4ac})^{1/3} \operatorname{Log}\left[(b - \sqrt{b^2 - 4ac})^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{1/3} \sqrt{b^2 - 4ac}} +$$

$$\frac{(b + \sqrt{b^2 - 4ac})^{1/3} \operatorname{Log}\left[(b + \sqrt{b^2 - 4ac})^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{1/3} \sqrt{b^2 - 4ac}} +$$

$$\left((b - \sqrt{b^2 - 4ac})^{1/3} \operatorname{Log}\left[(b - \sqrt{b^2 - 4ac})^{2/3} - 2^{1/3} c^{1/3} (b - \sqrt{b^2 - 4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2 \right] \right) /$$

$$\left(6 \times 2^{1/3} c^{1/3} \sqrt{b^2 - 4ac} \right) -$$

$$\left((b + \sqrt{b^2 - 4ac})^{1/3} \operatorname{Log}\left[(b + \sqrt{b^2 - 4ac})^{2/3} - 2^{1/3} c^{1/3} (b + \sqrt{b^2 - 4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2 \right] \right) /$$

$$\left(6 \times 2^{1/3} c^{1/3} \sqrt{b^2 - 4ac} \right)$$

Result (type 7, 42 leaves):

$$\frac{1}{3} \operatorname{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{\operatorname{Log}[x - \#1] \#1}{b + 2c \#1^3} \& \right]$$

Problem 147: Result is not expressed in closed-form.

$$\int \frac{x}{a + bx^3 + cx^6} dx$$

Optimal (type 3, 558 leaves, 13 steps):

$$-\frac{2^{1/3} c^{1/3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b - \sqrt{b^2 - 4ac})^{1/3}}}{\sqrt{3}}\right]}{\sqrt{3} \sqrt{b^2 - 4ac} (b - \sqrt{b^2 - 4ac})^{1/3}} + \frac{2^{1/3} c^{1/3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b + \sqrt{b^2 - 4ac})^{1/3}}}{\sqrt{3}}\right]}{\sqrt{3} \sqrt{b^2 - 4ac} (b + \sqrt{b^2 - 4ac})^{1/3}} -$$

$$\frac{2^{1/3} c^{1/3} \operatorname{Log}\left[(b - \sqrt{b^2 - 4ac})^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \sqrt{b^2 - 4ac} (b - \sqrt{b^2 - 4ac})^{1/3}} + \frac{2^{1/3} c^{1/3} \operatorname{Log}\left[(b + \sqrt{b^2 - 4ac})^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \sqrt{b^2 - 4ac} (b + \sqrt{b^2 - 4ac})^{1/3}} +$$

$$\left(c^{1/3} \operatorname{Log}\left[(b - \sqrt{b^2 - 4ac})^{2/3} - 2^{1/3} c^{1/3} (b - \sqrt{b^2 - 4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2 \right] \right) /$$

$$\left(3 \times 2^{2/3} \sqrt{b^2 - 4ac} (b - \sqrt{b^2 - 4ac})^{1/3} \right) -$$

$$\left(c^{1/3} \operatorname{Log}\left[(b + \sqrt{b^2 - 4ac})^{2/3} - 2^{1/3} c^{1/3} (b + \sqrt{b^2 - 4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2 \right] \right) /$$

$$\left(3 \times 2^{2/3} \sqrt{b^2 - 4ac} (b + \sqrt{b^2 - 4ac})^{1/3} \right)$$

Result (type 7, 43 leaves):

$$\frac{1}{3} \text{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{\text{Log}[x - \#1]}{b \#1 + 2 c \#1^4} \&\right]$$

Problem 148: Result is not expressed in closed-form.

$$\int \frac{1}{a + b x^3 + c x^6} dx$$

Optimal (type 3, 558 leaves, 13 steps):

$$\begin{aligned} & -\frac{2^{2/3} c^{2/3} \text{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b - \sqrt{b^2 - 4ac})^{1/3}}}{\sqrt{3}}\right]}{\sqrt{3} \sqrt{b^2 - 4ac} (b - \sqrt{b^2 - 4ac})^{2/3}} + \frac{2^{2/3} c^{2/3} \text{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b + \sqrt{b^2 - 4ac})^{1/3}}}{\sqrt{3}}\right]}{\sqrt{3} \sqrt{b^2 - 4ac} (b + \sqrt{b^2 - 4ac})^{2/3}} + \\ & \frac{2^{2/3} c^{2/3} \text{Log}\left[\left(b - \sqrt{b^2 - 4ac}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \sqrt{b^2 - 4ac} (b - \sqrt{b^2 - 4ac})^{2/3}} - \frac{2^{2/3} c^{2/3} \text{Log}\left[\left(b + \sqrt{b^2 - 4ac}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \sqrt{b^2 - 4ac} (b + \sqrt{b^2 - 4ac})^{2/3}} - \\ & \left(c^{2/3} \text{Log}\left[\left(b - \sqrt{b^2 - 4ac}\right)^{2/3} - 2^{1/3} c^{1/3} \left(b - \sqrt{b^2 - 4ac}\right)^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) / \\ & \left(3 \times 2^{1/3} \sqrt{b^2 - 4ac} \left(b - \sqrt{b^2 - 4ac}\right)^{2/3}\right) + \\ & \left(c^{2/3} \text{Log}\left[\left(b + \sqrt{b^2 - 4ac}\right)^{2/3} - 2^{1/3} c^{1/3} \left(b + \sqrt{b^2 - 4ac}\right)^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) / \\ & \left(3 \times 2^{1/3} \sqrt{b^2 - 4ac} \left(b + \sqrt{b^2 - 4ac}\right)^{2/3}\right) \end{aligned}$$

Result (type 7, 45 leaves):

$$\frac{1}{3} \text{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{\text{Log}[x - \#1]}{b \#1^2 + 2 c \#1^5} \&\right]$$

Problem 149: Result is not expressed in closed-form.

$$\int \frac{1}{x^2 (a + b x^3 + c x^6)} dx$$

Optimal (type 3, 610 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{1}{ax} + \frac{c^{1/3} \left(1 + \frac{b}{\sqrt{b^2-4ac}}\right) \text{ArcTan}\left[\frac{1 - \frac{2^{2/3}c^{1/3}x}{(b-\sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{2/3}\sqrt{3}a(b-\sqrt{b^2-4ac})^{1/3}} + \frac{c^{1/3} \left(1 - \frac{b}{\sqrt{b^2-4ac}}\right) \text{ArcTan}\left[\frac{1 - \frac{2^{2/3}c^{1/3}x}{(b+\sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{2/3}\sqrt{3}a(b+\sqrt{b^2-4ac})^{1/3}} + \\
 & \frac{c^{1/3} \left(1 + \frac{b}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b - \sqrt{b^2-4ac}\right)^{1/3} + 2^{1/3}c^{1/3}x\right]}{3 \times 2^{2/3}a(b-\sqrt{b^2-4ac})^{1/3}} + \\
 & \frac{c^{1/3} \left(1 - \frac{b}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b + \sqrt{b^2-4ac}\right)^{1/3} + 2^{1/3}c^{1/3}x\right]}{3 \times 2^{2/3}a(b+\sqrt{b^2-4ac})^{1/3}} - \\
 & \left(c^{1/3} \left(1 + \frac{b}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b - \sqrt{b^2-4ac}\right)^{2/3} - 2^{1/3}c^{1/3}(b-\sqrt{b^2-4ac})^{1/3}x + 2^{2/3}c^{2/3}x^2\right] \right) / \\
 & \left(6 \times 2^{2/3}a(b-\sqrt{b^2-4ac})^{1/3} \right) - \\
 & \left(c^{1/3} \left(1 - \frac{b}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b + \sqrt{b^2-4ac}\right)^{2/3} - 2^{1/3}c^{1/3}(b+\sqrt{b^2-4ac})^{1/3}x + 2^{2/3}c^{2/3}x^2\right] \right) / \\
 & \left(6 \times 2^{2/3}a(b+\sqrt{b^2-4ac})^{1/3} \right)
 \end{aligned}$$

Result (type 7, 71 leaves):

$$-\frac{1}{ax} - \frac{\text{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{b \text{Log}[x-\#1] + c \text{Log}[x-\#1] \#1^3}{b \#1 + 2c \#1^4} \&\right]}{3a}$$

Problem 150: Result is not expressed in closed-form.

$$\int \frac{1}{x^3 (a + bx^3 + cx^6)} dx$$

Optimal (type 3, 612 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{1}{2 a x^2} + \frac{c^{2/3} \left(1 + \frac{b}{\sqrt{b^2-4 a c}}\right) \operatorname{ArcTan}\left[\frac{1-\frac{2^{2^{1/3}} c^{1/3} x}{(b-\sqrt{b^2-4 a c})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} a (b-\sqrt{b^2-4 a c})^{2/3}} + \frac{c^{2/3} \left(1 - \frac{b}{\sqrt{b^2-4 a c}}\right) \operatorname{ArcTan}\left[\frac{1-\frac{2^{2^{1/3}} c^{1/3} x}{(b+\sqrt{b^2-4 a c})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} a (b+\sqrt{b^2-4 a c})^{2/3}} - \\
 & \frac{c^{2/3} \left(1 + \frac{b}{\sqrt{b^2-4 a c}}\right) \operatorname{Log}\left[\left(b-\sqrt{b^2-4 a c}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} a (b-\sqrt{b^2-4 a c})^{2/3}} - \\
 & \frac{c^{2/3} \left(1 - \frac{b}{\sqrt{b^2-4 a c}}\right) \operatorname{Log}\left[\left(b+\sqrt{b^2-4 a c}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} a (b+\sqrt{b^2-4 a c})^{2/3}} + \\
 & \left(\frac{c^{2/3} \left(1 + \frac{b}{\sqrt{b^2-4 a c}}\right) \operatorname{Log}\left[\left(b-\sqrt{b^2-4 a c}\right)^{2/3} - 2^{1/3} c^{1/3} (b-\sqrt{b^2-4 a c})^{1/3} x + 2^{2/3} c^{2/3} x^2\right]}{6 \times 2^{1/3} a (b-\sqrt{b^2-4 a c})^{2/3}}\right) / \\
 & \left(\frac{c^{2/3} \left(1 - \frac{b}{\sqrt{b^2-4 a c}}\right) \operatorname{Log}\left[\left(b+\sqrt{b^2-4 a c}\right)^{2/3} - 2^{1/3} c^{1/3} (b+\sqrt{b^2-4 a c})^{1/3} x + 2^{2/3} c^{2/3} x^2\right]}{6 \times 2^{1/3} a (b+\sqrt{b^2-4 a c})^{2/3}}\right) /
 \end{aligned}$$

Result (type 7, 75 leaves):

$$-\frac{1}{2 a x^2} - \frac{\operatorname{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{b \operatorname{Log}[x-\#1] + c \operatorname{Log}[x-\#1] \#1^3}{b \#1^2 + 2 c \#1^5} \&\right]}{3 a}$$

Problem 154: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2}{3 + 4 x^3 + x^6} dx$$

Optimal (type 3, 10 leaves, 4 steps):

$$-\frac{1}{3} \operatorname{ArcTanh}\left[2 + x^3\right]$$

Result (type 3, 21 leaves):

$$\frac{1}{6} \operatorname{Log}\left[1 + x^3\right] - \frac{1}{6} \operatorname{Log}\left[3 + x^3\right]$$

Problem 170: Result is not expressed in closed-form.

$$\int \frac{x^6}{1 - x^3 + x^6} dx$$

Optimal (type 3, 412 leaves, 14 steps):

$$\begin{aligned}
 & x + \frac{\left(i - \sqrt{3}\right) \operatorname{ArcTan}\left[\frac{1+\frac{2 x}{\frac{1}{2}\left(1-i \sqrt{3}\right)^{1 / 3}}}{\sqrt{3}}\right]}{3 \times 2^{1 / 3}\left(1-i \sqrt{3}\right)^{2 / 3}} - \frac{\left(i + \sqrt{3}\right) \operatorname{ArcTan}\left[\frac{1+\frac{2 x}{\frac{1}{2}\left(1+i \sqrt{3}\right)^{1 / 3}}}{\sqrt{3}}\right]}{3 \times 2^{1 / 3}\left(1+i \sqrt{3}\right)^{2 / 3}} + \\
 & \frac{\left(3-i \sqrt{3}\right) \operatorname{Log}\left[\left(1-i \sqrt{3}\right)^{1 / 3}-2^{1 / 3} x\right]}{9 \times 2^{1 / 3}\left(1-i \sqrt{3}\right)^{2 / 3}} + \frac{\left(3+i \sqrt{3}\right) \operatorname{Log}\left[\left(1+i \sqrt{3}\right)^{1 / 3}-2^{1 / 3} x\right]}{9 \times 2^{1 / 3}\left(1+i \sqrt{3}\right)^{2 / 3}} - \\
 & \frac{\left(3-i \sqrt{3}\right) \operatorname{Log}\left[\left(1-i \sqrt{3}\right)^{2 / 3}+\left(2\left(1-i \sqrt{3}\right)\right)^{1 / 3} x+2^{2 / 3} x^2\right]}{18 \times 2^{1 / 3}\left(1-i \sqrt{3}\right)^{2 / 3}} - \\
 & \frac{\left(3+i \sqrt{3}\right) \operatorname{Log}\left[\left(1+i \sqrt{3}\right)^{2 / 3}+\left(2\left(1+i \sqrt{3}\right)\right)^{1 / 3} x+2^{2 / 3} x^2\right]}{18 \times 2^{1 / 3}\left(1+i \sqrt{3}\right)^{2 / 3}}
 \end{aligned}$$

Result (type 7, 59 leaves):

$$x + \frac{1}{3} \operatorname{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{-\operatorname{Log}[x - \#1] + \operatorname{Log}[x - \#1] \#1^3}{-\#1^2 + 2 \#1^5} \&\right]$$

Problem 172: Result is not expressed in closed-form.

$$\int \frac{x^4}{1-x^3+x^6} dx$$

Optimal (type 3, 411 leaves, 13 steps):

$$\begin{aligned}
 & \frac{\left(i + \sqrt{3}\right) \operatorname{ArcTan}\left[\frac{1+\frac{2 x}{\frac{1}{2}\left(1-i \sqrt{3}\right)^{1 / 3}}}{\sqrt{3}}\right]}{3 \times 2^{2 / 3}\left(1-i \sqrt{3}\right)^{1 / 3}} - \frac{\left(i - \sqrt{3}\right) \operatorname{ArcTan}\left[\frac{1+\frac{2 x}{\frac{1}{2}\left(1+i \sqrt{3}\right)^{1 / 3}}}{\sqrt{3}}\right]}{3 \times 2^{2 / 3}\left(1+i \sqrt{3}\right)^{1 / 3}} + \\
 & \frac{\left(3+i \sqrt{3}\right) \operatorname{Log}\left[\left(1-i \sqrt{3}\right)^{1 / 3}-2^{1 / 3} x\right]}{9 \times 2^{2 / 3}\left(1-i \sqrt{3}\right)^{1 / 3}} + \frac{\left(3-i \sqrt{3}\right) \operatorname{Log}\left[\left(1+i \sqrt{3}\right)^{1 / 3}-2^{1 / 3} x\right]}{9 \times 2^{2 / 3}\left(1+i \sqrt{3}\right)^{1 / 3}} - \\
 & \frac{\left(3+i \sqrt{3}\right) \operatorname{Log}\left[\left(1-i \sqrt{3}\right)^{2 / 3}+\left(2\left(1-i \sqrt{3}\right)\right)^{1 / 3} x+2^{2 / 3} x^2\right]}{18 \times 2^{2 / 3}\left(1-i \sqrt{3}\right)^{1 / 3}} - \\
 & \frac{\left(3-i \sqrt{3}\right) \operatorname{Log}\left[\left(1+i \sqrt{3}\right)^{2 / 3}+\left(2\left(1+i \sqrt{3}\right)\right)^{1 / 3} x+2^{2 / 3} x^2\right]}{18 \times 2^{2 / 3}\left(1+i \sqrt{3}\right)^{1 / 3}}
 \end{aligned}$$

Result (type 7, 41 leaves):

$$\frac{1}{3} \operatorname{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{\operatorname{Log}[x - \#1] \#1^2}{-1 + 2 \#1^3} \&\right]$$

Problem 173: Result is not expressed in closed-form.

$$\int \frac{x^3}{1-x^3+x^6} dx$$

Optimal (type 3, 411 leaves, 13 steps):

$$\begin{aligned} & -\frac{(i+\sqrt{3}) \operatorname{ArcTan}\left[\frac{1+\frac{2x}{\left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{1/3} (1-i\sqrt{3})^{2/3}} + \frac{(i-\sqrt{3}) \operatorname{ArcTan}\left[\frac{1+\frac{2x}{\left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{1/3} (1+i\sqrt{3})^{2/3}} + \\ & \frac{(3+i\sqrt{3}) \operatorname{Log}\left[\left(1-i\sqrt{3}\right)^{1/3}-2^{1/3}x\right]}{9 \times 2^{1/3} (1-i\sqrt{3})^{2/3}} + \frac{(3-i\sqrt{3}) \operatorname{Log}\left[\left(1+i\sqrt{3}\right)^{1/3}-2^{1/3}x\right]}{9 \times 2^{1/3} (1+i\sqrt{3})^{2/3}} - \\ & \frac{(3+i\sqrt{3}) \operatorname{Log}\left[\left(1-i\sqrt{3}\right)^{2/3}+\left(2\left(1-i\sqrt{3}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{18 \times 2^{1/3} (1-i\sqrt{3})^{2/3}} - \\ & \frac{(3-i\sqrt{3}) \operatorname{Log}\left[\left(1+i\sqrt{3}\right)^{2/3}+\left(2\left(1+i\sqrt{3}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{18 \times 2^{1/3} (1+i\sqrt{3})^{2/3}} \end{aligned}$$

Result (type 7, 39 leaves):

$$\frac{1}{3} \operatorname{RootSum}\left[1-\#1^3+\#1^6 \&, \frac{\operatorname{Log}[x-\#1] \#1}{-1+2\#1^3} \&\right]$$

Problem 175: Result is not expressed in closed-form.

$$\int \frac{x}{1-x^3+x^6} dx$$

Optimal (type 3, 375 leaves, 13 steps):

$$\begin{aligned} & \frac{i \operatorname{ArcTan}\left[\frac{1+\frac{2x}{\left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}} - \frac{i \operatorname{ArcTan}\left[\frac{1+\frac{2x}{\left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}} + \frac{i \operatorname{Log}\left[\left(1-i\sqrt{3}\right)^{1/3}-2^{1/3}x\right]}{3\sqrt{3} \left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}} - \\ & \frac{i \operatorname{Log}\left[\left(1+i\sqrt{3}\right)^{1/3}-2^{1/3}x\right]}{3\sqrt{3} \left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}} - \frac{i \operatorname{Log}\left[\left(1-i\sqrt{3}\right)^{2/3}+\left(2\left(1-i\sqrt{3}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{3 \times 2^{2/3} \sqrt{3} (1-i\sqrt{3})^{1/3}} + \\ & \frac{i \operatorname{Log}\left[\left(1+i\sqrt{3}\right)^{2/3}+\left(2\left(1+i\sqrt{3}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{3 \times 2^{2/3} \sqrt{3} (1+i\sqrt{3})^{1/3}} \end{aligned}$$

Result (type 7, 40 leaves):

$$\frac{1}{3} \text{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{\text{Log}[x - \#1]}{-\#1 + 2 \#1^4} \&\right]$$

Problem 176: Result is not expressed in closed-form.

$$\int \frac{1}{1 - x^3 + x^6} dx$$

Optimal (type 3, 186 leaves, 13 steps):

$$\begin{aligned} & -\frac{1}{3} (-1)^{13/18} \text{ArcTan}\left[\frac{1 + 2 (-1)^{1/9} x}{\sqrt{3}}\right] + \frac{1}{3} (-1)^{5/18} \text{ArcTan}\left[\frac{1 - 2 (-1)^{8/9} x}{\sqrt{3}}\right] - \\ & \frac{(-1)^{5/18} \left(\text{Log}[2] + 3 \text{Log}\left[(-1)^{1/9} - x\right]\right)}{9 \sqrt{3}} + \frac{(-1)^{13/18} \text{Log}\left[-2^{1/3} \left((-1)^{8/9} + x\right)\right]}{3 \sqrt{3}} - \\ & \frac{(-1)^{13/18} \text{Log}\left[-2^{2/3} \left((-1)^{7/9} + \left((-1)^{8/9} - x\right) x\right)\right]}{6 \sqrt{3}} + \frac{(-1)^{5/18} \text{Log}\left[2^{2/3} \left((-1)^{2/9} + x \left((-1)^{1/9} + x\right)\right)\right]}{6 \sqrt{3}} \end{aligned}$$

Result (type 7, 42 leaves):

$$\frac{1}{3} \text{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{\text{Log}[x - \#1]}{-\#1^2 + 2 \#1^5} \&\right]$$

Problem 177: Result is not expressed in closed-form.

$$\int \frac{1}{x (1 - x^3 + x^6)} dx$$

Optimal (type 3, 41 leaves, 7 steps):

$$-\frac{\text{ArcTan}\left[\frac{1-2x^3}{\sqrt{3}}\right]}{3 \sqrt{3}} + \text{Log}[x] - \frac{1}{6} \text{Log}\left[1 - x^3 + x^6\right]$$

Result (type 7, 55 leaves):

$$\text{Log}[x] - \frac{1}{3} \text{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{-\text{Log}[x - \#1] + \text{Log}[x - \#1] \#1^3}{-1 + 2 \#1^3} \&\right]$$

Problem 178: Result is not expressed in closed-form.

$$\int \frac{1}{x^2 (1 - x^3 + x^6)} dx$$

Optimal (type 3, 416 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{1}{x} + \frac{(i - \sqrt{3}) \operatorname{ArcTan}\left[\frac{1 + \frac{2x}{\left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{2/3} (1 - i\sqrt{3})^{1/3}} - \frac{(i + \sqrt{3}) \operatorname{ArcTan}\left[\frac{1 + \frac{2x}{\left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{2/3} (1 + i\sqrt{3})^{1/3}} - \\
 & \frac{(3 - i\sqrt{3}) \operatorname{Log}\left[(1 - i\sqrt{3})^{1/3} - 2^{1/3} x\right]}{9 \times 2^{2/3} (1 - i\sqrt{3})^{1/3}} - \frac{(3 + i\sqrt{3}) \operatorname{Log}\left[(1 + i\sqrt{3})^{1/3} - 2^{1/3} x\right]}{9 \times 2^{2/3} (1 + i\sqrt{3})^{1/3}} + \\
 & \frac{(3 - i\sqrt{3}) \operatorname{Log}\left[(1 - i\sqrt{3})^{2/3} + (2(1 - i\sqrt{3}))^{1/3} x + 2^{2/3} x^2\right]}{18 \times 2^{2/3} (1 - i\sqrt{3})^{1/3}} + \\
 & \frac{(3 + i\sqrt{3}) \operatorname{Log}\left[(1 + i\sqrt{3})^{2/3} + (2(1 + i\sqrt{3}))^{1/3} x + 2^{2/3} x^2\right]}{18 \times 2^{2/3} (1 + i\sqrt{3})^{1/3}}
 \end{aligned}$$

Result (type 7, 61 leaves):

$$-\frac{1}{x} - \frac{1}{3} \operatorname{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{-\operatorname{Log}[x - \#1] + \operatorname{Log}[x - \#1] \#1^3}{-\#1 + 2 \#1^4} \&\right]$$

Problem 179: Result is not expressed in closed-form.

$$\int \frac{1}{x^3 (1 - x^3 + x^6)} dx$$

Optimal (type 3, 418 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{1}{2x^2} - \frac{(i - \sqrt{3}) \operatorname{ArcTan}\left[\frac{1 + \frac{2x}{\left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{1/3} (1 - i\sqrt{3})^{2/3}} + \frac{(i + \sqrt{3}) \operatorname{ArcTan}\left[\frac{1 + \frac{2x}{\left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{1/3} (1 + i\sqrt{3})^{2/3}} - \\
 & \frac{(3 - i\sqrt{3}) \operatorname{Log}\left[(1 - i\sqrt{3})^{1/3} - 2^{1/3} x\right]}{9 \times 2^{1/3} (1 - i\sqrt{3})^{2/3}} - \frac{(3 + i\sqrt{3}) \operatorname{Log}\left[(1 + i\sqrt{3})^{1/3} - 2^{1/3} x\right]}{9 \times 2^{1/3} (1 + i\sqrt{3})^{2/3}} + \\
 & \frac{(3 - i\sqrt{3}) \operatorname{Log}\left[(1 - i\sqrt{3})^{2/3} + (2(1 - i\sqrt{3}))^{1/3} x + 2^{2/3} x^2\right]}{18 \times 2^{1/3} (1 - i\sqrt{3})^{2/3}} + \\
 & \frac{(3 + i\sqrt{3}) \operatorname{Log}\left[(1 + i\sqrt{3})^{2/3} + (2(1 + i\sqrt{3}))^{1/3} x + 2^{2/3} x^2\right]}{18 \times 2^{1/3} (1 + i\sqrt{3})^{2/3}}
 \end{aligned}$$

Result (type 7, 65 leaves):

$$-\frac{1}{2x^2} - \frac{1}{3} \operatorname{RootSum}\left[1 - \#1^3 + \#1^6 \&, \frac{-\operatorname{Log}[x - \#1] + \operatorname{Log}[x - \#1] \#1^3}{-\#1^2 + 2 \#1^5} \&\right]$$

Problem 180: Result is not expressed in closed-form.

$$\int \frac{1}{x^4 (1 - x^3 + x^6)} dx$$

Optimal (type 3, 48 leaves, 8 steps):

$$-\frac{1}{3x^3} + \frac{\text{ArcTan}\left[\frac{1-2x^3}{\sqrt{3}}\right]}{3\sqrt{3}} + \text{Log}[x] - \frac{1}{6} \text{Log}[1 - x^3 + x^6]$$

Result (type 7, 51 leaves):

$$-\frac{1}{3x^3} + \text{Log}[x] - \frac{1}{3} \text{RootSum}\left[1 - \#1^3 + \#1^6, \frac{\text{Log}[x - \#1] \#1^3}{-1 + 2 \#1^3} \&\right]$$

Problem 181: Result is not expressed in closed-form.

$$\int \frac{1}{x^5 (1 - x^3 + x^6)} dx$$

Optimal (type 3, 423 leaves, 16 steps):

$$\begin{aligned} &-\frac{1}{4x^4} - \frac{1}{x} - \frac{(i + \sqrt{3}) \text{ArcTan}\left[\frac{1 + \frac{2x}{\left(\frac{1}{2}(1-i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{2/3} (1 - i\sqrt{3})^{1/3}} + \frac{(i - \sqrt{3}) \text{ArcTan}\left[\frac{1 + \frac{2x}{\left(\frac{1}{2}(1+i\sqrt{3})\right)^{1/3}}}{\sqrt{3}}}\right]}{3 \times 2^{2/3} (1 + i\sqrt{3})^{1/3}} - \\ &\frac{(3 + i\sqrt{3}) \text{Log}\left[\left(1 - i\sqrt{3}\right)^{1/3} - 2^{1/3}x\right]}{9 \times 2^{2/3} (1 - i\sqrt{3})^{1/3}} - \frac{(3 - i\sqrt{3}) \text{Log}\left[\left(1 + i\sqrt{3}\right)^{1/3} - 2^{1/3}x\right]}{9 \times 2^{2/3} (1 + i\sqrt{3})^{1/3}} + \\ &\frac{(3 + i\sqrt{3}) \text{Log}\left[\left(1 - i\sqrt{3}\right)^{2/3} + \left(2(1 - i\sqrt{3})\right)^{1/3}x + 2^{2/3}x^2\right]}{18 \times 2^{2/3} (1 - i\sqrt{3})^{1/3}} + \\ &\frac{(3 - i\sqrt{3}) \text{Log}\left[\left(1 + i\sqrt{3}\right)^{2/3} + \left(2(1 + i\sqrt{3})\right)^{1/3}x + 2^{2/3}x^2\right]}{18 \times 2^{2/3} (1 + i\sqrt{3})^{1/3}} \end{aligned}$$

Result (type 7, 54 leaves):

$$-\frac{1}{4x^4} - \frac{1}{x} - \frac{1}{3} \text{RootSum}\left[1 - \#1^3 + \#1^6, \frac{\text{Log}[x - \#1] \#1^2}{-1 + 2 \#1^3} \&\right]$$

Problem 182: Result is not expressed in closed-form.

$$\int \frac{1}{2 + x^3 + x^6} dx$$

Optimal (type 3, 381 leaves, 13 steps):

$$\frac{i \operatorname{ArcTan}\left[\frac{1-\frac{2x}{\left(\frac{1}{2}(1-i\sqrt{7})\right)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{21}\left(\frac{1}{2}(1-i\sqrt{7})\right)^{2/3}} - \frac{i \operatorname{ArcTan}\left[\frac{1-\frac{2x}{\left(\frac{1}{2}(1+i\sqrt{7})\right)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{21}\left(\frac{1}{2}(1+i\sqrt{7})\right)^{2/3}} - \frac{i \operatorname{Log}\left[\left(1-i\sqrt{7}\right)^{1/3}+2^{1/3}x\right]}{3\sqrt{7}\left(\frac{1}{2}(1-i\sqrt{7})\right)^{2/3}} +$$

$$\frac{i \operatorname{Log}\left[\left(1+i\sqrt{7}\right)^{1/3}+2^{1/3}x\right]}{3\sqrt{7}\left(\frac{1}{2}(1+i\sqrt{7})\right)^{2/3}} + \frac{i \operatorname{Log}\left[\left(1-i\sqrt{7}\right)^{2/3}-\left(2\left(1-i\sqrt{7}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{3\times 2^{1/3}\sqrt{7}\left(1-i\sqrt{7}\right)^{2/3}} -$$

$$\frac{i \operatorname{Log}\left[\left(1+i\sqrt{7}\right)^{2/3}-\left(2\left(1+i\sqrt{7}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{3\times 2^{1/3}\sqrt{7}\left(1+i\sqrt{7}\right)^{2/3}}$$

Result (type 7, 38 leaves):

$$\frac{1}{3} \operatorname{RootSum}\left[2+\#1^3+\#1^6 \&, \frac{\operatorname{Log}[x-\#1]}{\#1^2+2\#1^5} \&\right]$$

Problem 184: Result is not expressed in closed-form.

$$\int \frac{x^3}{2+x^3+x^6} dx$$

Optimal (type 3, 399 leaves, 13 steps):

$$-\frac{i\left(\frac{1}{2}(1-i\sqrt{7})\right)^{1/3} \operatorname{ArcTan}\left[\frac{1-\frac{2x}{\left(\frac{1}{2}(1-i\sqrt{7})\right)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{21}} + \frac{i\left(\frac{1}{2}(1+i\sqrt{7})\right)^{1/3} \operatorname{ArcTan}\left[\frac{1-\frac{2x}{\left(\frac{1}{2}(1+i\sqrt{7})\right)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{21}} +$$

$$\frac{(7+i\sqrt{7}) \operatorname{Log}\left[\left(1-i\sqrt{7}\right)^{1/3}+2^{1/3}x\right]}{21\times 2^{1/3}\left(1-i\sqrt{7}\right)^{2/3}} + \frac{(7-i\sqrt{7}) \operatorname{Log}\left[\left(1+i\sqrt{7}\right)^{1/3}+2^{1/3}x\right]}{21\times 2^{1/3}\left(1+i\sqrt{7}\right)^{2/3}} -$$

$$\frac{(7+i\sqrt{7}) \operatorname{Log}\left[\left(1-i\sqrt{7}\right)^{2/3}-\left(2\left(1-i\sqrt{7}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{42\times 2^{1/3}\left(1-i\sqrt{7}\right)^{2/3}} -$$

$$\frac{(7-i\sqrt{7}) \operatorname{Log}\left[\left(1+i\sqrt{7}\right)^{2/3}-\left(2\left(1+i\sqrt{7}\right)\right)^{1/3}x+2^{2/3}x^2\right]}{42\times 2^{1/3}\left(1+i\sqrt{7}\right)^{2/3}}$$

Result (type 7, 37 leaves):

$$\frac{1}{3} \operatorname{RootSum}\left[2+\#1^3+\#1^6 \&, \frac{\operatorname{Log}[x-\#1]\#1}{1+2\#1^3} \&\right]$$

Problem 196: Result more than twice size of optimal antiderivative.

$$\int x^3 \sqrt{a+bx^3+cx^6} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$\frac{x^4 \sqrt{a + b x^3 + c x^6} \operatorname{AppellF1}\left[\frac{4}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]}{4 \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}}$$

Result (type 6, 1043 leaves):

$$\frac{1}{448 c^2 (a + b x^3 + c x^6)^{3/2}} \left(8 c (3 b x + 8 c x^4) (a + b x^3 + c x^6)^2 + \left(96 a^2 b x (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \right. \\ \left. - 16 a \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \right. \\ \left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) + \\ \left(336 a^2 c x^4 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ \left(28 a \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \right. \\ \left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) + \\ \left(105 a b^2 x^4 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ \left(- 28 a \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \right. \\ \left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right)$$

Problem 197: Result more than twice size of optimal antiderivative.

$$\int x \sqrt{a + b x^3 + c x^6} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$x^2 \sqrt{a + b x^3 + c x^6} \operatorname{AppellF1}\left[\frac{2}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

$$\frac{2 \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}}{1}$$

Result (type 6, 701 leaves):

$$\frac{1}{25 (a + b x^3 + c x^6)^{3/2}}$$

$$x^2 \left(5 (a + b x^3 + c x^6)^2 + \left(75 a^2 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \right.$$

$$\left(40 a c \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - \right.$$

$$6 c x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right.$$

$$\left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) +$$

$$\left(12 a b x^3 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \right.$$

$$\left. \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) /$$

$$\left(c \left(32 a \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - \right.$$

$$3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right.$$

$$\left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right)$$

Problem 198: Result more than twice size of optimal antiderivative.

$$\int \sqrt{a + b x^3 + c x^6} dx$$

Optimal (type 6, 135 leaves, 2 steps):

$$\frac{x \sqrt{a + b x^3 + c x^6} \operatorname{AppellF1}\left[\frac{1}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}}$$

Result (type 6, 702 leaves):

$$\frac{1}{8 (a + b x^3 + c x^6)^{3/2}} x \left(2 (a + b x^3 + c x^6)^2 + \left(24 a^2 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \right. \\ \left. \left(c \left(16 a \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) + \right. \\ \left. \left(21 a b x^3 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \right. \\ \left. \left(4 c \left(28 a \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) \right) \right)$$

Problem 199: Result more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a + b x^3 + c x^6}}{x^2} dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$\frac{\sqrt{a + b x^3 + c x^6} \operatorname{AppellF1}\left[-\frac{1}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{2}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]}{x \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}}$$

Result (type 6, 702 leaves):

$$\begin{aligned}
 & \frac{1}{5 x (a+b x^3+c x^6)^{3/2}} \\
 & \left(-5 (a+b x^3+c x^6)^2 + \left(75 a b x^3 \left(b-\sqrt{b^2-4 a c}+2 c x^3 \right) \left(b+\sqrt{b^2-4 a c}+2 c x^3 \right) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) / \\
 & \left(4 c \left(20 a \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] - \right. \right. \\
 & \quad \left. \left. 3 x^3 \left(\left(b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left(b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) + \\
 & \left(24 a x^6 \left(b-\sqrt{b^2-4 a c}+2 c x^3 \right) \left(b+\sqrt{b^2-4 a c}+2 c x^3 \right) \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(32 a \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. 3 x^3 \left(\left(b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \quad \left. \left. \left(b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right)
 \end{aligned}$$

Problem 200: Result more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+b x^3+c x^6}}{x^3} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$\frac{\sqrt{a+b x^3+c x^6} \text{AppellF1}\left[-\frac{2}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{3}, -\frac{2 c x^3}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}\right]}{2 x^2 \sqrt{1+\frac{2 c x^3}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}}}$$

Result (type 6, 702 leaves):

$$\frac{1}{2x^2(a+bx^3+cx^6)^{3/2}} \left(- (a+bx^3+cx^6)^2 + \left(6abx^3 \left(b-\sqrt{b^2-4ac} + 2cx^3 \right) \left(b+\sqrt{b^2-4ac} + 2cx^3 \right) \right. \right. \\ \left. \left. \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \right. \\ \left(c \left(16a \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\ \left. \left. 3x^3 \left(\left(b+\sqrt{b^2-4ac} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \right. \right. \\ \left. \left. \left(b-\sqrt{b^2-4ac} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\ \left(21ax^6 \left(b-\sqrt{b^2-4ac} + 2cx^3 \right) \left(b+\sqrt{b^2-4ac} + 2cx^3 \right) \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \right. \right. \\ \left. \left. \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\ \left(4 \left(28a \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\ \left. \left. 3x^3 \left(\left(b+\sqrt{b^2-4ac} \right) \text{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \right. \right. \\ \left. \left. \left(b-\sqrt{b^2-4ac} \right) \text{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right)$$

Problem 214: Result more than twice size of optimal antiderivative.

$$\int x^3 (a+bx^3+cx^6)^{3/2} dx$$

Optimal (type 6, 141 leaves, 2 steps):

$$\left(ax^4 \sqrt{a+bx^3+cx^6} \text{AppellF1} \left[\frac{4}{3}, -\frac{3}{2}, -\frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b-\sqrt{b^2-4ac}}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}} \right] / \right. \\ \left. \left(4 \sqrt{1 + \frac{2cx^3}{b-\sqrt{b^2-4ac}}} \sqrt{1 + \frac{2cx^3}{b+\sqrt{b^2-4ac}}} \right) \right)$$

Result (type 6, 1746 leaves):

$$\frac{1}{232960c^3(a+bx^3+cx^6)^{3/2}} \\ x \left(8c(a+bx^3+cx^6)^2 (-297b^3 + 216b^2cx^3 + 320c^2x^3(16a+7cx^6) + 4bc(459a+812cx^6)) + \right. \\ \left. (9504a^2b^3(b-\sqrt{b^2-4ac} + 2cx^3)(b+\sqrt{b^2-4ac} + 2cx^3)) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] / \\
 & \left(16a \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] + \right. \\
 & \quad \left. \left. (b-\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right]\right) \right) - \\
 & \left(58752a^3bc \left(b-\sqrt{b^2-4ac}+2cx^3\right) \left(b+\sqrt{b^2-4ac}+2cx^3\right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] / \right. \\
 & \quad \left(16a \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \quad \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] + \right. \\
 & \quad \quad \left. \left. (b-\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right]\right) \right) \right) + \\
 & \left(10395ab^4x^3 \left(b-\sqrt{b^2-4ac}+2cx^3\right) \left(b+\sqrt{b^2-4ac}+2cx^3\right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] / \right. \\
 & \quad \left(28a \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \quad \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] + \right. \\
 & \quad \quad \left. \left. (b-\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right]\right) \right) \right) + \\
 & \left(120960a^3c^2x^3 \left(b-\sqrt{b^2-4ac}+2cx^3\right) \left(b+\sqrt{b^2-4ac}+2cx^3\right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] / \right. \\
 & \quad \left(28a \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \quad \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] + \right. \\
 & \quad \quad \left. \left. (b-\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right]\right) \right) \right) + \\
 & \left(76356a^2b^2cx^3 \left(b-\sqrt{b^2-4ac}+2cx^3\right) \left(b+\sqrt{b^2-4ac}+2cx^3\right) \right.
 \end{aligned}$$

$$\begin{aligned} & \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] / \\ & \left(-28 a \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\ & \left. 3 x^3 \left((b+\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\ & \left. \left. (b-\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \end{aligned}$$

Problem 215: Result more than twice size of optimal antiderivative.

$$\int x (a+b x^3+c x^6)^{3/2} dx$$

Optimal (type 6, 141 leaves, 2 steps):

$$\begin{aligned} & \left(a x^2 \sqrt{a+b x^3+c x^6} \text{AppellF1}\left[\frac{2}{3}, -\frac{3}{2}, -\frac{3}{2}, \frac{5}{3}, -\frac{2 c x^3}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}\right] \right) / \\ & \left(2 \sqrt{1+\frac{2 c x^3}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}} \right) \end{aligned}$$

Result (type 6, 1391 leaves):

$$\begin{aligned} & \frac{1}{8800 c^2 (a+b x^3+c x^6)^{3/2}} \\ & x^2 \left(5 c (a+b x^3+c x^6)^2 (27 b^2+250 b c x^3+32 c (14 a+5 c x^6)) - \left(675 a^2 b^2 (b-\sqrt{b^2-4 a c}+2 c x^3) \right. \right. \\ & \left. \left. (b+\sqrt{b^2-4 a c}+2 c x^3) \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) / \right. \\ & \left(20 a \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\ & \left. 3 x^3 \left((b+\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\ & \left. \left. (b-\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) + \\ & \left(10800 a^3 c (b-\sqrt{b^2-4 a c}+2 c x^3) (b+\sqrt{b^2-4 a c}+2 c x^3) \right. \\ & \left. \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\ & \left(20 a \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\ & \left. 3 x^3 \left((b+\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left((b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) + \\
 & \left(5616 a^2 b c x^3 (b - \sqrt{b^2 - 4ac} + 2cx^3) (b + \sqrt{b^2 - 4ac} + 2cx^3) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(32 a \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. 3 x^3 \left((b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left. (b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
 & \left(756 a b^3 x^3 (b - \sqrt{b^2 - 4ac} + 2cx^3) (b + \sqrt{b^2 - 4ac} + 2cx^3) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(-32 a \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad \left. 3 x^3 \left((b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left. (b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \Big)
 \end{aligned}$$

Problem 216: Result more than twice size of optimal antiderivative.

$$\int (a + bx^3 + cx^6)^{3/2} dx$$

Optimal (type 6, 136 leaves, 2 steps):

$$\begin{aligned}
 & \left(a x \sqrt{a + bx^3 + cx^6} \operatorname{AppellF1} \left[\frac{1}{3}, -\frac{3}{2}, -\frac{3}{2}, \frac{4}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(\sqrt{1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}}} \right)
 \end{aligned}$$

Result (type 6, 1389 leaves):

$$\begin{aligned}
 & \frac{1}{8960 c^2 (a + bx^3 + cx^6)^{3/2}} \\
 & x \left(8c (a + bx^3 + cx^6)^2 (27b^2 + 184bcx^3 + 28c(13a + 4cx^6)) - \left(864a^2b^2 (b - \sqrt{b^2 - 4ac} + 2cx^3) \right. \right. \\
 & \quad \left. \left. (b + \sqrt{b^2 - 4ac} + 2cx^3) \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left(16 a \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
& 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
& \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
& \left(24 192 a^3 c \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
& \left(16 a \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
& 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
& \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
& \left(8316 a^2 b c x^3 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
& \left(28 a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
& 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
& \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
& \left(945 a b^3 x^3 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
& \left(-28 a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
& 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
& \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right)
\end{aligned}$$

Problem 217: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^{3/2}}{x^2} dx$$

Optimal (type 6, 139 leaves, 2 steps):

$$- \left(a \sqrt{a + b x^3 + c x^6} \operatorname{AppellF1} \left[-\frac{1}{3}, -\frac{3}{2}, -\frac{3}{2}, \frac{2}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(x \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}} \right)$$

Result (type 6, 1058 leaves):

$$\frac{1}{100 (a + b x^3 + c x^6)^{3/2}} \left(\frac{5 (a + b x^3 + c x^6)^2 (-80 a + 19 b x^3 + 10 c x^6)}{4 x} + \left(2025 a^2 b x^2 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \right. \\ \left. \left. \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \right. \\ \left. \left(4 c \left(20 a \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \right. \\ \left. \left. 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) + \\ \left(540 a^2 x^5 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ \left. \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ \left(32 a \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\ \left. 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) + \\ \left(27 a b^2 x^5 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ \left. \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ \left(c \left(32 a \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ \left. \left. 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) \right) \right)$$

Problem 218: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^{3/2}}{x^3} dx$$

Optimal (type 6, 141 leaves, 2 steps):

$$- \left(\left(a \sqrt{a+bx^3+cx^6} \operatorname{AppellF1} \left[-\frac{2}{3}, -\frac{3}{2}, -\frac{3}{2}, \frac{1}{3}, -\frac{2cx^3}{b-\sqrt{b^2-4ac}}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}} \right] \right) / \right. \\ \left. \left(2x^2 \sqrt{1+\frac{2cx^3}{b-\sqrt{b^2-4ac}}} \sqrt{1+\frac{2cx^3}{b+\sqrt{b^2-4ac}}} \right) \right)$$

Result (type 6, 1054 leaves):

$$\frac{1}{112 (a+bx^3+cx^6)^{3/2}} \\ \left(\frac{2 (a+bx^3+cx^6)^2 (-28a+17bx^3+8cx^6)}{x^2} + \left(648a^2bx (b-\sqrt{b^2-4ac}+2cx^3) \right. \right. \\ \left. \left. (b+\sqrt{b^2-4ac}+2cx^3) \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \right. \\ \left. \left(c \left(16a \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \right. \\ \left. \left. 3x^3 \left(\left(b+\sqrt{b^2-4ac} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \right. \right. \\ \left. \left. \left(b-\sqrt{b^2-4ac} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\ \left(378a^2x^4 (b-\sqrt{b^2-4ac}+2cx^3) (b+\sqrt{b^2-4ac}+2cx^3) \right. \\ \left. \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\ \left(28a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \\ \left. 3x^3 \left(\left(b+\sqrt{b^2-4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \right. \\ \left. \left. \left(b-\sqrt{b^2-4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\ \left(189ab^2x^4 (b-\sqrt{b^2-4ac}+2cx^3) (b+\sqrt{b^2-4ac}+2cx^3) \right. \\ \left. \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\ \left(4c \left(28a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\ \left. \left. 3x^3 \left(\left(b+\sqrt{b^2-4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \right. \right. \\ \left. \left. \left(b-\sqrt{b^2-4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right)$$

Problem 229: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3}{\sqrt{a + b x^3 + c x^6}} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$\frac{1}{4 \sqrt{a + b x^3 + c x^6}} x^4 \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}$$

$$\text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 380 leaves):

$$\left(7 a^2 x^4 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3\right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3\right) \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right]\right) /$$

$$\left(\left(b - \sqrt{b^2 - 4 a c}\right) \left(b + \sqrt{b^2 - 4 a c}\right) \left(a + b x^3 + c x^6\right)^{3/2} \left(28 a \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - \right.$$

$$3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c}\right) \text{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \left(b - \sqrt{b^2 - 4 a c}\right) \text{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right]\right)\right)$$

Problem 230: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{\sqrt{a + b x^3 + c x^6}} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$\frac{1}{2 \sqrt{a + b x^3 + c x^6}} x^2 \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}$$

$$\text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 380 leaves):

$$\begin{aligned}
 & \left(10 a^2 x^2 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) \left(a + b x^3 + c x^6 \right)^{3/2} \right. \\
 & \quad \left(20 a \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 231: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{a + b x^3 + c x^6}} dx$$

Optimal (type 6, 135 leaves, 2 steps):

$$\begin{aligned}
 & \frac{1}{\sqrt{a + b x^3 + c x^6}} x \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}} \\
 & \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right]
 \end{aligned}$$

Result (type 6, 378 leaves):

$$\begin{aligned}
 & \left(16 a^2 x \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) \left(a + b x^3 + c x^6 \right)^{3/2} \right. \\
 & \quad \left(16 a \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 232: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^2 \sqrt{a + b x^3 + c x^6}} dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$-\frac{1}{x \sqrt{a + b x^3 + c x^6}} \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}$$

$$\text{AppellF1}\left[-\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{2}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 705 leaves):

$$\frac{1}{5 a x (a + b x^3 + c x^6)^{3/2}}$$

$$\left(-5 (a + b x^3 + c x^6)^2 + \left(25 a b x^3 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3)\right.\right.$$

$$\left.\left.\text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right]\right) /$$

$$\left(4 c \left(20 a \text{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - \right.\right.$$

$$\left.\left.3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c}\right) \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right.\right.$$

$$\left.\left.\left(b - \sqrt{b^2 - 4 a c}\right) \text{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right]\right)\right) \right) +$$

$$\left(16 a x^6 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \right.\right.$$

$$\left.\left.\frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right]\right) /$$

$$\left(32 a \text{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - \right.$$

$$\left.\left.3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c}\right) \text{AppellF1}\left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right.\right.$$

$$\left.\left.\left(b - \sqrt{b^2 - 4 a c}\right) \text{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right]\right)\right) \right) \right)$$

Problem 233: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^3 \sqrt{a + b x^3 + c x^6}} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$- \left(\left(\sqrt{1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}}} \right. \right. \\ \left. \left. \text{AppellF1} \left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{1}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(2x^2 \sqrt{a + bx^3 + cx^6} \right) \right)$$

Result (type 6, 705 leaves):

$$\frac{1}{2ax^2 (a + bx^3 + cx^6)^{3/2}} \\ \left(- (a + bx^3 + cx^6)^2 - \left(2abx^3 \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \right. \\ \left. \left. \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \right. \\ \left(c \left(16a \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\ \left. \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) + \\ \left(7ax^6 \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \right. \right. \\ \left. \left. \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ \left(4 \left(28a \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\ \left. \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) \right)$$

Problem 243: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3}{(a + bx^3 + cx^6)^{3/2}} dx$$

Optimal (type 6, 143 leaves, 2 steps):

$$\left(x^4 \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}} \operatorname{AppellF1}\left[\frac{4}{3}, \frac{3}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right] \right) / \left(4 a \sqrt{a + b x^3 + c x^6} \right)$$

Result (type 6, 711 leaves):

$$\frac{1}{3 (b^2 - 4 a c) (a + b x^3 + c x^6)^{3/2}} 2 x \left(- (b + 2 c x^3) (a + b x^3 + c x^6) + \left(4 a b (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \left(c \left(16 a \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) + \left(7 a x^3 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \left(56 a \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - 6 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right)$$

Problem 244: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{(a + b x^3 + c x^6)^{3/2}} dx$$

Optimal (type 6, 143 leaves, 2 steps):

$$\left(x^2 \sqrt{1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}}} \right. \\
 \left. \text{AppellF1} \left[\frac{2}{3}, \frac{3}{2}, \frac{3}{2}, \frac{5}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(2a \sqrt{a + bx^3 + cx^6} \right)$$

Result (type 6, 1054 leaves):

$$\frac{1}{30a(-b^2 + 4ac)(a + bx^3 + cx^6)^{3/2}} \\
 x^2 \left(-20(b^2 - 2ac + bcx^3)(a + bx^3 + cx^6) + \left(100a^2(b - \sqrt{b^2 - 4ac} + 2cx^3) \right. \right. \\
 \left. \left. (b + \sqrt{b^2 - 4ac} + 2cx^3) \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \right. \\
 \left(20a \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 3x^3 \left((b + \sqrt{b^2 - 4ac}) \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 \left. (b - \sqrt{b^2 - 4ac}) \text{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \left. \right) + \\
 \left(25a^2(b - \sqrt{b^2 - 4ac} + 2cx^3)(b + \sqrt{b^2 - 4ac} + 2cx^3) \right. \\
 \left. \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 \left(c \left(20a \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 3x^3 \left((b + \sqrt{b^2 - 4ac}) \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 \left. (b - \sqrt{b^2 - 4ac}) \text{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \left. \right) \left. \right) + \\
 \left(64abx^3(b - \sqrt{b^2 - 4ac} + 2cx^3)(b + \sqrt{b^2 - 4ac} + 2cx^3) \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \right. \right. \\
 \left. \left. \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 \left(32a \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 3x^3 \left((b + \sqrt{b^2 - 4ac}) \text{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 \left. (b - \sqrt{b^2 - 4ac}) \text{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \left. \right) \left. \right)$$

Problem 245: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + b x^3 + c x^6)^{3/2}} dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$\frac{1}{a \sqrt{a + b x^3 + c x^6}} x \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}}$$

$$\text{AppellF1}\left[\frac{1}{3}, \frac{3}{2}, \frac{3}{2}, \frac{4}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 1056 leaves):

$$\begin{aligned}
 & \frac{1}{3a(-b^2+4ac)(a+bx^3+cx^6)^{3/2}} \\
 & 2 \left(-x(b^2-2ac+bcx^3)(a+bx^3+cx^6) + \left(16a^2x(b-\sqrt{b^2-4ac}+2cx^3) \right. \right. \\
 & \quad \left. \left. (b+\sqrt{b^2-4ac}+2cx^3) \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \right. \\
 & \quad \left(16a \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \\
 & \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. \left. (b-\sqrt{b^2-4ac}) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) - \\
 & \quad \left(2ab^2x(b-\sqrt{b^2-4ac}+2cx^3)(b+\sqrt{b^2-4ac}+2cx^3) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \quad \left(c \left(16a \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\
 & \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. \left. (b-\sqrt{b^2-4ac}) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right) + \\
 & \quad \left(7abx^4(b-\sqrt{b^2-4ac}+2cx^3)(b+\sqrt{b^2-4ac}+2cx^3) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \quad \left(4 \left(28a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\
 & \quad 3x^3 \left((b+\sqrt{b^2-4ac}) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. \left. (b-\sqrt{b^2-4ac}) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 246: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^2(a+bx^3+cx^6)^{3/2}} dx$$

Optimal (type 6, 141 leaves, 2 steps):

$$- \left(\left(\sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}} \operatorname{AppellF1} \left[-\frac{1}{3}, \frac{3}{2}, \frac{3}{2}, \frac{2}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(a x \sqrt{a + b x^3 + c x^6} \right) \right)$$

Result (type 6, 1599 leaves):

$$\begin{aligned} & \frac{1}{15 (a + b x^3 + c x^6)^{3/2}} \left(\frac{10 x^2 (b^3 - 3 a b c + b^2 c x^3 - 2 a c^2 x^3) (a + b x^3 + c x^6)}{a^2 (-b^2 + 4 a c)} - \frac{15 (a + b x^3 + c x^6)^2}{a^2 x} \right. \\ & \left(125 b^3 x^2 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \operatorname{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \right. \right. \\ & \left. \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] / \left((b^2 - 4 a c) (-b + \sqrt{b^2 - 4 a c}) \right) \\ & (b + \sqrt{b^2 - 4 a c}) \left(-20 a \operatorname{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & \left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \left. \right) - \\ & \left(300 a b c x^2 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \right. \\ & \left. \operatorname{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] / \right. \\ & \left((b^2 - 4 a c) (-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c}) \right) \\ & \left(-20 a \operatorname{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & 3 x^3 \left((b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & \left. \left. (b - \sqrt{b^2 - 4 a c}) \operatorname{AppellF1} \left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \left. \right) + \\ & \left(320 b^2 c x^5 (b - \sqrt{b^2 - 4 a c} + 2 c x^3) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \right. \\ & \left. \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] / \right. \\ & \left((b^2 - 4 a c) (-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c}) \right) \\ & \left(-32 a \operatorname{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \end{aligned}$$

$$\begin{aligned}
 & 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Bigg) - \\
 & \left(1024ac^2x^5 \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\
 & \left. \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((b^2 - 4ac) \left(-b + \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) \right) \\
 & \left(-32a \text{AppellF1} \left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \Bigg) \Bigg)
 \end{aligned}$$

Problem 247: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^3 (a + bx^3 + cx^6)^{3/2}} dx$$

Optimal (type 6, 143 leaves, 2 steps):

$$\begin{aligned}
 & - \left(\left(\sqrt{1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}}} \right. \right. \\
 & \left. \left. \text{AppellF1} \left[-\frac{2}{3}, \frac{3}{2}, \frac{3}{2}, \frac{1}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(2ax^2 \sqrt{a + bx^3 + cx^6} \right) \right)
 \end{aligned}$$

Result (type 6, 1593 leaves):

$$\begin{aligned}
 & \frac{1}{6(a + bx^3 + cx^6)^{3/2}} \left(\frac{4x(b^3 - 3abc + b^2cx^3 - 2a^2cx^3)(a + bx^3 + cx^6)}{a^2(-b^2 + 4ac)} - \frac{3(a + bx^3 + cx^6)^2}{a^2x^2} - \right. \\
 & \left(56b^3x \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \left((b^2 - 4ac) \left(-b + \sqrt{b^2 - 4ac} \right) \right) \\
 & \left(b + \sqrt{b^2 - 4ac} \right) \left(-16a \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left((b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) + \\
 & \left(288abcx \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((b^2 - 4ac) \left(-b + \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) \right) \\
 & \left(-16a \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
 & \left(49b^2cx^4 \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((b^2 - 4ac) \left(-b + \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) \right) \\
 & \left(-28a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\
 & \left(140ac^2x^4 \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((b^2 - 4ac) \left(-b + \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) \right) \\
 & \left(-28a \operatorname{AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{1}{2}, \frac{3}{2}, \frac{10}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{7}{3}, \frac{3}{2}, \frac{1}{2}, \frac{10}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right)
 \end{aligned}$$

Problem 250: Result is not expressed in closed-form.

$$\int \frac{(dx)^m}{a+bx^3+cx^6} dx$$

Optimal (type 5, 173 leaves, 3 steps):

$$\frac{2c(dx)^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{3}, \frac{4+m}{3}, -\frac{2cx^3}{b-\sqrt{b^2-4ac}}\right]}{\sqrt{b^2-4ac} (b-\sqrt{b^2-4ac}) d(1+m)} - \frac{2c(dx)^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{3}, \frac{4+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}\right]}{\sqrt{b^2-4ac} (b+\sqrt{b^2-4ac}) d(1+m)}$$

Result (type 7, 84 leaves):

$$\frac{1}{3m} (dx)^m \operatorname{RootSum}\left[a+b\sqrt[3]{1^3}+c\sqrt[3]{1^6}, \frac{\operatorname{Hypergeometric2F1}\left[-m, -m, 1-m, -\frac{\sqrt[3]{1}}{x-\sqrt[3]{1}}\right] \left(\frac{x}{x-\sqrt[3]{1}}\right)^{-m}}{b\sqrt[3]{1^2}+2c\sqrt[3]{1^5}} \&\right]$$

Problem 251: Result unnecessarily involves higher level functions.

$$\int \frac{(dx)^m}{(a+bx^3+cx^6)^2} dx$$

Optimal (type 5, 315 leaves, 4 steps):

$$\frac{(dx)^{1+m} (b^2-2ac+bcx^3)}{3a(b^2-4ac)d(a+bx^3+cx^6)} + \frac{\left(c(b^2(2-m)+b\sqrt{b^2-4ac}(2-m)-4ac(5-m))(dx)^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{3}, \frac{4+m}{3}, -\frac{2cx^3}{b-\sqrt{b^2-4ac}}\right]\right)}{\left(3a(b^2-4ac)^{3/2}(b-\sqrt{b^2-4ac})d(1+m)\right)} - \frac{\left(c(b^2(2-m)-b\sqrt{b^2-4ac}(2-m)-4ac(5-m))(dx)^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{3}, \frac{4+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}\right]\right)}{\left(3a(b^2-4ac)^{3/2}(b+\sqrt{b^2-4ac})d(1+m)\right)}$$

Result (type 6, 376 leaves):

$$\left(a(4+m)x(dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\ \left. \operatorname{AppellF1} \left[\frac{1+m}{3}, 2, 2, \frac{4+m}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \left(4c(1+m) \right) \\ \left(a + bx^3 + cx^6 \right)^3 \left(a(4+m) \operatorname{AppellF1} \left[\frac{1+m}{3}, 2, 2, \frac{4+m}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\ \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+m}{3}, 2, 3, \frac{7+m}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+m}{3}, 3, 2, \frac{7+m}{3}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right)$$

Problem 252: Result more than twice size of optimal antiderivative.

$$\int (dx)^m (a + bx^3 + cx^6)^{3/2} dx$$

Optimal (type 6, 158 leaves, 2 steps):

$$\left(a(dx)^{1+m} \sqrt{a + bx^3 + cx^6} \operatorname{AppellF1} \left[\frac{1+m}{3}, -\frac{3}{2}, -\frac{3}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \\ \left(d(1+m) \sqrt{1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}}} \right)$$

Result (type 6, 1083 leaves):

$$\begin{aligned}
 & \frac{1}{4c^2 \sqrt{a+bx^3+cx^6}} \\
 & \left((b - \sqrt{b^2 - 4ac}) \left(b + \sqrt{b^2 - 4ac} \right) x (dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\
 & \left. \left(\left(a(4+m) \operatorname{AppellF1} \left[\frac{1+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \right. \right. \\
 & \left. \left((1+m) \left(4a(4+m) \operatorname{AppellF1} \left[\frac{1+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) + \right. \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+m}{3}, -\frac{1}{2}, \frac{1}{2}, \frac{7+m}{3}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1} \left[\frac{4+m}{3}, \frac{1}{2}, -\frac{1}{2}, \frac{7+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\
 & \left(b(7+m)x^3 \operatorname{AppellF1} \left[\frac{4+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{7+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left((4+m) \left(4a(7+m) \operatorname{AppellF1} \left[\frac{4+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{7+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{7+m}{3}, -\frac{1}{2}, \frac{1}{2}, \frac{10+m}{3}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1} \left[\frac{7+m}{3}, \frac{1}{2}, -\frac{1}{2}, \frac{10+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\
 & \left(c(10+m)x^6 \operatorname{AppellF1} \left[\frac{7+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{10+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left((7+m) \left(4a(10+m) \operatorname{AppellF1} \left[\frac{7+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{10+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) + \right. \\
 & \left. 3x^3 \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{10+m}{3}, -\frac{1}{2}, \frac{1}{2}, \frac{13+m}{3}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1} \left[\frac{10+m}{3}, \frac{1}{2}, -\frac{1}{2}, \frac{13+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 253: Result more than twice size of optimal antiderivative.

$$\int (dx)^m \sqrt{a+bx^3+cx^6} dx$$

Optimal (type 6, 157 leaves, 2 steps):

$$\left((dx)^{1+m} \sqrt{a+bx^3+cx^6} \operatorname{AppellF1}\left[\frac{1+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b-\sqrt{b^2-4ac}}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}\right] \right) / \left(d(1+m) \sqrt{1+\frac{2cx^3}{b-\sqrt{b^2-4ac}}} \sqrt{1+\frac{2cx^3}{b+\sqrt{b^2-4ac}}} \right)$$

Result (type 6, 424 leaves):

$$\left((b-\sqrt{b^2-4ac}) (b+\sqrt{b^2-4ac}) (4+m) x (dx)^m \operatorname{AppellF1}\left[\frac{1+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] \right) / \left(4c^2(1+m) \sqrt{a+bx^3+cx^6} \right) + \left(4a(4+m) \operatorname{AppellF1}\left[\frac{1+m}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] + 3x^3 \left((b+\sqrt{b^2-4ac}) \operatorname{AppellF1}\left[\frac{4+m}{3}, -\frac{1}{2}, \frac{1}{2}, \frac{7+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] + (b-\sqrt{b^2-4ac}) \operatorname{AppellF1}\left[\frac{4+m}{3}, \frac{1}{2}, -\frac{1}{2}, \frac{7+m}{3}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}, \frac{2cx^3}{-b+\sqrt{b^2-4ac}}\right] \right) \right)$$

Problem 254: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx)^m}{\sqrt{a+bx^3+cx^6}} dx$$

Optimal (type 6, 157 leaves, 2 steps):

$$\left((dx)^{1+m} \sqrt{1+\frac{2cx^3}{b-\sqrt{b^2-4ac}}} \sqrt{1+\frac{2cx^3}{b+\sqrt{b^2-4ac}}} \operatorname{AppellF1}\left[\frac{1+m}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4+m}{3}, -\frac{2cx^3}{b-\sqrt{b^2-4ac}}, -\frac{2cx^3}{b+\sqrt{b^2-4ac}}\right] \right) / \left(d(1+m) \sqrt{a+bx^3+cx^6} \right)$$

Result (type 6, 426 leaves):

$$\begin{aligned}
 & \left(4 a^2 (4+m) x (d x)^m \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+m) (a + b x^3 + c x^6)^{3/2} \right. \\
 & \quad \left(4 a (4+m) \text{AppellF1} \left[\frac{1+m}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. 3 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4+m}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4+m}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 255: Result more than twice size of optimal antiderivative.

$$\int \frac{(d x)^m}{(a + b x^3 + c x^6)^{3/2}} dx$$

Optimal (type 6, 160 leaves, 2 steps):

$$\begin{aligned}
 & \left((d x)^{1+m} \sqrt{1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}} \text{AppellF1} \left[\frac{1+m}{3}, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4+m}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(a d (1+m) \sqrt{a + b x^3 + c x^6} \right)
 \end{aligned}$$

Result (type 6, 426 leaves):

$$\begin{aligned}
 & \left(4 a^2 (4+m) x (d x)^m \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{3}, \frac{3}{2}, \frac{3}{2}, \frac{4+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+m) (a + b x^3 + c x^6)^{5/2} \right. \\
 & \quad \left(4 a (4+m) \text{AppellF1} \left[\frac{1+m}{3}, \frac{3}{2}, \frac{3}{2}, \frac{4+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. 9 x^3 \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4+m}{3}, \frac{3}{2}, \frac{5}{2}, \frac{7+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4+m}{3}, \frac{5}{2}, \frac{3}{2}, \frac{7+m}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 256: Result more than twice size of optimal antiderivative.

$$\int (d x)^m (a+b x^3+c x^6)^p d x$$

Optimal (type 6, 155 leaves, 2 steps):

$$\frac{1}{d(1+m)} (d x)^{1+m} \left(1+\frac{2 c x^3}{b-\sqrt{b^2-4 a c}}\right)^{-p} \left(1+\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}\right)^{-p} (a+b x^3+c x^6)^p \operatorname{AppellF1}\left[\frac{1+m}{3},-p,-p,\frac{4+m}{3},-\frac{2 c x^3}{b-\sqrt{b^2-4 a c}},-\frac{2 c x^3}{b+\sqrt{b^2-4 a c}}\right]$$

Result (type 6, 501 leaves):

$$\begin{aligned} & \left(2^{-1-p} c\left(b+\sqrt{b^2-4 a c}\right)(4+m) x(d x)^m\left(\frac{b-\sqrt{b^2-4 a c}}{2 c}+x^3\right)^{-p}\right. \\ & \left.\left(\frac{b-\sqrt{b^2-4 a c}+2 c x^3}{c}\right)^{1+p}\left(-2 a+\left(-b+\sqrt{b^2-4 a c}\right) x^3\right)^2(a+b x^3+c x^6)^{-1+p}\right. \\ & \left.\operatorname{AppellF1}\left[\frac{1+m}{3},-p,-p,\frac{4+m}{3},-\frac{2 c x^3}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\ & \left(\left(-b+\sqrt{b^2-4 a c}\right)(1+m)\left(b+\sqrt{b^2-4 a c}+2 c x^3\right)\right. \\ & \left(-2 a(4+m) \operatorname{AppellF1}\left[\frac{1+m}{3},-p,-p,\frac{4+m}{3},-\frac{2 c x^3}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right]+3 p x^3\left(\left(-b+\sqrt{b^2-4 a c}\right) \operatorname{AppellF1}\left[\frac{4+m}{3}, 1-p,-p,\frac{7+m}{3},-\frac{2 c x^3}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right]-\left(b+\sqrt{b^2-4 a c}\right) \operatorname{AppellF1}\left[\frac{4+m}{3},-p, 1-p,\frac{7+m}{3},-\frac{2 c x^3}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^3}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \end{aligned}$$

Problem 257: Result unnecessarily involves higher level functions.

$$\int x^8 (a+b x^3+c x^6)^p d x$$

Optimal (type 5, 224 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{b(2+p)(a+bx^3+cx^6)^{1+p}}{6c^2(1+p)(3+2p)} + \frac{x^3(a+bx^3+cx^6)^{1+p}}{3c(3+2p)} + \\
 & \left(2^p(2ac-b^2(2+p)) \left(-\frac{b-\sqrt{b^2-4ac}+2cx^3}{\sqrt{b^2-4ac}} \right)^{-1-p} (a+bx^3+cx^6)^{1+p} \text{Hypergeometric2F1} \left[\right. \right. \\
 & \quad \left. \left. -p, 1+p, 2+p, \frac{b+\sqrt{b^2-4ac}+2cx^3}{2\sqrt{b^2-4ac}} \right] \right) / \left(3c^2\sqrt{b^2-4ac}(1+p)(3+2p) \right)
 \end{aligned}$$

Result (type 6, 395 leaves):

$$\begin{aligned}
 & \left(2 \left(b + \sqrt{b^2 - 4ac} \right) x^9 \left(b - \sqrt{b^2 - 4ac} + 2cx^3 \right) \left(2a + \left(b - \sqrt{b^2 - 4ac} \right) x^3 \right)^2 \right. \\
 & \quad \left. \left(a + x^3(b + cx^3) \right)^{-1+p} \text{AppellF1} \left[3, -p, -p, 4, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(9 \left(-b + \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) \right. \\
 & \quad \left(-8a \text{AppellF1} \left[3, -p, -p, 4, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad \left. px^3 \left(\left(-b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[4, 1-p, -p, 5, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. \left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[4, -p, 1-p, 5, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^3}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 258: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x^5 (a + bx^3 + cx^6)^p dx$$

Optimal (type 5, 161 leaves, 3 steps):

$$\begin{aligned}
 & \frac{(a + bx^3 + cx^6)^{1+p}}{6c(1+p)} + \left(2^p b \left(-\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{\sqrt{b^2 - 4ac}} \right)^{-1-p} (a + bx^3 + cx^6)^{1+p} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[-p, 1+p, 2+p, \frac{b + \sqrt{b^2 - 4ac} + 2cx^3}{2\sqrt{b^2 - 4ac}} \right] \right) / \left(3c\sqrt{b^2 - 4ac}(1+p) \right)
 \end{aligned}$$

Result (type 6, 439 leaves):

$$\begin{aligned} & \left(2^{-2-p} c \left(b + \sqrt{b^2 - 4 a c} \right) x^6 \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \right. \\ & \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^{1+p} \left(2 a + \left(b - \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 \left(a + x^3 \left(b + c x^3 \right) \right)^{-1+p} \right. \\ & \left. \text{AppellF1} \left[2, -p, -p, 3, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ & \left(-6 a \text{AppellF1} \left[2, -p, -p, 3, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & \left. p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[3, 1-p, -p, 4, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ & \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[3, -p, 1-p, 4, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \end{aligned}$$

Problem 260: Result more than twice size of optimal antiderivative.

$$\int x^4 (a + b x^3 + c x^6)^p dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$\begin{aligned} & \frac{1}{5} x^5 \left(1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}} \right)^{-p} \left(1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right)^{-p} (a + b x^3 + c x^6)^p \\ & \text{AppellF1} \left[\frac{5}{3}, -p, -p, \frac{8}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right] \end{aligned}$$

Result (type 6, 411 leaves):

$$\begin{aligned} & \left(4 \left(b + \sqrt{b^2 - 4 a c} \right) x^5 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(-2 a + \left(-b + \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 \right. \\ & \left. \left(a + b x^3 + c x^6 \right)^{-1+p} \text{AppellF1} \left[\frac{5}{3}, -p, -p, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left(5 \left(-b + \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ & \left(-16 a \text{AppellF1} \left[\frac{5}{3}, -p, -p, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{8}{3}, 1-p, -p, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ & \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{8}{3}, -p, 1-p, \frac{11}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \end{aligned}$$

Problem 261: Result more than twice size of optimal antiderivative.

$$\int x^3 (a + b x^3 + c x^6)^p dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$\frac{1}{4} x^4 \left(1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}} \right)^{-p} \left(1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right)^{-p} (a + b x^3 + c x^6)^p$$

$$\text{AppellF1}\left[\frac{4}{3}, -p, -p, \frac{7}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 456 leaves):

$$\begin{aligned} & \left(7 \times 2^{-3-p} c (b + \sqrt{b^2 - 4 a c}) x^4 \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \right. \\ & \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^{1+p} \left(-2 a + (-b + \sqrt{b^2 - 4 a c}) x^3 \right)^2 (a + b x^3 + c x^6)^{-1+p} \right. \\ & \left. \text{AppellF1}\left[\frac{4}{3}, -p, -p, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ & \left((-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c} + 2 c x^3) \right. \\ & \left(-14 a \text{AppellF1}\left[\frac{4}{3}, -p, -p, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \\ & \left. 3 p x^3 \left((-b + \sqrt{b^2 - 4 a c}) \text{AppellF1}\left[\frac{7}{3}, 1-p, -p, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] - \right. \right. \\ & \left. \left. (b + \sqrt{b^2 - 4 a c}) \text{AppellF1}\left[\frac{7}{3}, -p, 1-p, \frac{10}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \end{aligned}$$

Problem 262: Result more than twice size of optimal antiderivative.

$$\int x (a + b x^3 + c x^6)^p dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$\frac{1}{2} x^2 \left(1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}} \right)^{-p} \left(1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right)^{-p} (a + b x^3 + c x^6)^p$$

$$\text{AppellF1}\left[\frac{2}{3}, -p, -p, \frac{5}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 454 leaves):

$$\begin{aligned} & \left(5 \times 2^{-2-p} c \left(b + \sqrt{b^2 - 4 a c} \right) \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \right. \\ & \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^{1+p} \left(-2 a x + \left(-b + \sqrt{b^2 - 4 a c} \right) x^4 \right)^2 \left(a + b x^3 + c x^6 \right)^{-1+p} \right. \\ & \left. \text{AppellF1} \left[\frac{2}{3}, -p, -p, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ & \left. \left(-10 a \text{AppellF1} \left[\frac{2}{3}, -p, -p, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\ & \left. \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{5}{3}, 1-p, -p, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \right. \\ & \left. \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{5}{3}, -p, 1-p, \frac{8}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) \end{aligned}$$

Problem 263: Result more than twice size of optimal antiderivative.

$$\int (a + b x^3 + c x^6)^p dx$$

Optimal (type 6, 133 leaves, 2 steps):

$$\begin{aligned} & x \left(1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}} \right)^{-p} \left(1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right)^{-p} \left(a + b x^3 + c x^6 \right)^p \\ & \text{AppellF1} \left[\frac{1}{3}, -p, -p, \frac{4}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right] \end{aligned}$$

Result (type 6, 487 leaves):

$$\begin{aligned} & \left(2^{1-2p} \left(b + \sqrt{b^2 - 4 a c} \right) x \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \left(\frac{b + \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \right. \\ & \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^{1+p} \left(\frac{b + \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^{-1+p} \left(-2 a + \left(-b + \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 \right. \\ & \left. \left(a + b x^3 + c x^6 \right)^{-1+p} \text{AppellF1} \left[\frac{1}{3}, -p, -p, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \left(-8 a \text{AppellF1} \left[\frac{1}{3}, -p, -p, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\ & \left. \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4}{3}, 1-p, -p, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \right. \\ & \left. \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{4}{3}, -p, 1-p, \frac{7}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) \end{aligned}$$

Problem 264: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x} dx$$

Optimal (type 6, 157 leaves, 3 steps):

$$\frac{1}{3p} 2^{-1+2p} \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^{-p} \left(\frac{b + \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^{-p} \\ (a + b x^3 + c x^6)^p \text{AppellF1} \left[-2p, -p, -p, 1 - 2p, -\frac{b - \sqrt{b^2 - 4ac}}{2cx^3}, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3} \right]$$

Result (type 6, 500 leaves):

$$\left(4^{-1-p} c (-1 + 2p) \left(1 + \frac{b - \sqrt{b^2 - 4ac}}{2cx^3} \right)^{-p} x^3 \left(\frac{b - \sqrt{b^2 - 4ac}}{2c} + x^3 \right)^{-p} \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{c} \right)^{1+p} \right. \\ \left. \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^p \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) (a + b x^3 + c x^6)^{-1+p} \right. \\ \left. \text{AppellF1} \left[-2p, -p, -p, 1 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] \right) / \left(3p \right. \\ \left. \left(- \left(b + \sqrt{b^2 - 4ac} \right) p \text{AppellF1} \left[1 - 2p, 1 - p, -p, 2 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] + \right. \right. \\ \left. \left(-b + \sqrt{b^2 - 4ac} \right) p \text{AppellF1} \left[1 - 2p, -p, 1 - p, 2 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] + \right. \\ \left. \left. 2c (-1 + 2p) x^3 \text{AppellF1} \left[-2p, -p, -p, 1 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] \right) \right)$$

Problem 265: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x^2} dx$$

Optimal (type 6, 136 leaves, 2 steps):

$$-\frac{1}{x} \left(1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}} \right)^{-p} \left(1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right)^{-p} \\ (a + b x^3 + c x^6)^p \text{AppellF1} \left[-\frac{1}{3}, -p, -p, \frac{2}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right]$$

Result (type 6, 408 leaves):

$$\left(\left(b + \sqrt{b^2 - 4 a c} \right) \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^3 \right) \left(-2 a + \left(-b + \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 \right. \\ \left. (a + b x^3 + c x^6)^{-1+p} \operatorname{AppellF1} \left[-\frac{1}{3}, -p, -p, \frac{2}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ \left(\left(-b + \sqrt{b^2 - 4 a c} \right) x \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ \left(-4 a \operatorname{AppellF1} \left[-\frac{1}{3}, -p, -p, \frac{2}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{2}{3}, 1-p, -p, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{2}{3}, -p, 1-p, \frac{5}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right)$$

Problem 266: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x^3} dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$-\frac{1}{2 x^2} \left(1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}} \right)^{-p} \left(1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right)^{-p} \\ (a + b x^3 + c x^6)^p \operatorname{AppellF1} \left[-\frac{2}{3}, -p, -p, \frac{1}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right]$$

Result (type 6, 474 leaves):

$$\left(2^{-2-p} \left(b + \sqrt{b^2 - 4 a c} \right) \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^3 \right) \right. \\ \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^p \left(-2 a + \left(-b + \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 (a + b x^3 + c x^6)^{-1+p} \right. \\ \left. \operatorname{AppellF1} \left[-\frac{2}{3}, -p, -p, \frac{1}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ \left(\left(-b + \sqrt{b^2 - 4 a c} \right) x^2 \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ \left(-2 a \operatorname{AppellF1} \left[-\frac{2}{3}, -p, -p, \frac{1}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{1}{3}, 1-p, -p, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{1}{3}, -p, 1-p, \frac{4}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right)$$

Problem 267: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x^4} dx$$

Optimal (type 6, 164 leaves, 3 steps):

$$-\frac{1}{3(1-2p)x^3} {}_4F_3 \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^{-p} \left(\frac{b + \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^{-p} \\ (a + b x^3 + c x^6)^p \text{AppellF1} \left[1 - 2p, -p, -p, 2(1-p), -\frac{b - \sqrt{b^2 - 4ac}}{2cx^3}, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3} \right]$$

Result (type 6, 510 leaves):

$$\left((-1+p) \left(4 + \frac{2(b - \sqrt{b^2 - 4ac})}{cx^3} \right)^{-p} \left(\frac{b - \sqrt{b^2 - 4ac}}{2c} + x^3 \right)^{-p} \left(-b + \sqrt{b^2 - 4ac} - 2cx^3 \right) \right. \\ \left. \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{c} \right)^p \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^p \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) (a + b x^3 + c x^6)^{-1+p} \right. \\ \left. \text{AppellF1} \left[1 - 2p, -p, -p, 2 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] \right) / \left(3(-1+2p) \right. \\ \left. \left(-4c(-1+p)x^3 \text{AppellF1} \left[1 - 2p, -p, -p, 2 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] + \right. \right. \\ \left. \left(b + \sqrt{b^2 - 4ac} \right)^p \text{AppellF1} \left[2 - 2p, 1 - p, -p, 3 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] + \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4ac} \right)^p \text{AppellF1} \left[2 - 2p, -p, 1 - p, 3 - 2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] \right) \right)$$

Problem 268: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x^5} dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$-\frac{1}{4x^4} \left(1 + \frac{2cx^3}{b - \sqrt{b^2 - 4ac}} \right)^{-p} \left(1 + \frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right)^{-p} \\ (a + b x^3 + c x^6)^p \text{AppellF1} \left[-\frac{4}{3}, -p, -p, -\frac{1}{3}, -\frac{2cx^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^3}{b + \sqrt{b^2 - 4ac}} \right]$$

Result (type 6, 455 leaves):

$$\begin{aligned} & \left(2^{-3-p} c \left(b + \sqrt{b^2 - 4 a c} \right) \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^3 \right)^{-p} \right. \\ & \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^3}{c} \right)^{1+p} \left(-2 a + \left(-b + \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 \left(a + b x^3 + c x^6 \right)^{-1+p} \right. \\ & \left. \text{AppellF1} \left[-\frac{4}{3}, -p, -p, -\frac{1}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left(\left(-b + \sqrt{b^2 - 4 a c} \right) x^4 \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ & \left(2 a \text{AppellF1} \left[-\frac{4}{3}, -p, -p, -\frac{1}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[-\frac{1}{3}, 1-p, -p, \frac{2}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ & \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[-\frac{1}{3}, -p, 1-p, \frac{2}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \end{aligned}$$

Problem 269: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x^6} dx$$

Optimal (type 6, 138 leaves, 2 steps):

$$\begin{aligned} & -\frac{1}{5 x^5} \left(1 + \frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}} \right)^{-p} \left(1 + \frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right)^{-p} \\ & (a + b x^3 + c x^6)^p \text{AppellF1} \left[-\frac{5}{3}, -p, -p, -\frac{2}{3}, -\frac{2 c x^3}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}} \right] \end{aligned}$$

Result (type 6, 411 leaves):

$$\begin{aligned} & \left(\left(b + \sqrt{b^2 - 4 a c} \right) \left(b - \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \left(-2 a + \left(-b + \sqrt{b^2 - 4 a c} \right) x^3 \right)^2 \right. \\ & \left. \left(a + b x^3 + c x^6 \right)^{-1+p} \text{AppellF1} \left[-\frac{5}{3}, -p, -p, -\frac{2}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left(5 \left(-b + \sqrt{b^2 - 4 a c} \right) x^5 \left(b + \sqrt{b^2 - 4 a c} + 2 c x^3 \right) \right. \\ & \left(4 a \text{AppellF1} \left[-\frac{5}{3}, -p, -p, -\frac{2}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\ & \left. 3 p x^3 \left(\left(-b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[-\frac{2}{3}, 1-p, -p, \frac{1}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\ & \left. \left. \left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[-\frac{2}{3}, -p, 1-p, \frac{1}{3}, -\frac{2 c x^3}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^3}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \end{aligned}$$

Problem 270: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^3 + c x^6)^p}{x^7} dx$$

Optimal (type 6, 168 leaves, 3 steps):

$$-\frac{1}{3(1-p)x^6} 2^{-1+2p} \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^{-p} \left(\frac{b + \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^{-p} \\ (a + b x^3 + c x^6)^p \text{AppellF1} \left[2(1-p), -p, -p, 3-2p, -\frac{b - \sqrt{b^2 - 4ac}}{2cx^3}, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3} \right]$$

Result (type 6, 507 leaves):

$$\left(4^{-1-p} c (-3+2p) \left(1 + \frac{b - \sqrt{b^2 - 4ac}}{2cx^3} \right)^{-p} \left(\frac{b - \sqrt{b^2 - 4ac}}{2c} + x^3 \right)^{-p} \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{c} \right)^{1+p} \right. \\ \left. \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^3}{cx^3} \right)^p \left(b + \sqrt{b^2 - 4ac} + 2cx^3 \right) (a + b x^3 + c x^6)^{-1+p} \right. \\ \left. \text{AppellF1} \left[2-2p, -p, -p, 3-2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] \right) / \left(3(-1+p)x^3 \right. \\ \left. \left(2c(-3+2p)x^3 \text{AppellF1} \left[2-2p, -p, -p, 3-2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] - \right. \right. \\ \left. \left. p \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[3-2p, 1-p, -p, 4-2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] + \right. \right. \right. \\ \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[3-2p, -p, 1-p, \right. \right. \right. \\ \left. \left. \left. 4-2p, -\frac{b + \sqrt{b^2 - 4ac}}{2cx^3}, \frac{-b + \sqrt{b^2 - 4ac}}{2cx^3} \right] \right) \right) \right)$$

Problem 309: Result is not expressed in closed-form.

$$\int \frac{x^m}{a + b x^4 + c x^8} dx$$

Optimal (type 5, 163 leaves, 3 steps):

$$\frac{2cx^{1+m} \text{Hypergeometric2F1} \left[1, \frac{1+m}{4}, \frac{5+m}{4}, -\frac{2cx^4}{b - \sqrt{b^2 - 4ac}} \right]}{\sqrt{b^2 - 4ac} (b - \sqrt{b^2 - 4ac}) (1+m)} - \\ \frac{2cx^{1+m} \text{Hypergeometric2F1} \left[1, \frac{1+m}{4}, \frac{5+m}{4}, -\frac{2cx^4}{b + \sqrt{b^2 - 4ac}} \right]}{\sqrt{b^2 - 4ac} (b + \sqrt{b^2 - 4ac}) (1+m)}$$

Result (type 7, 82 leaves):

$$x^m \text{RootSum}\left[a + b x^{1^4} + c x^{1^8}, \frac{\text{Hypergeometric2F1}\left[-m, -m, 1-m, -\frac{1}{x-1}\right] \left(\frac{x}{x-1}\right)^{-m}}{b x^{1^3} + 2 c x^{1^7}}\right] \&$$

4 m

Problem 316: Result is not expressed in closed-form.

$$\int \frac{1}{x (a + b x^4 + c x^8)} dx$$

Optimal (type 3, 69 leaves, 7 steps):

$$\frac{b \text{ArcTanh}\left[\frac{b+2 c x^4}{\sqrt{b^2-4 a c}}\right]}{4 a \sqrt{b^2-4 a c}} + \frac{\text{Log}[x]}{a} - \frac{\text{Log}[a + b x^4 + c x^8]}{8 a}$$

Result (type 7, 66 leaves):

$$\frac{\text{Log}[x]}{a} - \frac{\text{RootSum}\left[a + b x^{1^4} + c x^{1^8}, \frac{b \text{Log}[x-1] + c \text{Log}[x-1] x^{1^4}}{b+2 c x^{1^4}}\right]}{4 a}$$

Problem 317: Result is not expressed in closed-form.

$$\int \frac{1}{x^3 (a + b x^4 + c x^8)} dx$$

Optimal (type 3, 184 leaves, 5 steps):

$$-\frac{1}{2 a x^2} - \frac{\sqrt{c} \left(1 + \frac{b}{\sqrt{b^2-4 a c}}\right) \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{c} x^2}{b - \sqrt{b^2-4 a c}}\right]}{2 \sqrt{2} a \sqrt{b - \sqrt{b^2-4 a c}}} - \frac{\sqrt{c} \left(1 - \frac{b}{\sqrt{b^2-4 a c}}\right) \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{c} x^2}{b + \sqrt{b^2-4 a c}}\right]}{2 \sqrt{2} a \sqrt{b + \sqrt{b^2-4 a c}}}$$

Result (type 7, 75 leaves):

$$-\frac{1}{2 a x^2} - \frac{\text{RootSum}\left[a + b x^{1^4} + c x^{1^8}, \frac{b \text{Log}[x-1] + c \text{Log}[x-1] x^{1^4}}{b x^{1^2} + 2 c x^{1^6}}\right]}{4 a}$$

Problem 318: Result is not expressed in closed-form.

$$\int \frac{1}{x^5 (a + b x^4 + c x^8)} dx$$

Optimal (type 3, 89 leaves, 8 steps):

$$-\frac{1}{4 a x^4} - \frac{(b^2 - 2 a c) \text{ArcTanh}\left[\frac{b+2 c x^4}{\sqrt{b^2-4 a c}}\right]}{4 a^2 \sqrt{b^2-4 a c}} - \frac{b \text{Log}[x]}{a^2} + \frac{b \text{Log}[a + b x^4 + c x^8]}{8 a^2}$$

Result (type 7, 92 leaves):

$$-\frac{1}{4ax^4} - \frac{b \operatorname{Log}[x]}{a^2} + \frac{\operatorname{RootSum}\left[a + b \sqrt[4]{1} + c \sqrt[4]{1}^8 \&, \frac{b^2 \operatorname{Log}[x-\sqrt[4]{1}] - ac \operatorname{Log}[x-\sqrt[4]{1}] + bc \operatorname{Log}[x-\sqrt[4]{1}] \sqrt[4]{1}^4}{b+2c \sqrt[4]{1}} \&\right]}{4a^2}$$

Problem 319: Result is not expressed in closed-form.

$$\int \frac{x^{10}}{a + bx^4 + cx^8} dx$$

Optimal (type 3, 381 leaves, 8 steps):

$$\frac{x^3}{3c} - \frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTan}\left[\frac{2^{1/4}c^{1/4}x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{3/4}c^{7/4}(-b-\sqrt{b^2-4ac})^{1/4}} - \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTan}\left[\frac{2^{1/4}c^{1/4}x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{3/4}c^{7/4}(-b+\sqrt{b^2-4ac})^{1/4}} +$$

$$\frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTanh}\left[\frac{2^{1/4}c^{1/4}x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{3/4}c^{7/4}(-b-\sqrt{b^2-4ac})^{1/4}} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTanh}\left[\frac{2^{1/4}c^{1/4}x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{3/4}c^{7/4}(-b+\sqrt{b^2-4ac})^{1/4}}$$

Result (type 7, 70 leaves):

$$\frac{4x^3 - 3 \operatorname{RootSum}\left[a + b \sqrt[4]{1} + c \sqrt[4]{1}^8 \&, \frac{a \operatorname{Log}[x-\sqrt[4]{1}] + b \operatorname{Log}[x-\sqrt[4]{1}] \sqrt[4]{1}^4}{b \sqrt[4]{1} + 2c \sqrt[4]{1}^5} \&\right]}{12c}$$

Problem 320: Result is not expressed in closed-form.

$$\int \frac{x^8}{a + bx^4 + cx^8} dx$$

Optimal (type 3, 376 leaves, 8 steps):

$$\frac{x}{c} + \frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTan}\left[\frac{2^{1/4}c^{1/4}x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4}c^{5/4}(-b-\sqrt{b^2-4ac})^{3/4}} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTan}\left[\frac{2^{1/4}c^{1/4}x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4}c^{5/4}(-b+\sqrt{b^2-4ac})^{3/4}} +$$

$$\frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTanh}\left[\frac{2^{1/4}c^{1/4}x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4}c^{5/4}(-b-\sqrt{b^2-4ac})^{3/4}} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \operatorname{ArcTanh}\left[\frac{2^{1/4}c^{1/4}x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4}c^{5/4}(-b+\sqrt{b^2-4ac})^{3/4}}$$

Result (type 7, 70 leaves):

$$\frac{x}{c} - \frac{\operatorname{RootSum}\left[a + b \sqrt[4]{1} + c \sqrt[4]{1}^8 \&, \frac{a \operatorname{Log}[x-\sqrt[4]{1}] + b \operatorname{Log}[x-\sqrt[4]{1}] \sqrt[4]{1}^4}{b \sqrt[4]{1}^3 + 2c \sqrt[4]{1}^7} \&\right]}{4c}$$

Problem 321: Result is not expressed in closed-form.

$$\int \frac{x^6}{a+b x^4+c x^8} dx$$

Optimal (type 3, 325 leaves, 7 steps):

$$\frac{\left(-b-\sqrt{b^2-4ac}\right)^{3/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b-\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{3/4} c^{3/4} \sqrt{b^2-4ac}} + \frac{\left(-b+\sqrt{b^2-4ac}\right)^{3/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b+\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{3/4} c^{3/4} \sqrt{b^2-4ac}} +$$

$$\frac{\left(-b-\sqrt{b^2-4ac}\right)^{3/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b-\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{3/4} c^{3/4} \sqrt{b^2-4ac}} - \frac{\left(-b+\sqrt{b^2-4ac}\right)^{3/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b+\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{3/4} c^{3/4} \sqrt{b^2-4ac}}$$

Result (type 7, 44 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[a+b \#1^4+c \#1^8 \&, \frac{\operatorname{Log}[x-\#1] \#1^3}{b+2c \#1^4} \&\right]$$

Problem 322: Result is not expressed in closed-form.

$$\int \frac{x^4}{a+b x^4+c x^8} dx$$

Optimal (type 3, 325 leaves, 7 steps):

$$\frac{\left(-b-\sqrt{b^2-4ac}\right)^{1/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b-\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{1/4} c^{1/4} \sqrt{b^2-4ac}} - \frac{\left(-b+\sqrt{b^2-4ac}\right)^{1/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b+\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{1/4} c^{1/4} \sqrt{b^2-4ac}} +$$

$$\frac{\left(-b-\sqrt{b^2-4ac}\right)^{1/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b-\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{1/4} c^{1/4} \sqrt{b^2-4ac}} - \frac{\left(-b+\sqrt{b^2-4ac}\right)^{1/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{\left(-b+\sqrt{b^2-4ac}\right)^{1/4}}\right]}{2 \times 2^{1/4} c^{1/4} \sqrt{b^2-4ac}}$$

Result (type 7, 42 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[a+b \#1^4+c \#1^8 \&, \frac{\operatorname{Log}[x-\#1] \#1}{b+2c \#1^4} \&\right]$$

Problem 323: Result is not expressed in closed-form.

$$\int \frac{x^2}{a+b x^4+c x^8} dx$$

Optimal (type 3, 315 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{c^{1/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2^{3/4} \sqrt{b^2-4ac} (-b-\sqrt{b^2-4ac})^{1/4}} + \frac{c^{1/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2^{3/4} \sqrt{b^2-4ac} (-b+\sqrt{b^2-4ac})^{1/4}} + \\
 & \frac{c^{1/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2^{3/4} \sqrt{b^2-4ac} (-b-\sqrt{b^2-4ac})^{1/4}} - \frac{c^{1/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2^{3/4} \sqrt{b^2-4ac} (-b+\sqrt{b^2-4ac})^{1/4}}
 \end{aligned}$$

Result (type 7, 43 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[a + b \#1^4 + c \#1^8 \&, \frac{\operatorname{Log}[x - \#1]}{b \#1 + 2 c \#1^5} \&\right]$$

Problem 324: Result is not expressed in closed-form.

$$\int \frac{1}{a + b x^4 + c x^8} dx$$

Optimal (type 3, 315 leaves, 7 steps):

$$\begin{aligned}
 & \frac{c^{3/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2^{1/4} \sqrt{b^2-4ac} (-b-\sqrt{b^2-4ac})^{3/4}} - \frac{c^{3/4} \operatorname{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2^{1/4} \sqrt{b^2-4ac} (-b+\sqrt{b^2-4ac})^{3/4}} + \\
 & \frac{c^{3/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2^{1/4} \sqrt{b^2-4ac} (-b-\sqrt{b^2-4ac})^{3/4}} - \frac{c^{3/4} \operatorname{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2^{1/4} \sqrt{b^2-4ac} (-b+\sqrt{b^2-4ac})^{3/4}}
 \end{aligned}$$

Result (type 7, 45 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[a + b \#1^4 + c \#1^8 \&, \frac{\operatorname{Log}[x - \#1]}{b \#1^3 + 2 c \#1^7} \&\right]$$

Problem 325: Result is not expressed in closed-form.

$$\int \frac{1}{x^2 (a + b x^4 + c x^8)} dx$$

Optimal (type 3, 363 leaves, 8 steps):

$$\frac{1}{a x} - \frac{c^{1/4} \left(1 - \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b - \sqrt{b^2 - 4 a c})^{1/4}}\right] - c^{1/4} \left(1 + \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b + \sqrt{b^2 - 4 a c})^{1/4}}\right]}{2 \times 2^{3/4} a (-b - \sqrt{b^2 - 4 a c})^{1/4} - 2 \times 2^{3/4} a (-b + \sqrt{b^2 - 4 a c})^{1/4}} +$$

$$\frac{c^{1/4} \left(1 - \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b - \sqrt{b^2 - 4 a c})^{1/4}}\right] - c^{1/4} \left(1 + \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b + \sqrt{b^2 - 4 a c})^{1/4}}\right]}{2 \times 2^{3/4} a (-b - \sqrt{b^2 - 4 a c})^{1/4} - 2 \times 2^{3/4} a (-b + \sqrt{b^2 - 4 a c})^{1/4}}$$

Result (type 7, 71 leaves):

$$\frac{1}{a x} - \frac{\text{RootSum}\left[a + b \#1^4 + c \#1^8 \&, \frac{b \text{Log}[x - \#1] + c \text{Log}[x - \#1] \#1^4}{b \#1 + 2 c \#1^5} \&\right]}{4 a}$$

Problem 326: Result is not expressed in closed-form.

$$\int \frac{1}{x^4 (a + b x^4 + c x^8)} dx$$

Optimal (type 3, 365 leaves, 8 steps):

$$\frac{1}{3 a x^3} + \frac{c^{3/4} \left(1 - \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b - \sqrt{b^2 - 4 a c})^{1/4}}\right] - c^{3/4} \left(1 + \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b + \sqrt{b^2 - 4 a c})^{1/4}}\right]}{2 \times 2^{1/4} a (-b - \sqrt{b^2 - 4 a c})^{3/4} - 2 \times 2^{1/4} a (-b + \sqrt{b^2 - 4 a c})^{3/4}} +$$

$$\frac{c^{3/4} \left(1 - \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b - \sqrt{b^2 - 4 a c})^{1/4}}\right] - c^{3/4} \left(1 + \frac{b}{\sqrt{b^2 - 4 a c}}\right) \text{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b + \sqrt{b^2 - 4 a c})^{1/4}}\right]}{2 \times 2^{1/4} a (-b - \sqrt{b^2 - 4 a c})^{3/4} - 2 \times 2^{1/4} a (-b + \sqrt{b^2 - 4 a c})^{3/4}}$$

Result (type 7, 75 leaves):

$$\frac{1}{3 a x^3} - \frac{\text{RootSum}\left[a + b \#1^4 + c \#1^8 \&, \frac{b \text{Log}[x - \#1] + c \text{Log}[x - \#1] \#1^4}{b \#1^3 + 2 c \#1^7} \&\right]}{4 a}$$

Problem 327: Result is not expressed in closed-form.

$$\int \frac{x^m}{1 + x^4 + x^8} dx$$

Optimal (type 5, 127 leaves, 3 steps):

$$\frac{2 x^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, -\frac{2 x^4}{1-i \sqrt{3}}\right]}{\sqrt{3} (i + \sqrt{3}) (1+m)} - \frac{2 x^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, -\frac{2 x^4}{1+i \sqrt{3}}\right]}{\sqrt{3} (i - \sqrt{3}) (1+m)}$$

Result (type 7, 488 leaves):

$$\begin{aligned}
 & \frac{1}{4m} \\
 & x^m \left(-\frac{1}{\sqrt{3}} i \left(\left(\frac{x}{-(-1)^{1/3}+x} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, \frac{(-1)^{1/3}}{(-1)^{1/3}-x} \right] + \left(\frac{x}{-(-1)^{2/3}+x} \right)^{-m} \right. \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[-m, -m, 1-m, \frac{(-1)^{2/3}}{(-1)^{2/3}-x} \right] - \right. \\
 & \quad \left. \left(\frac{x}{(-1)^{1/3}+x} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, \frac{(-1)^{1/3}}{(-1)^{1/3}+x} \right] - \right. \\
 & \quad \left. \left(\frac{x}{(-1)^{2/3}+x} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, \frac{(-1)^{2/3}}{(-1)^{2/3}+x} \right] \right) + \\
 & \text{RootSum} \left[1 - \#1^2 + \#1^4 \&, \frac{\text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{\#1}{x-\#1} \right] \left(\frac{x}{x-\#1} \right)^{-m}}{-\#1 + 2\#1^3} \& \right] - \\
 & \frac{1}{2+3m+m^2} \text{RootSum} \left[1 - \#1^2 + \#1^4 \&, \frac{1}{-\#1 + 2\#1^3} \right. \\
 & \quad \left. \left(m x^2 + m^2 x^2 + 2 m x \#1 + m^2 x \#1 + 2 \text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{\#1}{x-\#1} \right] \left(\frac{x}{x-\#1} \right)^{-m} \#1^2 + \right. \right. \\
 & \quad \left. \left. 3 m \text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{\#1}{x-\#1} \right] \left(\frac{x}{x-\#1} \right)^{-m} \#1^2 + \right. \right. \\
 & \quad \left. \left. m^2 \text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{\#1}{x-\#1} \right] \left(\frac{x}{x-\#1} \right)^{-m} \#1^2 + m \left(\frac{x}{\#1} \right)^{-m} \#1^2 \right) \& \right]
 \end{aligned}$$

Problem 329: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^9}{1+x^4+x^8} dx$$

Optimal (type 3, 54 leaves, 7 steps):

$$\frac{x^2}{2} + \frac{\text{ArcTan} \left[\frac{1-2x^2}{\sqrt{3}} \right]}{2\sqrt{3}} - \frac{\text{ArcTan} \left[\frac{1+2x^2}{\sqrt{3}} \right]}{2\sqrt{3}}$$

Result (type 3, 98 leaves):

$$\frac{x^2}{2} - \frac{(i+\sqrt{3}) \text{ArcTan} \left[\frac{1}{2} (-i+\sqrt{3}) x^2 \right]}{2\sqrt{6+6i\sqrt{3}}} - \frac{(-i+\sqrt{3}) \text{ArcTan} \left[\frac{1}{2} (i+\sqrt{3}) x^2 \right]}{2\sqrt{6-6i\sqrt{3}}}$$

Problem 331: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5}{1+x^4+x^8} dx$$

Optimal (type 3, 75 leaves, 10 steps):

$$-\frac{\text{ArcTan}\left[\frac{1-2x^2}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{\text{ArcTan}\left[\frac{1+2x^2}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{1}{8}\text{Log}[1-x^2+x^4] - \frac{1}{8}\text{Log}[1+x^2+x^4]$$

Result (type 3, 94 leaves):

$$\frac{1}{4\sqrt{6}} \left(\sqrt{1-i\sqrt{3}} (-i+\sqrt{3}) \text{ArcTan}\left[\frac{1}{2}(-i+\sqrt{3})x^2\right] + \sqrt{1+i\sqrt{3}} (i+\sqrt{3}) \text{ArcTan}\left[\frac{1}{2}(i+\sqrt{3})x^2\right] \right)$$

Problem 333: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x}{1+x^4+x^8} dx$$

Optimal (type 3, 75 leaves, 10 steps):

$$-\frac{\text{ArcTan}\left[\frac{1-2x^2}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{\text{ArcTan}\left[\frac{1+2x^2}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{1}{8}\text{Log}[1-x^2+x^4] + \frac{1}{8}\text{Log}[1+x^2+x^4]$$

Result (type 3, 79 leaves):

$$\frac{1}{2\sqrt{6}} i \left(\sqrt{1-i\sqrt{3}} \text{ArcTan}\left[\frac{1}{2}(-i+\sqrt{3})x^2\right] - \sqrt{1+i\sqrt{3}} \text{ArcTan}\left[\frac{1}{2}(i+\sqrt{3})x^2\right] \right)$$

Problem 334: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{1}{x(1+x^4+x^8)} dx$$

Optimal (type 3, 39 leaves, 7 steps):

$$-\frac{\text{ArcTan}\left[\frac{1+2x^4}{\sqrt{3}}\right]}{4\sqrt{3}} + \text{Log}[x] - \frac{1}{8}\text{Log}[1+x^4+x^8]$$

Result (type 3, 138 leaves):

$$\frac{1}{24} \left(2\sqrt{3} \text{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right] - 2\sqrt{3} \text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] + 24\text{Log}[x] - \sqrt{3}(-i+\sqrt{3}) \text{Log}\left[-\frac{1}{2} - \frac{i\sqrt{3}}{2} + x^2\right] - \sqrt{3}(i+\sqrt{3}) \text{Log}\left[\frac{1}{2}i(i+\sqrt{3}) + x^2\right] - 3\text{Log}[1-x+x^2] - 3\text{Log}[1+x+x^2] \right)$$

Problem 335: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{1}{x^3 (1+x^4+x^8)} dx$$

Optimal (type 3, 54 leaves, 7 steps):

$$-\frac{1}{2x^2} + \frac{\text{ArcTan}\left[\frac{1-2x^2}{\sqrt{3}}\right]}{2\sqrt{3}} - \frac{\text{ArcTan}\left[\frac{1+2x^2}{\sqrt{3}}\right]}{2\sqrt{3}}$$

Result (type 3, 100 leaves):

$$\frac{1}{12} \left(-\frac{6}{x^2} - 2\sqrt{3} \text{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right] + 2\sqrt{3} \text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] + \right. \\ \left. i\sqrt{3} \text{Log}[-1-i\sqrt{3}+2x^2] - i\sqrt{3} \text{Log}[-1+i\sqrt{3}+2x^2] \right)$$

Problem 336: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{1}{x^5 (1+x^4+x^8)} dx$$

Optimal (type 3, 48 leaves, 8 steps):

$$-\frac{1}{4x^4} - \frac{\text{ArcTan}\left[\frac{1+2x^4}{\sqrt{3}}\right]}{4\sqrt{3}} - \text{Log}[x] + \frac{1}{8} \text{Log}[1+x^4+x^8]$$

Result (type 3, 141 leaves):

$$\frac{1}{24} \left(-\frac{6}{x^4} + 2\sqrt{3} \text{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right] - \right. \\ \left. 2\sqrt{3} \text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] - 24 \text{Log}[x] + \sqrt{3} (i+\sqrt{3}) \text{Log}\left[-\frac{1}{2} - \frac{i\sqrt{3}}{2} + x^2\right] + \right. \\ \left. \sqrt{3} (-i+\sqrt{3}) \text{Log}\left[\frac{1}{2} i (i+\sqrt{3}) + x^2\right] + 3 \text{Log}[1-x+x^2] + 3 \text{Log}[1+x+x^2] \right)$$

Problem 337: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{1}{x^7 (1+x^4+x^8)} dx$$

Optimal (type 3, 89 leaves, 13 steps):

$$-\frac{1}{6x^6} + \frac{1}{2x^2} - \frac{\text{ArcTan}\left[\frac{1-2x^2}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{\text{ArcTan}\left[\frac{1+2x^2}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{1}{8} \text{Log}[1-x^2+x^4] - \frac{1}{8} \text{Log}[1+x^2+x^4]$$

Result (type 3, 142 leaves):

$$\frac{1}{24} \left(-\frac{4}{x^6} + \frac{12}{x^2} + 2\sqrt{3} \operatorname{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right] - 2\sqrt{3} \operatorname{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] + \sqrt{3}(-i+\sqrt{3}) \operatorname{Log}\left[-\frac{1}{2} - \frac{i\sqrt{3}}{2} + x^2\right] + \sqrt{3}(i+\sqrt{3}) \operatorname{Log}\left[\frac{1}{2}i(i+\sqrt{3}) + x^2\right] - 3 \operatorname{Log}[1-x+x^2] - 3 \operatorname{Log}[1+x+x^2] \right)$$

Problem 338: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^8}{1+x^4+x^8} dx$$

Optimal (type 3, 141 leaves, 20 steps):

$$x + \frac{\operatorname{ArcTan}\left[\frac{1-2x}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}-2x] - \frac{\operatorname{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}+2x] + \frac{1}{8} \operatorname{Log}[1-x+x^2] - \frac{1}{8} \operatorname{Log}[1+x+x^2] + \frac{\operatorname{Log}[1-\sqrt{3}x+x^2]}{8\sqrt{3}} - \frac{\operatorname{Log}[1+\sqrt{3}x+x^2]}{8\sqrt{3}}$$

Result (type 3, 139 leaves):

$$-\frac{i \operatorname{ArcTan}\left[\frac{1}{2}(1-i\sqrt{3})x\right]}{\sqrt{-6+6i\sqrt{3}}} + \frac{i \operatorname{ArcTan}\left[\frac{1}{2}(1+i\sqrt{3})x\right]}{\sqrt{-6-6i\sqrt{3}}} + \frac{1}{24} \left(24x - 2\sqrt{3} \operatorname{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right] - 2\sqrt{3} \operatorname{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] + 3 \operatorname{Log}[1-x+x^2] - 3 \operatorname{Log}[1+x+x^2] \right)$$

Problem 340: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^4}{1+x^4+x^8} dx$$

Optimal (type 3, 140 leaves, 19 steps):

$$\frac{\operatorname{ArcTan}\left[\frac{1-2x}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}-2x] - \frac{\operatorname{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}+2x] - \frac{1}{8} \operatorname{Log}[1-x+x^2] + \frac{1}{8} \operatorname{Log}[1+x+x^2] + \frac{\operatorname{Log}[1-\sqrt{3}x+x^2]}{8\sqrt{3}} - \frac{\operatorname{Log}[1+\sqrt{3}x+x^2]}{8\sqrt{3}}$$

Result (type 3, 135 leaves):

$$\frac{1}{24} \left(-2i \sqrt{-6+6i\sqrt{3}} \operatorname{ArcTan} \left[\frac{1}{2} (1-i\sqrt{3})x \right] + 2i \sqrt{-6-6i\sqrt{3}} \operatorname{ArcTan} \left[\frac{1}{2} (1+i\sqrt{3})x \right] - 2\sqrt{3} \operatorname{ArcTan} \left[\frac{-1+2x}{\sqrt{3}} \right] - 2\sqrt{3} \operatorname{ArcTan} \left[\frac{1+2x}{\sqrt{3}} \right] - 3 \operatorname{Log} [1-x+x^2] + 3 \operatorname{Log} [1+x+x^2] \right)$$

Problem 341: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2}{1+x^4+x^8} dx$$

Optimal (type 3, 140 leaves, 19 steps):

$$\frac{\operatorname{ArcTan} \left[\frac{1-2x}{\sqrt{3}} \right]}{4\sqrt{3}} - \frac{1}{4} \operatorname{ArcTan} [\sqrt{3}-2x] - \frac{\operatorname{ArcTan} \left[\frac{1+2x}{\sqrt{3}} \right]}{4\sqrt{3}} + \frac{1}{4} \operatorname{ArcTan} [\sqrt{3}+2x] + \frac{1}{8} \operatorname{Log} [1-x+x^2] - \frac{1}{8} \operatorname{Log} [1+x+x^2] - \frac{\operatorname{Log} [1-\sqrt{3}x+x^2]}{8\sqrt{3}} + \frac{\operatorname{Log} [1+\sqrt{3}x+x^2]}{8\sqrt{3}}$$

Result (type 3, 135 leaves):

$$\frac{1}{48} \left(4i \sqrt{-6-6i\sqrt{3}} \operatorname{ArcTan} \left[\frac{1}{2} (1-i\sqrt{3})x \right] - 4i \sqrt{-6+6i\sqrt{3}} \operatorname{ArcTan} \left[\frac{1}{2} (1+i\sqrt{3})x \right] - 4\sqrt{3} \operatorname{ArcTan} \left[\frac{-1+2x}{\sqrt{3}} \right] - 4\sqrt{3} \operatorname{ArcTan} \left[\frac{1+2x}{\sqrt{3}} \right] + 6 \operatorname{Log} [1-x+x^2] - 6 \operatorname{Log} [1+x+x^2] \right)$$

Problem 343: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{1}{x^2(1+x^4+x^8)} dx$$

Optimal (type 3, 145 leaves, 20 steps):

$$-\frac{1}{x} + \frac{\operatorname{ArcTan} \left[\frac{1-2x}{\sqrt{3}} \right]}{4\sqrt{3}} + \frac{1}{4} \operatorname{ArcTan} [\sqrt{3}-2x] - \frac{\operatorname{ArcTan} \left[\frac{1+2x}{\sqrt{3}} \right]}{4\sqrt{3}} - \frac{1}{4} \operatorname{ArcTan} [\sqrt{3}+2x] - \frac{1}{8} \operatorname{Log} [1-x+x^2] + \frac{1}{8} \operatorname{Log} [1+x+x^2] - \frac{\operatorname{Log} [1-\sqrt{3}x+x^2]}{8\sqrt{3}} + \frac{\operatorname{Log} [1+\sqrt{3}x+x^2]}{8\sqrt{3}}$$

Result (type 3, 140 leaves):

$$\frac{1}{24} \left(-\frac{24}{x} + 2i \sqrt{-6+6i\sqrt{3}} \operatorname{ArcTan} \left[\frac{1}{2} (1-i\sqrt{3})x \right] - 2i \sqrt{-6-6i\sqrt{3}} \operatorname{ArcTan} \left[\frac{1}{2} (1+i\sqrt{3})x \right] - 2\sqrt{3} \operatorname{ArcTan} \left[\frac{-1+2x}{\sqrt{3}} \right] - 2\sqrt{3} \operatorname{ArcTan} \left[\frac{1+2x}{\sqrt{3}} \right] - 3 \operatorname{Log} [1-x+x^2] + 3 \operatorname{Log} [1+x+x^2] \right)$$

Problem 344: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{1}{x^4 (1+x^4+x^8)} dx$$

Optimal (type 3, 147 leaves, 20 steps):

$$-\frac{1}{3x^3} + \frac{\text{ArcTan}\left[\frac{1-2x}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{1}{4} \text{ArcTan}[\sqrt{3}-2x] - \frac{\text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{1}{4} \text{ArcTan}[\sqrt{3}+2x] +$$

$$\frac{1}{8} \text{Log}[1-x+x^2] - \frac{1}{8} \text{Log}[1+x+x^2] + \frac{\text{Log}[1-\sqrt{3}x+x^2]}{8\sqrt{3}} - \frac{\text{Log}[1+\sqrt{3}x+x^2]}{8\sqrt{3}}$$

Result (type 3, 148 leaves):

$$\frac{1}{24} \left(-\frac{8}{x^3} - \frac{4i \text{ArcTan}\left[\frac{1}{2}(1-i\sqrt{3})x\right]}{\sqrt{\frac{1}{6}i(i+\sqrt{3})}} + \frac{4i \text{ArcTan}\left[\frac{1}{2}(1+i\sqrt{3})x\right]}{\sqrt{-\frac{1}{6}i(-i+\sqrt{3})}} - \right.$$

$$\left. 2\sqrt{3} \text{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right] - 2\sqrt{3} \text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] + 3 \text{Log}[1-x+x^2] - 3 \text{Log}[1+x+x^2] \right)$$

Problem 346: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{1}{x^8 (1+x^4+x^8)} dx$$

Optimal (type 3, 154 leaves, 22 steps):

$$-\frac{1}{7x^7} + \frac{1}{3x^3} + \frac{\text{ArcTan}\left[\frac{1-2x}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{1}{4} \text{ArcTan}[\sqrt{3}-2x] - \frac{\text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{4\sqrt{3}} + \frac{1}{4} \text{ArcTan}[\sqrt{3}+2x] -$$

$$\frac{1}{8} \text{Log}[1-x+x^2] + \frac{1}{8} \text{Log}[1+x+x^2] + \frac{\text{Log}[1-\sqrt{3}x+x^2]}{8\sqrt{3}} - \frac{\text{Log}[1+\sqrt{3}x+x^2]}{8\sqrt{3}}$$

Result (type 3, 171 leaves):

$$-\frac{1}{7x^7} + \frac{1}{3x^3} + \frac{(i+\sqrt{3}) \text{ArcTan}\left[\frac{1}{2}(1-i\sqrt{3})x\right]}{2\sqrt{-6+6i\sqrt{3}}} + \frac{(-i+\sqrt{3}) \text{ArcTan}\left[\frac{1}{2}(1+i\sqrt{3})x\right]}{2\sqrt{-6-6i\sqrt{3}}} -$$

$$\frac{\text{ArcTan}\left[\frac{-1+2x}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{\text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{4\sqrt{3}} - \frac{1}{8} \text{Log}[1-x+x^2] + \frac{1}{8} \text{Log}[1+x+x^2]$$

Problem 347: Result is not expressed in closed-form.

$$\int \frac{x^m}{1-x^4+x^8} dx$$

Optimal (type 5, 127 leaves, 3 steps):

$$\frac{2 x^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, \frac{2 x^4}{1-i \sqrt{3}}\right]}{\sqrt{3} (i+\sqrt{3}) (1+m)} - \frac{2 x^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, \frac{2 x^4}{1+i \sqrt{3}}\right]}{\sqrt{3} (i-\sqrt{3}) (1+m)}$$

Result (type 7, 79 leaves):

$$\frac{x^m \text{RootSum}\left[1-i t^4+i t^8 \&, \frac{\text{Hypergeometric2F1}\left[-m,-m,1-m,-\frac{m+1}{x-i}\right]\left(\frac{x}{x-i}\right)^{-m}}{-i t^3+2 i t^7} \&\right]}{4 m}$$

Problem 351: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5}{1-x^4+x^8} dx$$

Optimal (type 3, 82 leaves, 10 steps):

$$-\frac{1}{4} \text{ArcTan}\left[\sqrt{3}-2 x^2\right] + \frac{1}{4} \text{ArcTan}\left[\sqrt{3}+2 x^2\right] + \frac{\text{Log}\left[1-\sqrt{3} x^2+x^4\right]}{8 \sqrt{3}} - \frac{\text{Log}\left[1+\sqrt{3} x^2+x^4\right]}{8 \sqrt{3}}$$

Result (type 3, 98 leaves):

$$\frac{1}{4 \sqrt{6}} \left(\sqrt{-1-i \sqrt{3}} (i+\sqrt{3}) \text{ArcTan}\left[\frac{1}{2} (1-i \sqrt{3}) x^2\right] + \sqrt{-1+i \sqrt{3}} (-i+\sqrt{3}) \text{ArcTan}\left[\frac{1}{2} (1+i \sqrt{3}) x^2\right] \right)$$

Problem 353: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x}{1-x^4+x^8} dx$$

Optimal (type 3, 82 leaves, 10 steps):

$$-\frac{1}{4} \text{ArcTan}\left[\sqrt{3}-2 x^2\right] + \frac{1}{4} \text{ArcTan}\left[\sqrt{3}+2 x^2\right] - \frac{\text{Log}\left[1-\sqrt{3} x^2+x^4\right]}{8 \sqrt{3}} + \frac{\text{Log}\left[1+\sqrt{3} x^2+x^4\right]}{8 \sqrt{3}}$$

Result (type 3, 83 leaves):

$$\frac{1}{2 \sqrt{6}} i \left(\sqrt{-1-i \sqrt{3}} \text{ArcTan}\left[\frac{1}{2} (1-i \sqrt{3}) x^2\right] - \sqrt{-1+i \sqrt{3}} \text{ArcTan}\left[\frac{1}{2} (1+i \sqrt{3}) x^2\right] \right)$$

Problem 354: Result is not expressed in closed-form.

$$\int \frac{1}{x(1-x^4+x^8)} dx$$

Optimal (type 3, 41 leaves, 7 steps):

$$-\frac{\text{ArcTan}\left[\frac{1-2x^4}{\sqrt{3}}\right]}{4\sqrt{3}} + \text{Log}[x] - \frac{1}{8} \text{Log}[1-x^4+x^8]$$

Result (type 7, 55 leaves):

$$\text{Log}[x] - \frac{1}{4} \text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{-\text{Log}[x - \#1] + \text{Log}[x - \#1] \#1^4}{-1 + 2 \#1^4} \&\right]$$

Problem 356: Result is not expressed in closed-form.

$$\int \frac{1}{x^5(1-x^4+x^8)} dx$$

Optimal (type 3, 48 leaves, 8 steps):

$$-\frac{1}{4x^4} + \frac{\text{ArcTan}\left[\frac{1-2x^4}{\sqrt{3}}\right]}{4\sqrt{3}} + \text{Log}[x] - \frac{1}{8} \text{Log}[1-x^4+x^8]$$

Result (type 7, 51 leaves):

$$-\frac{1}{4x^4} + \text{Log}[x] - \frac{1}{4} \text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\text{Log}[x - \#1] \#1^4}{-1 + 2 \#1^4} \&\right]$$

Problem 357: Result is not expressed in closed-form.

$$\int \frac{1}{x^7(1-x^4+x^8)} dx$$

Optimal (type 3, 96 leaves, 13 steps):

$$-\frac{1}{6x^6} - \frac{1}{2x^2} + \frac{1}{4} \text{ArcTan}[\sqrt{3} - 2x^2] - \frac{1}{4} \text{ArcTan}[\sqrt{3} + 2x^2] - \frac{\text{Log}[1 - \sqrt{3}x^2 + x^4]}{8\sqrt{3}} + \frac{\text{Log}[1 + \sqrt{3}x^2 + x^4]}{8\sqrt{3}}$$

Result (type 7, 56 leaves):

$$-\frac{1}{6x^6} - \frac{1}{2x^2} - \frac{1}{4} \text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\text{Log}[x - \#1] \#1^2}{-1 + 2 \#1^4} \&\right]$$

Problem 358: Result is not expressed in closed-form.

$$\int \frac{x^8}{1-x^4+x^8} dx$$

Optimal (type 3, 356 leaves, 20 steps):

$$\begin{aligned}
 & x + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} - \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} - \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} \\
 & \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\operatorname{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right] + \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\operatorname{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right] + \\
 & \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\operatorname{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right] - \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\operatorname{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]
 \end{aligned}$$

Result (type 7, 59 leaves):

$$x + \frac{1}{4}\operatorname{RootSum}\left[1-\#1^4+\#1^8 \&, \frac{-\operatorname{Log}[x-\#1]+\operatorname{Log}[x-\#1]\#1^4}{-\#1^3+2\#1^7} \&\right]$$

Problem 359: Result is not expressed in closed-form.

$$\int \frac{x^6}{1-x^4+x^8} dx$$

Optimal (type 3, 275 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{\operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{2\sqrt{6}} - \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{2\sqrt{6}} + \\
 & \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{2\sqrt{6}} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{2\sqrt{6}} + \frac{\operatorname{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right]}{4\sqrt{6}} - \\
 & \frac{\operatorname{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right]}{4\sqrt{6}} + \frac{\operatorname{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right]}{4\sqrt{6}} - \frac{\operatorname{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]}{4\sqrt{6}}
 \end{aligned}$$

Result (type 7, 41 leaves):

$$\frac{1}{4}\operatorname{RootSum}\left[1-\#1^4+\#1^8 \&, \frac{\operatorname{Log}[x-\#1]\#1^3}{-1+2\#1^4} \&\right]$$

Problem 360: Result is not expressed in closed-form.

$$\int \frac{x^4}{1-x^4+x^8} dx$$

Optimal (type 3, 347 leaves, 19 steps):

$$\frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} -$$

$$\frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} - \frac{\text{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right]}{8\sqrt{3(2-\sqrt{3})}} +$$

$$\frac{\text{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right]}{8\sqrt{3(2-\sqrt{3})}} + \frac{\text{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right]}{8\sqrt{3(2+\sqrt{3})}} - \frac{\text{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]}{8\sqrt{3(2+\sqrt{3})}}$$

Result (type 7, 39 leaves):

$$\frac{1}{4} \text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\text{Log}[x - \#1] \#1}{-1 + 2 \#1^4} \&\right]$$

Problem 361: Result is not expressed in closed-form.

$$\int \frac{x^2}{1-x^4+x^8} dx$$

Optimal (type 3, 355 leaves, 19 steps):

$$\frac{1}{4} \sqrt{\frac{1}{3} (2 - \sqrt{3})} \operatorname{ArcTan}\left[\frac{\sqrt{2 - \sqrt{3}} - 2x}{\sqrt{2 + \sqrt{3}}}\right] -$$

$$\frac{1}{4} \sqrt{\frac{1}{3} (2 + \sqrt{3})} \operatorname{ArcTan}\left[\frac{\sqrt{2 + \sqrt{3}} - 2x}{\sqrt{2 - \sqrt{3}}}\right] - \frac{1}{4} \sqrt{\frac{1}{3} (2 - \sqrt{3})} \operatorname{ArcTan}\left[\frac{\sqrt{2 - \sqrt{3}} + 2x}{\sqrt{2 + \sqrt{3}}}\right] +$$

$$\frac{1}{4} \sqrt{\frac{1}{3} (2 + \sqrt{3})} \operatorname{ArcTan}\left[\frac{\sqrt{2 + \sqrt{3}} + 2x}{\sqrt{2 - \sqrt{3}}}\right] + \frac{\operatorname{Log}[1 - \sqrt{2 - \sqrt{3}} x + x^2]}{8 \sqrt{3} (2 - \sqrt{3})} -$$

$$\frac{\operatorname{Log}[1 + \sqrt{2 - \sqrt{3}} x + x^2]}{8 \sqrt{3} (2 - \sqrt{3})} - \frac{\operatorname{Log}[1 - \sqrt{2 + \sqrt{3}} x + x^2]}{8 \sqrt{3} (2 + \sqrt{3})} + \frac{\operatorname{Log}[1 + \sqrt{2 + \sqrt{3}} x + x^2]}{8 \sqrt{3} (2 + \sqrt{3})}$$

Result (type 7, 40 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\operatorname{Log}[x - \#1]}{-\#1 + 2 \#1^5} \&\right]$$

Problem 362: Result is not expressed in closed-form.

$$\int \frac{1}{1 - x^4 + x^8} dx$$

Optimal (type 3, 275 leaves, 19 steps):

$$-\frac{\operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{2\sqrt{6}} - \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{2\sqrt{6}} +$$

$$\frac{\operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{2\sqrt{6}} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{2\sqrt{6}} - \frac{\operatorname{Log}[1 - \sqrt{2 - \sqrt{3}} x + x^2]}{4\sqrt{6}} +$$

$$\frac{\operatorname{Log}[1 + \sqrt{2 - \sqrt{3}} x + x^2]}{4\sqrt{6}} - \frac{\operatorname{Log}[1 - \sqrt{2 + \sqrt{3}} x + x^2]}{4\sqrt{6}} + \frac{\operatorname{Log}[1 + \sqrt{2 + \sqrt{3}} x + x^2]}{4\sqrt{6}}$$

Result (type 7, 42 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\operatorname{Log}[x - \#1]}{-\#1^3 + 2 \#1^7} \&\right]$$

Problem 363: Result is not expressed in closed-form.

$$\int \frac{1}{x^2 (1 - x^4 + x^8)} dx$$

Optimal (type 3, 360 leaves, 22 steps):

$$\begin{aligned}
 & -\frac{1}{x} + \frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} + \\
 & \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right] - \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right] - \\
 & \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right] + \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]
 \end{aligned}$$

Result (type 7, 61 leaves):

$$-\frac{1}{x} - \frac{1}{4}\text{RootSum}\left[1-\#1^4+\#1^8\ \&, \frac{-\text{Log}[x-\#1]+\text{Log}[x-\#1]\#1^4}{-\#1+2\#1^5}\ \&\right]$$

Problem 364: Result is not expressed in closed-form.

$$\int \frac{1}{x^4(1-x^4+x^8)} dx$$

Optimal (type 3, 370 leaves, 20 steps):

$$\begin{aligned}
 & -\frac{1}{3x^3} - \frac{1}{4}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right] + \frac{1}{4}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right] + \\
 & \frac{1}{4}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right] - \frac{1}{4}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right] + \\
 & \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right] - \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right] - \\
 & \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right] + \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]
 \end{aligned}$$

Result (type 7, 65 leaves):

$$-\frac{1}{3x^3} - \frac{1}{4}\text{RootSum}\left[1-\#1^4+\#1^8\ \&, \frac{-\text{Log}[x-\#1]+\text{Log}[x-\#1]\#1^4}{-\#1^3+2\#1^7}\ \&\right]$$

Problem 365: Result is not expressed in closed-form.

$$\int \frac{1}{x^6(1-x^4+x^8)} dx$$

Optimal (type 3, 287 leaves, 22 steps):

$$\begin{aligned}
 & -\frac{1}{5x^5} - \frac{1}{x} + \frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{2\sqrt{6}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{2\sqrt{6}} - \\
 & \frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{2\sqrt{6}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{2\sqrt{6}} - \frac{\text{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right]}{4\sqrt{6}} + \\
 & \frac{\text{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right]}{4\sqrt{6}} - \frac{\text{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right]}{4\sqrt{6}} + \frac{\text{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]}{4\sqrt{6}}
 \end{aligned}$$

Result (type 7, 54 leaves):

$$-\frac{1}{5x^5} - \frac{1}{x} - \frac{1}{4} \text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\text{Log}[x - \#1] \#1^3}{-1 + 2\#1^4} \&\right]$$

Problem 366: Result is not expressed in closed-form.

$$\int \frac{1}{x^8 (1-x^4+x^8)} dx$$

Optimal (type 3, 377 leaves, 22 steps):

$$\begin{aligned}
 & -\frac{1}{7x^7} - \frac{1}{3x^3} - \frac{1}{4} \sqrt{\frac{1}{3}(2-\sqrt{3})} \text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right] + \\
 & \frac{1}{4} \sqrt{\frac{1}{3}(2+\sqrt{3})} \text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right] + \\
 & \frac{1}{4} \sqrt{\frac{1}{3}(2-\sqrt{3})} \text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right] - \frac{1}{4} \sqrt{\frac{1}{3}(2+\sqrt{3})} \text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right] + \\
 & \frac{1}{8} \sqrt{\frac{1}{3}(2+\sqrt{3})} \text{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right] - \frac{1}{8} \sqrt{\frac{1}{3}(2+\sqrt{3})} \text{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right] - \\
 & \frac{1}{8} \sqrt{\frac{1}{3}(2-\sqrt{3})} \text{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right] + \frac{1}{8} \sqrt{\frac{1}{3}(2-\sqrt{3})} \text{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right]
 \end{aligned}$$

Result (type 7, 54 leaves):

$$-\frac{1}{7x^7} - \frac{1}{3x^3} - \frac{1}{4} \text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{\text{Log}[x - \#1] \#1}{-1 + 2\#1^4} \&\right]$$

Problem 367: Result is not expressed in closed-form.

$$\int \frac{x^m}{1+3x^4+x^8} dx$$

Optimal (type 5, 117 leaves, 3 steps):

$$\frac{2 x^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, -\frac{2 x^4}{3-\sqrt{5}}\right]}{\sqrt{5} (3-\sqrt{5}) (1+m)} - \frac{2 x^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, -\frac{2 x^4}{3+\sqrt{5}}\right]}{\sqrt{5} (3+\sqrt{5}) (1+m)}$$

Result (type 7, 79 leaves):

$$\frac{x^m \text{RootSum}\left[1+3 \#1^4+\#1^8 \&, \frac{\text{Hypergeometric2F1}\left[-m,-m,1-m,-\frac{\#1}{x-\#1}\right]\left(\frac{x}{x-\#1}\right)^{-m}}{3 \#1^3+2 \#1^7} \&\right]}{4 m}$$

Problem 375: Result is not expressed in closed-form.

$$\int \frac{1}{x^3 (1+3x^4+x^8)} dx$$

Optimal (type 3, 89 leaves, 5 steps):

$$-\frac{1}{2 x^2} + \frac{1}{2} \sqrt{\frac{1}{5} (9-4 \sqrt{5})} \text{ArcTan}\left[\sqrt{\frac{2}{3+\sqrt{5}}} x^2\right] - \frac{(3+\sqrt{5})^{3/2} \text{ArcTan}\left[\sqrt{\frac{1}{2} (3+\sqrt{5})} x^2\right]}{4 \sqrt{10}}$$

Result (type 7, 65 leaves):

$$-\frac{1}{2 x^2} - \frac{1}{4} \text{RootSum}\left[1+3 \#1^4+\#1^8 \&, \frac{3 \text{Log}[x-\#1] + \text{Log}[x-\#1] \#1^4}{3 \#1^2+2 \#1^6} \&\right]$$

Problem 377: Result is not expressed in closed-form.

$$\int \frac{1}{x^7 (1+3x^4+x^8)} dx$$

Optimal (type 3, 97 leaves, 6 steps):

$$-\frac{1}{6 x^6} + \frac{3}{2 x^2} - \frac{1}{2} \sqrt{\frac{1}{10} (123-55 \sqrt{5})} \text{ArcTan}\left[\sqrt{\frac{2}{3+\sqrt{5}}} x^2\right] +$$

$$\frac{1}{2} \sqrt{\frac{1}{10} (123+55 \sqrt{5})} \text{ArcTan}\left[\sqrt{\frac{1}{2} (3+\sqrt{5})} x^2\right]$$

Result (type 7, 73 leaves):

$$-\frac{1}{6 x^6} + \frac{3}{2 x^2} + \frac{1}{4} \text{RootSum}\left[1+3 \#1^4+\#1^8 \&, \frac{8 \text{Log}[x-\#1] + 3 \text{Log}[x-\#1] \#1^4}{3 \#1^2+2 \#1^6} \&\right]$$

Problem 378: Result is not expressed in closed-form.

$$\int \frac{x^8}{1 + 3x^4 + x^8} dx$$

Optimal (type 3, 460 leaves, 20 steps):

$$\begin{aligned} x & - \frac{\left(123 - 55\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} + \frac{\left(123 - 55\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} + \\ & - \frac{\left(123 + 55\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} - \frac{\left(123 + 55\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} - \\ & + \frac{\left(123 - 55\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5}) - 2(2(3-\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4}\sqrt{5}} + \\ & + \frac{\left(123 - 55\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5}) + 2(2(3-\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4}\sqrt{5}} + \\ & - \frac{\left(123 + 55\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5}) - 2(2(3+\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4}\sqrt{5}} - \\ & - \frac{\left(123 + 55\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5}) + 2(2(3+\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4}\sqrt{5}} \end{aligned}$$

Result (type 7, 58 leaves):

$$x - \frac{1}{4} \operatorname{RootSum}\left[1 + 3 \#1^4 + \#1^8 \&, \frac{\operatorname{Log}[x - \#1] + 3 \operatorname{Log}[x - \#1] \#1^4}{3 \#1^3 + 2 \#1^7} \&\right]$$

Problem 379: Result is not expressed in closed-form.

$$\int \frac{x^6}{1 + 3x^4 + x^8} dx$$

Optimal (type 3, 431 leaves, 19 steps):

$$\begin{aligned}
& \frac{(9-4\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2\sqrt{10}} - \frac{(9-4\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2\sqrt{10}} - \\
& \frac{(3+\sqrt{5})^{3/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{4 \times 2^{1/4} \sqrt{5}} + \frac{(3+\sqrt{5})^{3/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{4 \times 2^{1/4} \sqrt{5}} - \\
& \frac{(9-4\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})} - 2(2(3-\sqrt{5}))^{1/4}x + 2x^2\right]}{4\sqrt{10}} + \\
& \frac{(9-4\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})} + 2(2(3-\sqrt{5}))^{1/4}x + 2x^2\right]}{4\sqrt{10}} + \\
& \frac{(3+\sqrt{5})^{3/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})} - 2(2(3+\sqrt{5}))^{1/4}x + 2x^2\right]}{8 \times 2^{1/4} \sqrt{5}} - \\
& \frac{(3+\sqrt{5})^{3/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})} + 2(2(3+\sqrt{5}))^{1/4}x + 2x^2\right]}{8 \times 2^{1/4} \sqrt{5}}
\end{aligned}$$

Result (type 7, 41 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1 + 3\#1^4 + \#1^8 \&, \frac{\operatorname{Log}[x - \#1] \#1^3}{3 + 2\#1^4} \&\right]$$

Problem 380: Result is not expressed in closed-form.

$$\int \frac{x^4}{1 + 3x^4 + x^8} dx$$

Optimal (type 3, 451 leaves, 19 steps):

$$\begin{aligned}
 & \frac{(3-\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} - \frac{(3-\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} - \\
 & \frac{(3+\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} + \frac{(3+\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} + \\
 & \frac{(3-\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5}) - 2(2(3-\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4} \sqrt{5}} - \\
 & \frac{(3-\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5}) + 2(2(3-\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4} \sqrt{5}} - \\
 & \frac{(3+\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5}) - 2(2(3+\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4} \sqrt{5}} + \\
 & \frac{(3+\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5}) + 2(2(3+\sqrt{5}))^{1/4}x + 2x^2}\right]}{4 \times 2^{3/4} \sqrt{5}}
 \end{aligned}$$

Result (type 7, 39 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1 + 3 \#1^4 + \#1^8 \&, \frac{\operatorname{Log}[x - \#1] \#1}{3 + 2 \#1^4} \&\right]$$

Problem 381: Result is not expressed in closed-form.

$$\int \frac{x^2}{1 + 3x^4 + x^8} dx$$

Optimal (type 3, 427 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{\operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2\sqrt{5} (2(3-\sqrt{5}))^{1/4}} + \frac{\operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2\sqrt{5} (2(3-\sqrt{5}))^{1/4}} + \frac{\operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2\sqrt{5} (2(3+\sqrt{5}))^{1/4}} - \frac{\operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2\sqrt{5} (2(3+\sqrt{5}))^{1/4}} + \\
 & \frac{\operatorname{Log}\left[\sqrt{2(3-\sqrt{5}) - 2(2(3-\sqrt{5}))^{1/4}x + 2x^2}\right]}{4\sqrt{5} (2(3-\sqrt{5}))^{1/4}} - \frac{\operatorname{Log}\left[\sqrt{2(3-\sqrt{5}) + 2(2(3-\sqrt{5}))^{1/4}x + 2x^2}\right]}{4\sqrt{5} (2(3-\sqrt{5}))^{1/4}} - \\
 & \frac{\operatorname{Log}\left[\sqrt{2(3+\sqrt{5}) - 2(2(3+\sqrt{5}))^{1/4}x + 2x^2}\right]}{4\sqrt{5} (2(3+\sqrt{5}))^{1/4}} + \frac{\operatorname{Log}\left[\sqrt{2(3+\sqrt{5}) + 2(2(3+\sqrt{5}))^{1/4}x + 2x^2}\right]}{4\sqrt{5} (2(3+\sqrt{5}))^{1/4}}
 \end{aligned}$$

Result (type 7, 40 leaves):

$$\frac{1}{4} \text{RootSum}\left[1 + 3 \sqrt[4]{1} + \sqrt[4]{1}^8 \&, \frac{\text{Log}[x - \sqrt[4]{1}]}{3 \sqrt[4]{1} + 2 \sqrt[4]{1}^5} \&\right]$$

Problem 382: Result is not expressed in closed-form.

$$\int \frac{1}{1 + 3x^4 + x^8} dx$$

Optimal (type 3, 414 leaves, 19 steps):

$$\begin{aligned} & - \frac{(9 + 4\sqrt{5})^{1/4} \text{ArcTan}\left[1 - \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2\sqrt{10}} + \\ & \frac{(9 + 4\sqrt{5})^{1/4} \text{ArcTan}\left[1 + \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2\sqrt{10}} + \frac{\text{ArcTan}\left[1 - \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{\sqrt{5} (2(3+\sqrt{5}))^{3/4}} - \frac{\text{ArcTan}\left[1 + \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{\sqrt{5} (2(3+\sqrt{5}))^{3/4}} - \\ & \frac{(9 + 4\sqrt{5})^{1/4} \text{Log}\left[\sqrt{2(3-\sqrt{5})} - 2(2(3-\sqrt{5}))^{1/4}x + 2x^2\right]}{4\sqrt{10}} + \\ & \frac{(9 + 4\sqrt{5})^{1/4} \text{Log}\left[\sqrt{2(3-\sqrt{5})} + 2(2(3-\sqrt{5}))^{1/4}x + 2x^2\right]}{4\sqrt{10}} + \\ & \frac{\text{Log}\left[\sqrt{2(3+\sqrt{5})} - 2(2(3+\sqrt{5}))^{1/4}x + 2x^2\right]}{2\sqrt{5} (2(3+\sqrt{5}))^{3/4}} - \frac{\text{Log}\left[\sqrt{2(3+\sqrt{5})} + 2(2(3+\sqrt{5}))^{1/4}x + 2x^2\right]}{2\sqrt{5} (2(3+\sqrt{5}))^{3/4}} \end{aligned}$$

Result (type 7, 42 leaves):

$$\frac{1}{4} \text{RootSum}\left[1 + 3 \sqrt[4]{1} + \sqrt[4]{1}^8 \&, \frac{\text{Log}[x - \sqrt[4]{1}]}{3 \sqrt[4]{1}^3 + 2 \sqrt[4]{1}^7} \&\right]$$

Problem 383: Result is not expressed in closed-form.

$$\int \frac{1}{x^2 (1 + 3x^4 + x^8)} dx$$

Optimal (type 3, 416 leaves, 20 steps):

$$\begin{aligned}
 & -\frac{1}{x} + \frac{(3 + \sqrt{5})^{5/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4} x}{(3 - \sqrt{5})^{1/4}}\right]}{4 \times 2^{3/4} \sqrt{5}} - \\
 & \frac{(3 + \sqrt{5})^{5/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4} x}{(3 - \sqrt{5})^{1/4}}\right]}{4 \times 2^{3/4} \sqrt{5}} - \frac{1}{20} (6150 - 2750 \sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4} x}{(3 + \sqrt{5})^{1/4}}\right] + \\
 & \frac{1}{20} (6150 - 2750 \sqrt{5})^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4} x}{(3 + \sqrt{5})^{1/4}}\right] - \\
 & \frac{(3 + \sqrt{5})^{5/4} \operatorname{Log}\left[\sqrt{2(3 - \sqrt{5})} - 2(2(3 - \sqrt{5}))^{1/4} x + 2x^2\right]}{8 \times 2^{3/4} \sqrt{5}} + \\
 & \frac{(3 + \sqrt{5})^{5/4} \operatorname{Log}\left[\sqrt{2(3 - \sqrt{5})} + 2(2(3 - \sqrt{5}))^{1/4} x + 2x^2\right]}{8 \times 2^{3/4} \sqrt{5}} + \\
 & \frac{1}{40} (6150 - 2750 \sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3 + \sqrt{5})} - 2(2(3 + \sqrt{5}))^{1/4} x + 2x^2\right] - \\
 & \frac{1}{40} (6150 - 2750 \sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3 + \sqrt{5})} + 2(2(3 + \sqrt{5}))^{1/4} x + 2x^2\right]
 \end{aligned}$$

Result (type 7, 61 leaves):

$$-\frac{1}{x} - \frac{1}{4} \operatorname{RootSum}\left[1 + 3 \#1^4 + \#1^8 \&, \frac{3 \operatorname{Log}[x - \#1] + \operatorname{Log}[x - \#1] \#1^4}{3 \#1 + 2 \#1^5} \&\right]$$

Problem 384: Result is not expressed in closed-form.

$$\int \frac{1}{x^4 (1 + 3x^4 + x^8)} dx$$

Optimal (type 3, 466 leaves, 20 steps):

$$\begin{aligned}
& -\frac{1}{3x^3} + \frac{\left(843 + 377\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} - \frac{\left(843 + 377\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} \\
& \frac{\left(843 - 377\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 - \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} + \frac{\left(843 - 377\sqrt{5}\right)^{1/4} \operatorname{ArcTan}\left[1 + \frac{2^{3/4}x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}\sqrt{5}} + \\
& \frac{\left(843 + 377\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})} - 2\left(2(3-\sqrt{5})\right)^{1/4}x + 2x^2\right]}{4 \times 2^{3/4}\sqrt{5}} - \\
& \frac{\left(843 + 377\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})} + 2\left(2(3-\sqrt{5})\right)^{1/4}x + 2x^2\right]}{4 \times 2^{3/4}\sqrt{5}} - \\
& \frac{\left(843 - 377\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})} - 2\left(2(3+\sqrt{5})\right)^{1/4}x + 2x^2\right]}{4 \times 2^{3/4}\sqrt{5}} + \\
& \frac{\left(843 - 377\sqrt{5}\right)^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})} + 2\left(2(3+\sqrt{5})\right)^{1/4}x + 2x^2\right]}{4 \times 2^{3/4}\sqrt{5}}
\end{aligned}$$

Result (type 7, 65 leaves):

$$-\frac{1}{3x^3} - \frac{1}{4} \operatorname{RootSum}\left[1 + 3\#1^4 + \#1^8 \&, \frac{3 \operatorname{Log}[x - \#1] + \operatorname{Log}[x - \#1] \#1^4}{3\#1^3 + 2\#1^7} \&\right]$$

Problem 385: Result is not expressed in closed-form.

$$\int \frac{x^m}{1 - 3x^4 + x^8} dx$$

Optimal (type 5, 117 leaves, 3 steps):

$$\frac{2x^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, \frac{2x^4}{3-\sqrt{5}}\right]}{\sqrt{5}(3-\sqrt{5})(1+m)} - \frac{2x^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{4}, \frac{5+m}{4}, \frac{2x^4}{3+\sqrt{5}}\right]}{\sqrt{5}(3+\sqrt{5})(1+m)}$$

Result (type 7, 575 leaves):

$$\frac{1}{4m} x^m \left(-\text{RootSum}[-1 - \#1^2 + \#1^4 \&, \frac{\text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}]}{-\#1 + 2\#1^3} \left(\frac{x}{x-\#1}\right)^{-m} \&] + \frac{1}{2 + 3m + m^2} \right. \\ \left. \left(\text{RootSum}[-1 - \#1^2 + \#1^4 \&, \frac{1}{-\#1 + 2\#1^3} \left(m x^2 + m^2 x^2 + 2 m x \#1 + m^2 x \#1 + 2 \text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}] \left(\frac{x}{x-\#1}\right)^{-m} \#1^2 + 3 m \text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}] \left(\frac{x}{x-\#1}\right)^{-m} \#1^2 + m^2 \text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}] \left(\frac{x}{x-\#1}\right)^{-m} \#1^2 + m \left(\frac{x}{\#1}\right)^{-m} \#1^2 \right) \&] - (2 + 3m + m^2) \text{RootSum}[-1 + \#1^2 + \#1^4 \&, \frac{\text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}]}{\#1 + 2\#1^3} \left(\frac{x}{x-\#1}\right)^{-m} \&] - \text{RootSum}[-1 + \#1^2 + \#1^4 \&, \frac{1}{\#1 + 2\#1^3} \left(m x^2 + m^2 x^2 + 2 m x \#1 + m^2 x \#1 + 2 \text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}] \left(\frac{x}{x-\#1}\right)^{-m} \#1^2 + 3 m \text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}] \left(\frac{x}{x-\#1}\right)^{-m} \#1^2 + m^2 \text{Hypergeometric2F1}[-m, -m, 1 - m, -\frac{\#1}{x-\#1}] \left(\frac{x}{x-\#1}\right)^{-m} \#1^2 + m \left(\frac{x}{\#1}\right)^{-m} \#1^2 \right) \&] \right) \right)$$

Problem 409: Result is not expressed in closed-form.

$$\int \frac{1}{x(1+x^5+x^{10})} dx$$

Optimal (type 3, 39 leaves, 7 steps):

$$-\frac{\text{ArcTan}\left[\frac{1+2x^5}{\sqrt{3}}\right]}{5\sqrt{3}} + \text{Log}[x] - \frac{1}{10} \text{Log}[1+x^5+x^{10}]$$

Result (type 7, 197 leaves):

$$\frac{\text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{5\sqrt{3}} + \text{Log}[x] - \frac{1}{10} \text{Log}[1+x+x^2] - \frac{1}{5} \text{RootSum}\left[1 - \#1 + \#1^3 - \#1^4 + \#1^5 - \#1^7 + \#1^8 \&, \right. \\ \left. (-\text{Log}[x - \#1] \#1 + 2 \text{Log}[x - \#1] \#1^2 - \text{Log}[x - \#1] \#1^3 + 3 \text{Log}[x - \#1] \#1^4 - \text{Log}[x - \#1] \#1^5 - \right. \\ \left. 3 \text{Log}[x - \#1] \#1^6 + 4 \text{Log}[x - \#1] \#1^7) / (-1 + 3 \#1^2 - 4 \#1^3 + 5 \#1^4 - 7 \#1^6 + 8 \#1^7) \&] \right)$$

Problem 410: Result is not expressed in closed-form.

$$\int \frac{1}{x^6(1+x^5+x^{10})} dx$$

Optimal (type 3, 48 leaves, 8 steps):

$$-\frac{1}{5x^5} - \frac{\text{ArcTan}\left[\frac{1+2x^5}{\sqrt{3}}\right]}{5\sqrt{3}} - \text{Log}[x] + \frac{1}{10} \text{Log}[1+x^5+x^{10}]$$

Result (type 7, 208 leaves):

$$\frac{1}{30} \left(-\frac{6}{x^5} + 2\sqrt{3} \text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right] - 30 \text{Log}[x] + 3 \text{Log}[1+x+x^2] + 6 \text{RootSum}\left[1 - \#1 + \#1^3 - \#1^4 + \#1^5 - \#1^7 + \#1^8 \&, \right. \right. \\ \left. \left. (-\text{Log}[x - \#1] + \text{Log}[x - \#1] \#1 + \text{Log}[x - \#1] \#1^2 - 3 \text{Log}[x - \#1] \#1^3 + 2 \text{Log}[x - \#1] \#1^4 + \text{Log}[x - \#1] \#1^5 - 4 \text{Log}[x - \#1] \#1^6 + 4 \text{Log}[x - \#1] \#1^7) / \right. \right. \\ \left. \left. (-1 + 3 \#1^2 - 4 \#1^3 + 5 \#1^4 - 7 \#1^6 + 8 \#1^7) \& \right] \right)$$

Problem 411: Result is not expressed in closed-form.

$$\int \frac{1}{x + x^6 + x^{11}} dx$$

Optimal (type 3, 39 leaves, 8 steps):

$$-\frac{\text{ArcTan}\left[\frac{1+2x^5}{\sqrt{3}}\right]}{5\sqrt{3}} + \text{Log}[x] - \frac{1}{10} \text{Log}[1+x^5+x^{10}]$$

Result (type 7, 197 leaves):

$$\frac{\text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{5\sqrt{3}} + \text{Log}[x] - \frac{1}{10} \text{Log}[1+x+x^2] - \frac{1}{5} \text{RootSum}\left[1 - \#1 + \#1^3 - \#1^4 + \#1^5 - \#1^7 + \#1^8 \&, \right. \\ \left. (-\text{Log}[x - \#1] \#1 + 2 \text{Log}[x - \#1] \#1^2 - \text{Log}[x - \#1] \#1^3 + 3 \text{Log}[x - \#1] \#1^4 - \text{Log}[x - \#1] \#1^5 - 3 \text{Log}[x - \#1] \#1^6 + 4 \text{Log}[x - \#1] \#1^7) / (-1 + 3 \#1^2 - 4 \#1^3 + 5 \#1^4 - 7 \#1^6 + 8 \#1^7) \& \right]$$

Problem 457: Result is not expressed in closed-form.

$$\int \frac{1}{c + \frac{a}{x^6} + \frac{b}{x^3}} dx$$

Optimal (type 3, 631 leaves, 15 steps):

$$\frac{x}{c} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b-\sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{4/3} (b - \sqrt{b^2-4ac})^{2/3}} + \frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{(b+\sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{4/3} (b + \sqrt{b^2-4ac})^{2/3}} -$$

$$\frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b - \sqrt{b^2-4ac}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{4/3} (b - \sqrt{b^2-4ac})^{2/3}} -$$

$$\frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b + \sqrt{b^2-4ac}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{4/3} (b + \sqrt{b^2-4ac})^{2/3}} +$$

$$\left(\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b - \sqrt{b^2-4ac}\right)^{2/3} - 2^{1/3} c^{1/3} (b - \sqrt{b^2-4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) /$$

$$\left(6 \times 2^{1/3} c^{4/3} (b - \sqrt{b^2-4ac})^{2/3}\right) +$$

$$\left(\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{Log}\left[\left(b + \sqrt{b^2-4ac}\right)^{2/3} - 2^{1/3} c^{1/3} (b + \sqrt{b^2-4ac})^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) /$$

$$\left(6 \times 2^{1/3} c^{4/3} (b + \sqrt{b^2-4ac})^{2/3}\right)$$

Result (type 7, 70 leaves):

$$\frac{x}{c} - \frac{\text{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{a \text{Log}[x-\#1] + b \text{Log}[x-\#1] \#1^3}{b \#1^2 + 2c \#1^5} \&\right]}{3c}$$

Problem 458: Result is not expressed in closed-form.

$$\int \frac{1}{c + \frac{a}{x^8} + \frac{b}{x^4}} dx$$

Optimal (type 3, 376 leaves, 9 steps):

$$\frac{x}{c} + \frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4} c^{5/4} (-b - \sqrt{b^2-4ac})^{3/4}} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{ArcTan}\left[\frac{2^{1/4} c^{1/4} x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4} c^{5/4} (-b + \sqrt{b^2-4ac})^{3/4}} +$$

$$\frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b-\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4} c^{5/4} (-b - \sqrt{b^2-4ac})^{3/4}} + \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}}\right) \text{ArcTanh}\left[\frac{2^{1/4} c^{1/4} x}{(-b+\sqrt{b^2-4ac})^{1/4}}\right]}{2 \times 2^{1/4} c^{5/4} (-b + \sqrt{b^2-4ac})^{3/4}}$$

Result (type 7, 70 leaves):

$$\frac{x}{c} \frac{\text{RootSum}\left[a+b \sqrt[4]{1}+c \sqrt[8]{1}, \frac{a \text{Log}[x-\sqrt[4]{1}]+b \text{Log}[x-\sqrt[4]{1} \sqrt[4]{1}]}{b \sqrt[4]{1}^3+2 c \sqrt[4]{1}^7}\right]}{4 c}$$

Problem 500: Result is not expressed in closed-form.

$$\int \frac{x^{-1+\frac{n}{4}}}{b x^n+c x^{2 n}} dx$$

Optimal (type 3, 236 leaves, 12 steps):

$$-\frac{4 x^{-3 n / 4}}{3 b n}+\frac{\sqrt{2} c^{3 / 4} \text{ArcTan}\left[1-\frac{\sqrt{2} c^{1 / 4} x^{n / 4}}{b^{1 / 4}}\right]}{b^{7 / 4} n}-\frac{\sqrt{2} c^{3 / 4} \text{ArcTan}\left[1+\frac{\sqrt{2} c^{1 / 4} x^{n / 4}}{b^{1 / 4}}\right]}{b^{7 / 4} n}+\frac{c^{3 / 4} \text{Log}\left[\sqrt{b}-\sqrt{2} b^{1 / 4} c^{1 / 4} x^{n / 4}+\sqrt{c} x^{n / 2}\right]}{\sqrt{2} b^{7 / 4} n}-\frac{c^{3 / 4} \text{Log}\left[\sqrt{b}+\sqrt{2} b^{1 / 4} c^{1 / 4} x^{n / 4}+\sqrt{c} x^{n / 2}\right]}{\sqrt{2} b^{7 / 4} n}$$

Result (type 7, 60 leaves):

$$\frac{-16 b x^{-3 n / 4}+3 c \text{RootSum}\left[c+b \sqrt[4]{1}, \frac{n \text{Log}[x]+4 \text{Log}\left[x^{-n / 4}-\sqrt[4]{1}\right]}{\sqrt[4]{1}}\right]}{12 b^2 n}$$

Problem 501: Result is not expressed in closed-form.

$$\int \frac{x^{-1+\frac{n}{3}}}{b x^n+c x^{2 n}} dx$$

Optimal (type 3, 160 leaves, 9 steps):

$$-\frac{3 x^{-2 n / 3}}{2 b n}+\frac{\sqrt{3} c^{2 / 3} \text{ArcTan}\left[\frac{b^{1 / 3}-2 c^{1 / 3} x^{n / 3}}{\sqrt{3} b^{1 / 3}}\right]}{b^{5 / 3} n}-\frac{c^{2 / 3} \text{Log}\left[b^{1 / 3}+c^{1 / 3} x^{n / 3}\right]}{b^{5 / 3} n}+\frac{c^{2 / 3} \text{Log}\left[b^{2 / 3}-b^{1 / 3} c^{1 / 3} x^{n / 3}+c^{2 / 3} x^{2 n / 3}\right]}{2 b^{5 / 3} n}$$

Result (type 7, 60 leaves):

$$\frac{-9 b x^{-2 n / 3}+2 c \text{RootSum}\left[c+b \sqrt[3]{1}, \frac{n \text{Log}[x]+3 \text{Log}\left[x^{-n / 3}-\sqrt[3]{1}\right]}{\sqrt[3]{1}}\right]}{6 b^2 n}$$

Problem 504: Result is not expressed in closed-form.

$$\int \frac{x^{-1-\frac{n}{3}}}{b x^n+c x^{2 n}} dx$$

Optimal (type 3, 176 leaves, 11 steps):

$$-\frac{3 x^{-4 n/3}}{4 b n} + \frac{3 c x^{-n/3}}{b^2 n} + \frac{\sqrt{3} c^{4/3} \operatorname{ArcTan}\left[\frac{c^{1/3}-2 b^{1/3} x^{-n/3}}{\sqrt{3} c^{1/3}}\right]}{b^{7/3} n} - \frac{c^{4/3} \operatorname{Log}\left[c^{1/3}+b^{1/3} x^{-n/3}\right]}{b^{7/3} n} + \frac{c^{4/3} \operatorname{Log}\left[c^{2/3}+b^{2/3} x^{-2 n/3}-b^{1/3} c^{1/3} x^{-n/3}\right]}{2 b^{7/3} n}$$

Result (type 7, 70 leaves):

$$-\frac{1}{12 b^3 n} \left(9 b x^{-4 n/3} (b-4 c x^n) + 4 c^2 \operatorname{RootSum}\left[c+b \#1^3, \frac{n \operatorname{Log}[x]+3 \operatorname{Log}\left[x^{-n/3}-\#1\right]}{\#1^2}\right] \& \right)$$

Problem 505: Result is not expressed in closed-form.

$$\int \frac{x^{-1-\frac{n}{4}}}{b x^n+c x^{2 n}} dx$$

Optimal (type 3, 252 leaves, 14 steps):

$$-\frac{4 x^{-5 n/4}}{5 b n} + \frac{4 c x^{-n/4}}{b^2 n} + \frac{\sqrt{2} c^{5/4} \operatorname{ArcTan}\left[1-\frac{\sqrt{2} b^{1/4} x^{-n/4}}{c^{1/4}}\right]}{b^{9/4} n} - \frac{\sqrt{2} c^{5/4} \operatorname{ArcTan}\left[1+\frac{\sqrt{2} b^{1/4} x^{-n/4}}{c^{1/4}}\right]}{b^{9/4} n} + \frac{c^{5/4} \operatorname{Log}\left[\sqrt{c}+\sqrt{b} x^{-n/2}-\sqrt{2} b^{1/4} c^{1/4} x^{-n/4}\right]}{\sqrt{2} b^{9/4} n} - \frac{c^{5/4} \operatorname{Log}\left[\sqrt{c}+\sqrt{b} x^{-n/2}+\sqrt{2} b^{1/4} c^{1/4} x^{-n/4}\right]}{\sqrt{2} b^{9/4} n}$$

Result (type 7, 70 leaves):

$$-\frac{1}{20 b^3 n} \left(16 b x^{-5 n/4} (b-5 c x^n) + 5 c^2 \operatorname{RootSum}\left[c+b \#1^4, \frac{n \operatorname{Log}[x]+4 \operatorname{Log}\left[x^{-n/4}-\#1\right]}{\#1^3}\right] \& \right)$$

Problem 543: Result more than twice size of optimal antiderivative.

$$\int \left(a^2 + b^2 x^{-\frac{2}{1+2 p}} + 2 a b x^{-\frac{1}{1+2 p}} \right)^p dx$$

Optimal (type 3, 52 leaves, 2 steps):

$$\frac{x \left(a + b x^{\frac{1}{-1-2 p}} \right) \left(a^2 + 2 a b x^{\frac{1}{-1-2 p}} + b^2 x^{-\frac{2}{1+2 p}} \right)^p}{a}$$

Result (type 3, 121 leaves):

$$\frac{1}{a} x^{\frac{2 p}{1+2 p}} \left(x^{-\frac{2}{1+2 p}} \left(b + a x^{\frac{1}{1+2 p}} \right)^2 \right)^p \left(1 + \frac{a x^{\frac{1}{1+2 p}}}{b} \right)^{-2 p} \left(a x^{\frac{1}{1+2 p}} \left(1 + \frac{a x^{\frac{1}{1+2 p}}}{b} \right)^{2 p} + b \left(-1 + \left(1 + \frac{a x^{\frac{1}{1+2 p}}}{b} \right)^{2 p} \right) \right)$$

Problem 546: Result unnecessarily involves higher level functions.

$$\int \left(a^2 + 2 a b x^n + b^2 x^{2 n} \right)^{-\frac{1+2 n}{2 n}} dx$$

Optimal (type 3, 102 leaves, 3 steps):

$$\frac{x (a+b x^n) (a^2+2 a b x^n+b^2 x^{2 n})^{\frac{1}{2}} \left(-2-\frac{1}{n}\right)}{a(1+n)} + \frac{n x (a+b x^n)^2 (a^2+2 a b x^n+b^2 x^{2 n})^{\frac{1}{2}} \left(-2-\frac{1}{n}\right)}{a^2(1+n)}$$

Result (type 5, 59 leaves):

$$\frac{1}{a^2} x \left((a+b x^n)^2 \right)^{-\frac{1}{2n}} \left(1 + \frac{b x^n}{a} \right)^{\frac{1}{n}} \text{Hypergeometric2F1} \left[2 + \frac{1}{n}, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{b x^n}{a} \right]$$

Problem 547: Result unnecessarily involves higher level functions.

$$\int (d x)^{-1-2 n(1+p)} (a^2+2 a b x^n+b^2 x^{2 n})^p d x$$

Optimal (type 3, 117 leaves, 3 steps):

$$-\frac{(d x)^{-2 n(1+p)} (a+b x^n) (a^2+2 a b x^n+b^2 x^{2 n})^p}{a d n(1+2 p)} + \frac{(d x)^{-2 n(1+p)} (a^2+2 a b x^n+b^2 x^{2 n})^{1+p}}{2 a^2 d n(1+p)(1+2 p)}$$

Result (type 5, 75 leaves):

$$-\frac{1}{2 n(1+p)} x (d x)^{-1-2 n(1+p)} \left((a+b x^n)^2 \right)^p \left(1 + \frac{b x^n}{a} \right)^{-2 p} \text{Hypergeometric2F1} \left[-2 p, -2(1+p), 1-2(1+p), -\frac{b x^n}{a} \right]$$

Problem 556: Result is not expressed in closed-form.

$$\int \frac{x^{-1+\frac{n}{4}}}{a+b x^n+c x^{2 n}} d x$$

Optimal (type 3, 353 leaves, 8 steps):

$$\frac{2 \times 2^{3/4} c^{3/4} \text{ArcTan} \left[\frac{2^{1/4} c^{1/4} x^{n/4}}{(-b-\sqrt{b^2-4 a c})^{1/4}} \right]}{\sqrt{b^2-4 a c} (-b-\sqrt{b^2-4 a c})^{3/4} n} - \frac{2 \times 2^{3/4} c^{3/4} \text{ArcTan} \left[\frac{2^{1/4} c^{1/4} x^{n/4}}{(-b+\sqrt{b^2-4 a c})^{1/4}} \right]}{\sqrt{b^2-4 a c} (-b+\sqrt{b^2-4 a c})^{3/4} n} +$$

$$\frac{2 \times 2^{3/4} c^{3/4} \text{ArcTanh} \left[\frac{2^{1/4} c^{1/4} x^{n/4}}{(-b-\sqrt{b^2-4 a c})^{1/4}} \right]}{\sqrt{b^2-4 a c} (-b-\sqrt{b^2-4 a c})^{3/4} n} - \frac{2 \times 2^{3/4} c^{3/4} \text{ArcTanh} \left[\frac{2^{1/4} c^{1/4} x^{n/4}}{(-b+\sqrt{b^2-4 a c})^{1/4}} \right]}{\sqrt{b^2-4 a c} (-b+\sqrt{b^2-4 a c})^{3/4} n}$$

Result (type 7, 62 leaves):

$$\frac{\text{RootSum} \left[a+b \#1^4+c \#1^8, \frac{-n \text{Log}[x]+4 \text{Log} \left[x^{n/4}-\#1 \right]}{b \#1^3+2 c \#1^7} \& \right]}{4 n}$$

Problem 557: Result is not expressed in closed-form.

$$\int \frac{x^{-1+\frac{n}{3}}}{a+b x^n+c x^{2 n}} dx$$

Optimal (type 3, 610 leaves, 14 steps):

$$\begin{aligned} & -\frac{2^{2/3} \sqrt{3} c^{2/3} \operatorname{ArcTan}\left[\frac{1-\frac{2 \cdot 2^{1/3} c^{1/3} x^{n/3}}{\left(b-\sqrt{b^2-4 a c}\right)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{b^2-4 a c}\left(b-\sqrt{b^2-4 a c}\right)^{2/3} n} + \frac{2^{2/3} \sqrt{3} c^{2/3} \operatorname{ArcTan}\left[\frac{1-\frac{2 \cdot 2^{1/3} c^{1/3} x^{n/3}}{\left(b+\sqrt{b^2-4 a c}\right)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{b^2-4 a c}\left(b+\sqrt{b^2-4 a c}\right)^{2/3} n} + \\ & \frac{2^{2/3} c^{2/3} \operatorname{Log}\left[\left(b-\sqrt{b^2-4 a c}\right)^{1/3}+2^{1/3} c^{1/3} x^{n/3}\right]}{\sqrt{b^2-4 a c}\left(b-\sqrt{b^2-4 a c}\right)^{2/3} n} - \\ & \frac{2^{2/3} c^{2/3} \operatorname{Log}\left[\left(b+\sqrt{b^2-4 a c}\right)^{1/3}+2^{1/3} c^{1/3} x^{n/3}\right]}{\sqrt{b^2-4 a c}\left(b+\sqrt{b^2-4 a c}\right)^{2/3} n} - \\ & \left(\frac{c^{2/3} \operatorname{Log}\left[\left(b-\sqrt{b^2-4 a c}\right)^{2/3}-2^{1/3} c^{1/3}\left(b-\sqrt{b^2-4 a c}\right)^{1/3} x^{n/3}+2^{2/3} c^{2/3} x^{2 n/3}\right]}{2^{1/3} \sqrt{b^2-4 a c}\left(b-\sqrt{b^2-4 a c}\right)^{2/3} n} + \right. \\ & \left. \frac{c^{2/3} \operatorname{Log}\left[\left(b+\sqrt{b^2-4 a c}\right)^{2/3}-2^{1/3} c^{1/3}\left(b+\sqrt{b^2-4 a c}\right)^{1/3} x^{n/3}+2^{2/3} c^{2/3} x^{2 n/3}\right]}{2^{1/3} \sqrt{b^2-4 a c}\left(b+\sqrt{b^2-4 a c}\right)^{2/3} n}\right) / \end{aligned}$$

Result (type 7, 62 leaves):

$$\frac{\operatorname{RootSum}\left[a+b \#1^3+c \#1^6,\frac{-n \operatorname{Log}[x]+3 \operatorname{Log}\left[x^{n/3}-\#1\right]}{b \#1^2+2 c \#1^5}\right] \&}{3 n}$$

Problem 558: Result is not expressed in closed-form.

$$\int \frac{x^{-1+\frac{n}{2}}}{a+b x^n+c x^{2 n}} dx$$

Optimal (type 3, 169 leaves, 4 steps):

$$\frac{2 \sqrt{2} \sqrt{c} \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{c} x^{n/2}}{\sqrt{b-\sqrt{b^2-4 a c}}}\right]}{\sqrt{b^2-4 a c} \sqrt{b-\sqrt{b^2-4 a c}} n} - \frac{2 \sqrt{2} \sqrt{c} \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{c} x^{n/2}}{\sqrt{b+\sqrt{b^2-4 a c}}}\right]}{\sqrt{b^2-4 a c} \sqrt{b+\sqrt{b^2-4 a c}} n}$$

Result (type 7, 60 leaves):

$$\frac{\text{RootSum}\left[a+b \sqrt{1^2}+c \sqrt{1^4} \&, \frac{-n \text{Log}[x]+2 \text{Log}\left[x^{n/2}-\sqrt{1}\right]}{b \sqrt{1+2 c \sqrt{1^3}}}\right] \&]}{2 n}$$

Problem 559: Result is not expressed in closed-form.

$$\int \frac{x^{-1-\frac{n}{2}}}{a+b x^n+c x^{2 n}} dx$$

Optimal (type 3, 205 leaves, 6 steps):

$$-\frac{2 x^{-n/2}}{a n} + \frac{\sqrt{2} \left(b - \frac{b^2-2 a c}{\sqrt{b^2-4 a c}}\right) \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{a} x^{-n/2}}{\sqrt{b-\sqrt{b^2-4 a c}}}\right]}{a^{3/2} \sqrt{b-\sqrt{b^2-4 a c}} n} + \frac{\sqrt{2} \left(b + \frac{b^2-2 a c}{\sqrt{b^2-4 a c}}\right) \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{a} x^{-n/2}}{\sqrt{b+\sqrt{b^2-4 a c}}}\right]}{a^{3/2} \sqrt{b+\sqrt{b^2-4 a c}} n}$$

Result (type 7, 105 leaves):

$$-\frac{1}{2 a n} \left(4 x^{-n/2} - \text{RootSum}\left[c+b \sqrt{1^2}+a \sqrt{1^4} \&, \frac{1}{b \sqrt{1+2 a \sqrt{1^3}}}\left(c n \text{Log}[x]+2 c \text{Log}\left[x^{-n/2}-\sqrt{1}\right]+b n \text{Log}[x] \sqrt{1^2}+2 b \text{Log}\left[x^{-n/2}-\sqrt{1}\right] \sqrt{1^2}\right) \&\right]\right)$$

Problem 560: Result is not expressed in closed-form.

$$\int \frac{x^{-1-\frac{n}{3}}}{a+b x^n+c x^{2 n}} dx$$

Optimal (type 3, 699 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{3x^{-n/3}}{an} - \frac{\sqrt{3} \left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{ArcTan} \left[\frac{1 - \frac{2^{2/3} a^{1/3} x^{-n/3}}{(b-\sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}} \right]}{2^{1/3} a^{4/3} (b - \sqrt{b^2-4ac})^{2/3} n} - \frac{\sqrt{3} \left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{ArcTan} \left[\frac{1 - \frac{2^{2/3} a^{1/3} x^{-n/3}}{(b+\sqrt{b^2-4ac})^{1/3}}}{\sqrt{3}} \right]}{2^{1/3} a^{4/3} (b + \sqrt{b^2-4ac})^{2/3} n} + \\
 & \frac{\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{Log} \left[\left(b - \sqrt{b^2-4ac} \right)^{1/3} + 2^{1/3} a^{1/3} x^{-n/3} \right]}{2^{1/3} a^{4/3} (b - \sqrt{b^2-4ac})^{2/3} n} + \\
 & \frac{\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{Log} \left[\left(b + \sqrt{b^2-4ac} \right)^{1/3} + 2^{1/3} a^{1/3} x^{-n/3} \right]}{2^{1/3} a^{4/3} (b + \sqrt{b^2-4ac})^{2/3} n} - \\
 & \frac{\left(\left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{Log} \left[\left(b - \sqrt{b^2-4ac} \right)^{2/3} + 2^{2/3} a^{2/3} x^{-2n/3} - 2^{1/3} a^{1/3} \left(b - \sqrt{b^2-4ac} \right)^{1/3} x^{-n/3} \right] \right)}{\left(2 \times 2^{1/3} a^{4/3} (b - \sqrt{b^2-4ac})^{2/3} n \right)} - \\
 & \frac{\left(\left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{Log} \left[\left(b + \sqrt{b^2-4ac} \right)^{2/3} + 2^{2/3} a^{2/3} x^{-2n/3} - 2^{1/3} a^{1/3} \left(b + \sqrt{b^2-4ac} \right)^{1/3} x^{-n/3} \right] \right)}{\left(2 \times 2^{1/3} a^{4/3} (b + \sqrt{b^2-4ac})^{2/3} n \right)}
 \end{aligned}$$

Result (type 7, 107 leaves):

$$\begin{aligned}
 & - \frac{1}{3an} \left(9x^{-n/3} - \text{RootSum} \left[c + b \#1^3 + a \#1^6 \&, \right. \right. \\
 & \left. \left. \frac{1}{b \#1^2 + 2a \#1^5} \left(c n \text{Log}[x] + 3c \text{Log}[x^{-n/3} - \#1] + b n \text{Log}[x] \#1^3 + 3b \text{Log}[x^{-n/3} - \#1] \#1^3 \right) \& \right] \right)
 \end{aligned}$$

Problem 561: Result is not expressed in closed-form.

$$\int \frac{x^{-1-\frac{n}{4}}}{a+bx^n+cx^{2n}} dx$$

Optimal (type 3, 414 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{4x^{-n/4}}{an} - \frac{2^{3/4} \left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{ArcTan} \left[\frac{-2^{1/4} a^{1/4} x^{-n/4}}{(-b-\sqrt{b^2-4ac})^{1/4}} \right]}{a^{5/4} (-b - \sqrt{b^2-4ac})^{3/4} n} - \frac{2^{3/4} \left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{ArcTan} \left[\frac{-2^{1/4} a^{1/4} x^{-n/4}}{(-b+\sqrt{b^2-4ac})^{1/4}} \right]}{a^{5/4} (-b + \sqrt{b^2-4ac})^{3/4} n} - \\
 & \frac{2^{3/4} \left(b + \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{ArcTanh} \left[\frac{-2^{1/4} a^{1/4} x^{-n/4}}{(-b-\sqrt{b^2-4ac})^{1/4}} \right]}{a^{5/4} (-b - \sqrt{b^2-4ac})^{3/4} n} - \frac{2^{3/4} \left(b - \frac{b^2-2ac}{\sqrt{b^2-4ac}} \right) \text{ArcTanh} \left[\frac{-2^{1/4} a^{1/4} x^{-n/4}}{(-b+\sqrt{b^2-4ac})^{1/4}} \right]}{a^{5/4} (-b + \sqrt{b^2-4ac})^{3/4} n}
 \end{aligned}$$

Result (type 7, 105 leaves):

$$\frac{1}{4 a n} \left(-16 x^{-n/4} + \text{RootSum} \left[c + b \#1^4 + a \#1^8 \&, \right. \right. \\ \left. \left. \frac{1}{b \#1^3 + 2 a \#1^7} \left(c n \text{Log}[x] + 4 c \text{Log} \left[x^{-n/4} - \#1 \right] + b n \text{Log}[x] \#1^4 + 4 b \text{Log} \left[x^{-n/4} - \#1 \right] \#1^4 \right) \& \right] \right)$$

Problem 564: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{a + b x^n + c x^{2n}} dx$$

Optimal (type 5, 124 leaves, 3 steps):

$$\frac{2 c x \text{Hypergeometric2F1} \left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right]}{b^2 - 4 a c - b \sqrt{b^2 - 4 a c}} - \frac{2 c x \text{Hypergeometric2F1} \left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right]}{b^2 - 4 a c + b \sqrt{b^2 - 4 a c}}$$

Result (type 5, 261 leaves):

$$-2 c x \left(\left(1 - \left(\frac{x^n}{-\frac{b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1 + n}{n}, \frac{b - \sqrt{b^2 - 4 a c}}{b - \sqrt{b^2 - 4 a c} + 2 c x^n} \right] \right) / \right. \\ \left. \left(b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) + \left(1 - 2^{-1/n} \left(\frac{c x^n}{b + \sqrt{b^2 - 4 a c} + 2 c x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1 + n}{n}, \frac{b + \sqrt{b^2 - 4 a c}}{b + \sqrt{b^2 - 4 a c} + 2 c x^n} \right] \right) / \left(\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right) \right) \right)$$

Problem 568: Result more than twice size of optimal antiderivative.

$$\int x^3 \sqrt{a + b x^n + c x^{2n}} dx$$

Optimal (type 6, 148 leaves, 2 steps):

$$\left(x^4 \sqrt{a + b x^n + c x^{2n}} \text{AppellF1} \left[\frac{4}{n}, -\frac{1}{2}, -\frac{1}{2}, \frac{4 + n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(4 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right)$$

Result (type 6, 820 leaves):

$$\begin{aligned}
 & \frac{1}{(a+x^n(b+cx^n))^{3/2}} \\
 & x^4 \left(\frac{(a+x^n(b+cx^n))^2}{4+n} + \left(4a^2bn(2+n)x^n(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \right. \\
 & \quad \left((-b+\sqrt{b^2-4ac})(b+\sqrt{b^2-4ac})(4+n)^2 \left((b+\sqrt{b^2-4ac})nx^n \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[2+\frac{4}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - (-b+\sqrt{b^2-4ac}) \right) \right. \\
 & \quad \left. nx^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \quad \left. \left. 8a(2+n) \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) + \\
 & \quad \left(a^2n(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \text{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. \frac{4+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \quad \left(4c \left(4a(4+n) \text{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \right. \\
 & \quad \left. \left. nx^n \left((b+\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{4}{n}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] + (b-\sqrt{b^2-4ac}) \right) \right. \right. \\
 & \quad \left. \left. \left. \left. \text{AppellF1}\left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 569: Result more than twice size of optimal antiderivative.

$$\int x^2 \sqrt{a+bx^n+cx^{2n}} dx$$

Optimal (type 6, 148 leaves, 2 steps):

$$\begin{aligned}
 & \left(x^3 \sqrt{a+bx^n+cx^{2n}} \text{AppellF1}\left[\frac{3}{n}, -\frac{1}{2}, -\frac{1}{2}, \frac{3+n}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \left(3 \sqrt{1+\frac{2cx^n}{b-\sqrt{b^2-4ac}}} \sqrt{1+\frac{2cx^n}{b+\sqrt{b^2-4ac}}} \right)
 \end{aligned}$$

Result (type 6, 825 leaves):

$$\frac{1}{3 (a + x^n (b + c x^n))^{3/2}}$$

$$x^3 \left(\frac{3 (a + x^n (b + c x^n))^2}{3 + n} + \left(6 a^2 b n (3 + 2 n) x^n (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \right. \right.$$

$$\left. \left. \text{AppellF1} \left[\frac{3 + n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \right.$$

$$\left((-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c}) (3 + n)^2 \left((b + \sqrt{b^2 - 4 a c}) n x^n \right. \right.$$

$$\left. \left. \text{AppellF1} \left[2 + \frac{3}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - (-b + \sqrt{b^2 - 4 a c}) \right.$$

$$\left. n x^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right.$$

$$\left. \left. 4 a (3 + 2 n) \text{AppellF1} \left[\frac{3 + n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) +$$

$$\left(a^2 n (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{3 + n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) /$$

$$\left(c \left(4 a (3 + n) \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3 + n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right.$$

$$\left. n x^n \left((b + \sqrt{b^2 - 4 a c}) \text{AppellF1} \left[\frac{3 + n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{3}{n}, \right. \right. \right.$$

$$\left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + (b - \sqrt{b^2 - 4 a c}) \right.$$

$$\left. \left. \left. \left. \text{AppellF1} \left[\frac{3 + n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) \right)$$

Problem 570: Result more than twice size of optimal antiderivative.

$$\int x \sqrt{a + b x^n + c x^{2 n}} dx$$

Optimal (type 6, 148 leaves, 2 steps):

$$\left(x^2 \sqrt{a + b x^n + c x^{2 n}} \text{AppellF1} \left[\frac{2}{n}, -\frac{1}{2}, -\frac{1}{2}, \frac{2 + n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) /$$

$$\left(2 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right)$$

Result (type 6, 816 leaves):

$$\begin{aligned}
 & \frac{1}{(a+x^n(b+cx^n))^{3/2}} \\
 & x^2 \left(\frac{(a+x^n(b+cx^n))^2}{2+n} + \left(4a^2bn(1+n)x^n(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \right. \\
 & \quad \left((-b+\sqrt{b^2-4ac})(b+\sqrt{b^2-4ac})(2+n)^2 \left((b+\sqrt{b^2-4ac})nx^n \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[2+\frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - (-b+\sqrt{b^2-4ac}) \right. \right. \\
 & \quad \left. \left. nx^n \text{AppellF1}\left[2+\frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \right. \\
 & \quad \left. \left. 8a(1+n) \text{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) + \\
 & \quad \left(a^2n(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \text{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. \frac{2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \quad \left(8ac(2+n) \text{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - 2cn \right. \\
 & \quad \left. x^n \left((b+\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] + \right. \right. \\
 & \quad \left. \left. (b-\sqrt{b^2-4ac}) \text{AppellF1}\left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) \right)
 \end{aligned}$$

Problem 571: Result more than twice size of optimal antiderivative.

$$\int \sqrt{a+bx^n+cx^{2n}} dx$$

Optimal (type 6, 139 leaves, 2 steps):

$$\begin{aligned}
 & \left(x \sqrt{a+bx^n+cx^{2n}} \text{AppellF1}\left[\frac{1}{n}, -\frac{1}{2}, -\frac{1}{2}, 1+\frac{1}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \left(\sqrt{1+\frac{2cx^n}{b-\sqrt{b^2-4ac}}} \sqrt{1+\frac{2cx^n}{b+\sqrt{b^2-4ac}}} \right)
 \end{aligned}$$

Result (type 6, 786 leaves):

$$\frac{1}{(a+x^n(b+cx^n))^{3/2}}$$

$$x \left(\frac{(a+x^n(b+cx^n))^2}{1+n} + \left(2a^2bn(1+2n)x^n(b-\sqrt{b^2-4ac}+2cx^n) \left(b+\sqrt{b^2-4ac}+2cx^n \right) \right. \right.$$

$$\left. \left. \text{AppellF1} \left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \right.$$

$$\left(\left(-b+\sqrt{b^2-4ac} \right) \left(b+\sqrt{b^2-4ac} \right) (1+n)^2 \left(-4(a+2an) \text{AppellF1} \left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \right. \right. \right.$$

$$\left. \left. 2+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + nx^n \left(\left(b+\sqrt{b^2-4ac} \right) \text{AppellF1} \left[\right. \right.$$

$$\left. \left. 2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(b-\sqrt{b^2-4ac} \right) \right.$$

$$\left. \left. \text{AppellF1} \left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) +$$

$$\left(a^2n(b-\sqrt{b^2-4ac}+2cx^n) \left(b+\sqrt{b^2-4ac}+2cx^n \right) \text{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. 1+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) /$$

$$\left(c \left(-\left(b+\sqrt{b^2-4ac} \right) nx^n \text{AppellF1} \left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \right. \right. \right.$$

$$\left. \left. \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(-b+\sqrt{b^2-4ac} \right) nx^n \right.$$

$$\left. \left. \text{AppellF1} \left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right.$$

$$\left. \left. 4a(1+n) \text{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right)$$

Problem 573: Result more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+bx^n+cx^{2n}}}{x^2} dx$$

Optimal (type 6, 149 leaves, 2 steps):

$$-\left(\left(\sqrt{a+bx^n+cx^{2n}} \text{AppellF1} \left[-\frac{1}{n}, -\frac{1}{2}, -\frac{1}{2}, -\frac{1-n}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}} \right] \right) / \right.$$

$$\left. \left(x \sqrt{1+\frac{2cx^n}{b-\sqrt{b^2-4ac}}} \sqrt{1+\frac{2cx^n}{b+\sqrt{b^2-4ac}}} \right) \right)$$

Result (type 6, 821 leaves):

$$\begin{aligned}
 & \frac{1}{x (a + x^n (b + c x^n))^{3/2}} \\
 & \left(\frac{(a + x^n (b + c x^n))^2}{-1 + n} + \left(2 a^2 b n (-1 + 2 n) x^n (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{-1 + n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \right. \\
 & \quad \left((-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c}) (-1 + n)^2 \left((b + \sqrt{b^2 - 4 a c}) n x^n \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[2 - \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - (-b + \sqrt{b^2 - 4 a c}) \right) \right. \\
 & \quad \left. n x^n \text{AppellF1} \left[2 - \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left. 4 a (1 - 2 n) \text{AppellF1} \left[\frac{-1 + n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
 & \quad \left(a^2 n (-b + \sqrt{b^2 - 4 a c} - 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \right. \\
 & \quad \left. \left. \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1 + n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \right. \\
 & \quad \left(c \left(4 a (-1 + n) \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1 + n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left((b + \sqrt{b^2 - 4 a c}) \text{AppellF1} \left[\frac{-1 + n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + (b - \sqrt{b^2 - 4 a c}) \right) \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \text{AppellF1} \left[\frac{-1 + n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 574: Result more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a + b x^n + c x^{2n}}}{x^3} dx$$

Optimal (type 6, 151 leaves, 2 steps):

$$\begin{aligned}
 & - \left(\left(\sqrt{a + b x^n + c x^{2n}} \text{AppellF1} \left[-\frac{2}{n}, -\frac{1}{2}, -\frac{1}{2}, -\frac{2-n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \right. \\
 & \quad \left. \left(2 x^2 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right) \right)
 \end{aligned}$$

Result (type 6, 816 leaves):

$$\frac{1}{x^2 (a+x^n (b+c x^n))^{3/2}} \left(\frac{(a+x^n (b+c x^n))^2}{-2+n} + \left(4 a^2 b (-1+n) n x^n (b-\sqrt{b^2-4 a c}+2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right. \right. \\ \left. \left. \text{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) / \right. \\ \left. \left((-b+\sqrt{b^2-4 a c}) (b+\sqrt{b^2-4 a c}) (-2+n)^2 \left((b+\sqrt{b^2-4 a c}) n x^n \right. \right. \right. \\ \left. \left. \text{AppellF1} \left[2-\frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - (-b+\sqrt{b^2-4 a c}) \right. \right. \\ \left. \left. n x^n \text{AppellF1} \left[2-\frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - \right. \right. \\ \left. \left. 8 a (-1+n) \text{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) + \\ \left(a^2 n (-b+\sqrt{b^2-4 a c}-2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right. \\ \left. \text{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) / \\ \left(8 a c (-2+n) \text{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - 2 c n \right. \\ \left. x^n \left((b+\sqrt{b^2-4 a c}) \text{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] + \right. \right. \\ \left. \left. (b-\sqrt{b^2-4 a c}) \text{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) \right)$$

Problem 575: Result more than twice size of optimal antiderivative.

$$\int x^3 (a+b x^n+c x^{2 n})^{3/2} dx$$

Optimal (type 6, 149 leaves, 2 steps):

$$\left(a x^4 \sqrt{a+b x^n+c x^{2 n}} \text{AppellF1} \left[\frac{4}{n}, -\frac{3}{2}, -\frac{3}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}} \right] \right) / \\ \left(4 \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}} \right)$$

Result (type 6, 3165 leaves):

$$\sqrt{a+b x^n+c x^{2 n}} \left(\frac{(64 a c+96 a c n+3 b^2 n^2+32 a c n^2) x^4}{8 c(2+n)(4+n)(4+3 n)} + \frac{b(8+7 n) x^{4+n}}{4(2+n)(4+3 n)} + \frac{c x^{4+2 n}}{4+3 n} \right) - \\ \left(48 a^3 b n^2 x^{4+n} (b-\sqrt{b^2-4 a c}+2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] / \\
 & \left((b-\sqrt{b^2-4ac}) (b+\sqrt{b^2-4ac}) (4+n)^2 (4+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left((b+\sqrt{b^2-4ac}) n x^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \left. (-b+\sqrt{b^2-4ac}) n x^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \left. \left. 8a(2+n) \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) + \\
 & \left(12a^2 b^3 n^2 x^{4+n} (b-\sqrt{b^2-4ac} + 2cx^n) (b+\sqrt{b^2-4ac} + 2cx^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \left(c (b-\sqrt{b^2-4ac}) (b+\sqrt{b^2-4ac}) (4+n)^2 (4+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left((b+\sqrt{b^2-4ac}) n x^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \left. (-b+\sqrt{b^2-4ac}) n x^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \left. \left. 8a(2+n) \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) - \\
 & \left(18a^3 b n^3 x^{4+n} (b-\sqrt{b^2-4ac} + 2cx^n) (b+\sqrt{b^2-4ac} + 2cx^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \left((b-\sqrt{b^2-4ac}) (b+\sqrt{b^2-4ac}) (4+n)^2 (4+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left((b+\sqrt{b^2-4ac}) n x^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \left. (-b+\sqrt{b^2-4ac}) n x^n \text{AppellF1}\left[2+\frac{4}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\
 & \left. \left. 8a(2+n) \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) \right) + \\
 & \left(3a^2 b^3 n^3 x^{4+n} (b-\sqrt{b^2-4ac} + 2cx^n) (b+\sqrt{b^2-4ac} + 2cx^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \right) / \\
 & \left(2c (b-\sqrt{b^2-4ac}) (b+\sqrt{b^2-4ac}) (4+n)^2 (4+3n) (a+x^n (b+cx^n))^{3/2} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left((b + \sqrt{b^2 - 4ac}) n x^n \operatorname{AppellF1} \left[2 + \frac{4}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 + \frac{4}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left. 8a(2+n) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\
 & \left(6a^4 n^2 x^4 \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n) (4+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left(-4a(4+n) \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) + \\
 & \left(3a^3 b^2 n^2 x^4 \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(2c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n) (4+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left(-4a(4+n) \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) - \\
 & \left(3a^4 n^3 x^4 \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n) (4+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left(-4a(4+n) \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) -
 \end{aligned}$$

$$\left(\left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right)$$

Problem 576: Result more than twice size of optimal antiderivative.

$$\int x^2 (a + bx^n + cx^{2n})^{3/2} dx$$

Optimal (type 6, 149 leaves, 2 steps):

$$\left(ax^3 \sqrt{a + bx^n + cx^{2n}} \text{AppellF1} \left[\frac{3}{n}, -\frac{3}{2}, -\frac{3}{2}, \frac{3+n}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) /$$

$$\left(3 \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \right)$$

Result (type 6, 3165 leaves):

$$\sqrt{a + bx^n + cx^{2n}} \left(\frac{(36ac + 72acn + 3b^2n^2 + 32acn^2)x^3}{12c(1+n)(3+n)(3+2n)} + \frac{b(6+7n)x^{3+n}}{6(1+n)(3+2n)} + \frac{cx^{3+2n}}{3(1+n)} \right) -$$

$$\left(12a^3b^2n^2x^{3+n} (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right.$$

$$\left. \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) /$$

$$\left((b - \sqrt{b^2 - 4ac}) (b + \sqrt{b^2 - 4ac}) (1+n)(3+n)^2 (a + x^n(b + cx^n))^{3/2} \right.$$

$$\left((b + \sqrt{b^2 - 4ac}) nx^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right.$$

$$\left. (-b + \sqrt{b^2 - 4ac}) nx^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right.$$

$$\left. 4a(3+2n) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) +$$

$$\left(3a^2b^3n^2x^{3+n} (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right.$$

$$\left. \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) /$$

$$\left(c (b - \sqrt{b^2 - 4ac}) (b + \sqrt{b^2 - 4ac}) (1+n)(3+n)^2 (a + x^n(b + cx^n))^{3/2} \right.$$

$$\left((b + \sqrt{b^2 - 4ac}) nx^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right.$$

$$\left. (-b + \sqrt{b^2 - 4ac}) nx^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right.$$

$$\left. 4a(3+2n) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) -$$

$$\begin{aligned}
 & \left(6 a^3 b n^3 x^{3+n} \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+n) (3+n)^2 \left(a + x^n (b + c x^n) \right)^{3/2} \right. \\
 & \quad \left(\left(b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left(-b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (3+2 n) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
 & \left(a^2 b^3 n^3 x^{3+n} \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(2 c \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+n) (3+n)^2 \left(a + x^n (b + c x^n) \right)^{3/2} \right. \\
 & \quad \left(\left(b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left(-b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[2 + \frac{3}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (3+2 n) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\
 & \left(4 a^4 n^2 x^3 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+n) (3+2 n) \left(a + x^n (b + c x^n) \right)^{3/2} \right. \\
 & \quad \left(-4 a (3+n) \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{3+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) + \\
 & \left(a^3 b^2 n^2 x^3 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+n) (3+2n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left(-4a(3+n) \operatorname{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{3}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{3+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{3}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) - \\
 & \left(8a^4 n^3 x^3 \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(3 \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+n) (3+2n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left(-4a(3+n) \operatorname{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{3}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{3+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{3}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 577: Result more than twice size of optimal antiderivative.

$$\int x (a + bx^n + cx^{2n})^{3/2} dx$$

Optimal (type 6, 149 leaves, 2 steps):

$$\begin{aligned}
 & \left(ax^2 \sqrt{a + bx^n + cx^{2n}} \operatorname{AppellF1} \left[\frac{2}{n}, -\frac{3}{2}, -\frac{3}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(2 \sqrt{1 + \frac{2cx^n}{b-\sqrt{b^2-4ac}}} \sqrt{1 + \frac{2cx^n}{b+\sqrt{b^2-4ac}}} \right)
 \end{aligned}$$

Result (type 6, 3165 leaves):

$$\begin{aligned}
 & \sqrt{a + bx^n + cx^{2n}} \left(\frac{(16ac + 48acn + 3b^2n^2 + 32acn^2) x^2}{8c(1+n)(2+n)(2+3n)} + \frac{b(4+7n)x^{2+n}}{4(1+n)(2+3n)} + \frac{cx^{2+2n}}{2+3n} \right) - \\
 & \left(24a^3 b n^2 x^{2+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n)^2 (2+3n) (a+x^n (b+cx^n))^{3/2} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(\left((b + \sqrt{b^2 - 4ac}) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
& \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
& \left. \left. 8a(1+n) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
& \left(6a^2 b^3 n^2 x^{2+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
& \left(c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n)^2 (2+3n) \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
& \left((b + \sqrt{b^2 - 4ac}) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
& \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
& \left. \left. 8a(1+n) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\
& \left(18a^3 b n^3 x^{2+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
& \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n)^2 (2+3n) \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
& \left((b + \sqrt{b^2 - 4ac}) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
& \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
& \left. \left. 8a(1+n) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
& \left(3a^2 b^3 n^3 x^{2+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
& \left(2c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (2+n)^2 (2+3n) \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
& \left((b + \sqrt{b^2 - 4ac}) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
& \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 + \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right.
\end{aligned}$$

$$\begin{aligned}
 & 8 a (1+n) \operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \Big) - \\
 & \left(6 a^4 n^2 x^2 \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)(2+3 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left(-4 a(2+n) \operatorname{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \Big) \Big) + \\
 & \left(3 a^3 b^2 n^2 x^2 \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left(2 c\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)(2+3 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left(-4 a(2+n) \operatorname{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \Big) \Big) - \\
 & \left(6 a^4 n^3 x^2 \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)(2+3 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left(-4 a(2+n) \operatorname{AppellF1}\left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \Big) \Big) \Big)
 \end{aligned}$$

Problem 578: Result more than twice size of optimal antiderivative.

$$\int (a+b x^n+c x^{2 n})^{3/2} dx$$

Optimal (type 6, 140 leaves, 2 steps):

$$\left(a x \sqrt{a+b x^n+c x^{2 n}} \operatorname{AppellF1}\left[\frac{1}{n},-\frac{3}{2},-\frac{3}{2},1+\frac{1}{n},-\frac{2 c x^n}{b-\sqrt{b^2-4 a c}},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right] \right) / \left(\sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}} \right)$$

Result (type 6, 3058 leaves):

$$\begin{aligned} & \sqrt{a+b x^n+c x^{2 n}} \left(\frac{(4 a c+24 a c n+3 b^2 n^2+32 a c n^2) x}{4 c(1+n)(1+2 n)(1+3 n)}+\frac{b(2+7 n) x^{1+n}}{2(1+2 n)(1+3 n)}+\frac{c x^{1+2 n}}{1+3 n} \right)- \\ & \left(12 a^3 b n^2 x^{1+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\ & \left(\left(b-\sqrt{b^2-4 a c} \right) \left(b+\sqrt{b^2-4 a c} \right) (1+n)^2(1+3 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2} \right. \\ & \left. \left(-4(a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) + \\ & \left(3 a^2 b^3 n^2 x^{1+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\ & \left(c \left(b-\sqrt{b^2-4 a c} \right) \left(b+\sqrt{b^2-4 a c} \right) (1+n)^2(1+3 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2} \right. \\ & \left. \left(-4(a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) - \\ & \left(18 a^3 b n^3 x^{1+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \end{aligned}$$

$$\begin{aligned}
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+n)^2 (1+3n) (a+x^n (b+c x^n))^{3/2} \right. \\
 & \quad \left(-4(a+2an) \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) + \\
 & \left(3a^2 b^3 n^3 x^{1+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(2c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+n)^2 (1+3n) (a+x^n (b+c x^n))^{3/2} \right. \\
 & \quad \left(-4(a+2an) \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) - \\
 & \left(12a^4 n^2 x \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+2n) (1+3n) (a+x^n (b+c x^n))^{3/2} \right. \\
 & \quad \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right. \\
 & \quad \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \\
 & \quad \left. 4a(1+n) \operatorname{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) + \\
 & \left(3a^3 b^2 n^2 x \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+2n) (1+3n) (a+x^n (b+c x^n))^{3/2} \right. \\
 & \quad \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned} & \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \\ & 4a(1+n) \operatorname{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \Big) - \\ & \left(24a^4 n^3 x \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \left. \operatorname{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+2n)(1+3n)(a+x^n(b+cx^n))^{3/2} \right. \\ & \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\ & \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\ & \left. \left. 4a(1+n) \operatorname{AppellF1} \left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \end{aligned}$$

Problem 580: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^n + c x^{2n})^{3/2}}{x^2} dx$$

Optimal (type 6, 150 leaves, 2 steps):

$$\begin{aligned} & - \left(\left(a \sqrt{a + b x^n + c x^{2n}} \operatorname{AppellF1} \left[-\frac{1}{n}, -\frac{3}{2}, -\frac{3}{2}, -\frac{1-n}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) / \right. \\ & \left. \left(x \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \right) \right) \end{aligned}$$

Result (type 6, 3181 leaves):

$$\begin{aligned} & \sqrt{a + b x^n + c x^{2n}} \left(\frac{4ac - 24acn + 3b^2n^2 + 32acn^2}{4c(-1+n)(-1+2n)(-1+3n)x} + \frac{b(-2+7n)x^{-1+n}}{2(-1+2n)(-1+3n)} + \frac{cx^{-1+2n}}{-1+3n} \right) + \\ & \left(12a^3 b n^2 x^{-1+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \left. \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (-1+n)^2 (-1+3n)(a+x^n(b+cx^n))^{3/2} \right. \\ & \left. \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \\
 & 4a(1-2n) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \Big) - \\
 & \left(3a^2 b^3 n^2 x^{-1+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (-1+n)^2 (-1+3n) (a+x^n(b+cx^n))^{3/2} \right. \\
 & \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 4a(1-2n) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Big) - \\
 & \left(18a^3 b n^3 x^{-1+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (-1+n)^2 (-1+3n) (a+x^n(b+cx^n))^{3/2} \right. \\
 & \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 4a(1-2n) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Big) + \\
 & \left(3a^2 b^3 n^3 x^{-1+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(2c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (-1+n)^2 (-1+3n) (a+x^n(b+cx^n))^{3/2} \right. \\
 & \left(\left(b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left(-b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \left. 4a(1-2n) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(12 a^4 n^2 \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-1+2 n) (-1+3 n) x \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(-4 a (-1+n) \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) \left. \right) - \\
 & \left(3 a^3 b^2 n^2 \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(c \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-1+2 n) (-1+3 n) x \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(-4 a (-1+n) \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) \left. \right) - \\
 & \left(24 a^4 n^3 \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-1+2 n) (-1+3 n) x \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(-4 a (-1+n) \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 581: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b x^n + c x^{2n})^{3/2}}{x^3} dx$$

Optimal (type 6, 152 leaves, 2 steps):

$$- \left(\left(a \sqrt{a + b x^n + c x^{2n}} \operatorname{AppellF1} \left[-\frac{2}{n}, -\frac{3}{2}, -\frac{3}{2}, -\frac{2-n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \right. \\ \left. \left(2 x^2 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right) \right)$$

Result (type 6, 3165 leaves):

$$\sqrt{a + b x^n + c x^{2n}} \left(\frac{16 a c - 48 a c n + 3 b^2 n^2 + 32 a c n^2}{8 c (-2+n) (-1+n) (-2+3 n) x^2} + \frac{b (-4+7 n) x^{-2+n}}{4 (-1+n) (-2+3 n)} + \frac{c x^{-2+2 n}}{-2+3 n} \right) + \\ \left(24 a^3 b n^2 x^{-2+n} \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\ \left. \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-2+n)^2 (-2+3 n) (a + x^n (b + c x^n))^{3/2} \right. \\ \left(\left(b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\ \left. \left(-b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\ \left. \left. 8 a (-1+n) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\ \left(6 a^2 b^3 n^2 x^{-2+n} \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\ \left. \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ \left(c \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-2+n)^2 (-2+3 n) (a + x^n (b + c x^n))^{3/2} \right. \\ \left(\left(b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\ \left. \left(-b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[2 - \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\ \left. \left. 8 a (-1+n) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\ \left(18 a^3 b n^3 x^{-2+n} \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \\
 & \left((b-\sqrt{b^2-4 a c}) (b+\sqrt{b^2-4 a c}) (-2+n)^2 (-2+3 n) (a+x^n (b+c x^n))^{3/2} \right. \\
 & \left((b+\sqrt{b^2-4 a c}) n x^n \text{AppellF1}\left[2-\frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \left. (-b+\sqrt{b^2-4 a c}) n x^n \text{AppellF1}\left[2-\frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \left. \left. 8 a (-1+n) \text{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) + \\
 & \left(3 a^2 b^3 n^3 x^{-2+n} (b-\sqrt{b^2-4 a c}+2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(2 c (b-\sqrt{b^2-4 a c}) (b+\sqrt{b^2-4 a c}) (-2+n)^2 (-2+3 n) (a+x^n (b+c x^n))^{3/2} \right. \\
 & \left((b+\sqrt{b^2-4 a c}) n x^n \text{AppellF1}\left[2-\frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \left. (-b+\sqrt{b^2-4 a c}) n x^n \text{AppellF1}\left[2-\frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \left. \left. 8 a (-1+n) \text{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) + \\
 & \left(6 a^4 n^2 (-b+\sqrt{b^2-4 a c}-2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right. \\
 & \left. \text{AppellF1}\left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left((b-\sqrt{b^2-4 a c}) (b+\sqrt{b^2-4 a c}) (-1+n) (-2+3 n) x^2 (a+x^n (b+c x^n))^{3/2} \right. \\
 & \left(-4 a (-2+n) \text{AppellF1}\left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & n x^n \left((b+\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \left. (b-\sqrt{b^2-4 a c}) \text{AppellF1}\left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) - \\
 & \left(3 a^3 b^2 n^2 (-b+\sqrt{b^2-4 a c}-2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right. \\
 & \left. \text{AppellF1}\left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 c \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-1+n) (-2+3 n) x^2 \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \left(-4 a (-2+n) \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) - \\
 & \left(6 a^4 n^3 \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (-1+n) (-2+3 n) x^2 \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \left(-4 a (-2+n) \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 582: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3}{\sqrt{a + b x^n + c x^{2n}}} dx$$

Optimal (type 6, 148 leaves, 2 steps):

$$\left(x^4 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(4 \sqrt{a + b x^n + c x^{2n}} \right)$$

Result (type 6, 415 leaves):

$$\begin{aligned}
 & - \left(\left(a^2 (4+n) x^4 \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left(-4a(4+n) \text{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2 + \frac{4}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 583: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2}{\sqrt{a + bx^n + cx^{2n}}} dx$$

Optimal (type 6, 148 leaves, 2 steps):

$$\left(x^3 \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \right. \\
 \left. \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(3 \sqrt{a + bx^n + cx^{2n}} \right)$$

Result (type 6, 417 leaves):

$$\begin{aligned}
 & - \left(\left(4 a^2 (3+n) x^3 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) / \\
 & \left(3 \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(-4 a (3+n) \text{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{3+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 584: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{\sqrt{a + b x^n + c x^{2n}}} dx$$

Optimal (type 6, 148 leaves, 2 steps):

$$\begin{aligned}
 & \left(x^2 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(2 \sqrt{a + b x^n + c x^{2n}} \right)
 \end{aligned}$$

Result (type 6, 415 leaves):

$$\begin{aligned}
 & - \left(\left(2 a^2 (2+n) x^2 \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(-4 a (2+n) \text{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 585: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{a+bx^n+cx^{2n}}} dx$$

Optimal (type 6, 139 leaves, 2 steps):

$$\frac{1}{\sqrt{a+bx^n+cx^{2n}}} x \sqrt{1 + \frac{2cx^n}{b-\sqrt{b^2-4ac}}} \sqrt{1 + \frac{2cx^n}{b+\sqrt{b^2-4ac}}} \\ \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right]$$

Result (type 6, 400 leaves):

$$-\left(\left(4a^2(1+n)x\left(b-\sqrt{b^2-4ac}+2cx^n\right)\left(b+\sqrt{b^2-4ac}+2cx^n\right)\right. \right. \\ \left. \left. \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right)\right) / \\ \left(\left(b-\sqrt{b^2-4ac}\right)\left(b+\sqrt{b^2-4ac}\right)\left(a+x^n\left(b+cx^n\right)\right)^{3/2}\right. \\ \left(\left(b+\sqrt{b^2-4ac}\right)nx^n \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\ \left.\left(-b+\sqrt{b^2-4ac}\right)nx^n \text{AppellF1}\left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \\ \left. \left. 4a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right)\right)$$

Problem 587: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^2 \sqrt{a+bx^n+cx^{2n}}} dx$$

Optimal (type 6, 149 leaves, 2 steps):

$$-\left(\left(\sqrt{1 + \frac{2cx^n}{b-\sqrt{b^2-4ac}}} \sqrt{1 + \frac{2cx^n}{b+\sqrt{b^2-4ac}}}\right. \right. \\ \left. \left. \text{AppellF1}\left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, -\frac{1-n}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right]\right)\right) / \left(x \sqrt{a+bx^n+cx^{2n}}\right)$$

Result (type 6, 415 leaves):

$$\begin{aligned}
 & - \left(\left(4 a^2 (-1+n) \left(-b + \sqrt{b^2 - 4 a c} - 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) / \\
 & \left(\left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) x \left(a + x^n \left(b + c x^n \right) \right)^{3/2} \right. \right. \\
 & \quad \left. \left(-4 a (-1+n) \text{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right. \\
 & \quad \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \left(b - \sqrt{b^2 - 4 a c} \right) \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \left. \text{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 588: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^3 \sqrt{a + b x^n + c x^{2n}}} dx$$

Optimal (type 6, 151 leaves, 2 steps):

$$\begin{aligned}
 & - \left(\left(\sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, -\frac{2-n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(2 x^2 \sqrt{a + b x^n + c x^{2n}} \right) \right)
 \end{aligned}$$

Result (type 6, 415 leaves):

$$\begin{aligned}
 & - \left(\left(2 a^2 (-2+n) \left(-b+\sqrt{b^2-4 a c}-2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) / \\
 & \left(\left(b-\sqrt{b^2-4 a c} \right) \left(b+\sqrt{b^2-4 a c} \right) x^2 \left(a+x^n \left(b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(-4 a (-2+n) \text{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] + \right. \\
 & \quad \left. n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \text{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2-\frac{2}{n}, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] + \left(b-\sqrt{b^2-4 a c} \right) \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2-\frac{2}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 589: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3}{(a+b x^n+c x^{2 n})^{3/2}} dx$$

Optimal (type 6, 151 leaves, 2 steps):

$$\left(x^4 \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}} \right. \\
 \left. \text{AppellF1} \left[\frac{4}{n}, \frac{3}{2}, \frac{3}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}} \right] \right) / \left(4 a \sqrt{a+b x^n+c x^{2 n}} \right)$$

Result (type 6, 1947 leaves):

$$\begin{aligned}
 & \frac{1}{a \left(-b^2+4 a c \right) \left(a+x^n \left(b+c x^n \right) \right)^{3/2}} x^4 \left(-\frac{2 \left(b^2-2 a c+b c x^n \right) \left(a+x^n \left(b+c x^n \right) \right)}{n} + \right. \\
 & \quad \left(64 a^2 b c \left(2+n \right) x^n \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) / \\
 & \left(\left(-b+\sqrt{b^2-4 a c} \right) \left(b+\sqrt{b^2-4 a c} \right) n \left(4+n \right) \left(\left(b+\sqrt{b^2-4 a c} \right) n x^n \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[2+\frac{4}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - \left(-b+\sqrt{b^2-4 a c} \right) \right) \right. \\
 & \quad \left. \left. n x^n \text{AppellF1} \left[2+\frac{4}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 8 a (2+n) \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \Bigg) + \\
 & \left(a^2 (4+n) \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(4 a (4+n) \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \left. n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. \left. \left(b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) - \\
 & \left(a b^2 (4+n) \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(4 c \left(4 a (4+n) \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \right. \\
 & \left. \left. n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{4}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \left(b-\sqrt{b^2-4 a c} \right) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) - \\
 & \left(4 a^2 (4+n) \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(n \left(4 a (4+n) \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \right. \\
 & \left. \left. n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{4}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \left(b-\sqrt{b^2-4 a c} \right) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) + \\
 & \left(2 a b^2 (4+n) \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) /
 \end{aligned}$$

$$\left(c n \left(4 a (4+n) \operatorname{AppellF1} \left[\frac{4}{n}, \frac{1}{2}, \frac{1}{2}, \frac{4+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - \right. \right. \\ \left. \left. n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] + \left(b-\sqrt{b^2-4 a c} \right) \right. \right. \right. \\ \left. \left. \left. \operatorname{AppellF1} \left[\frac{4+n}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{4}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) \right)$$

Problem 590: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2}{(a+b x^n+c x^{2 n})^{3/2}} dx$$

Optimal (type 6, 151 leaves, 2 steps):

$$\left(x^3 \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}} \operatorname{AppellF1} \left[\frac{3}{n}, \frac{3}{2}, \frac{3}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}} \right] \right) / \left(3 a \sqrt{a+b x^n+c x^{2 n}} \right)$$

Result (type 6, 2229 leaves):

$$\frac{2 x^3 (-b^2+2 a c-b c x^n)}{a (-b^2+4 a c) n \sqrt{a+b x^n+c x^{2 n}}} - \\ \left(24 a b c (3+2 n) x^{3+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \operatorname{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{3}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) / \\ \left((-b^2+4 a c) \left(b-\sqrt{b^2-4 a c} \right) \left(b+\sqrt{b^2-4 a c} \right) n (3+n) \left(a+x^n (b+c x^n) \right)^{3/2} \right. \\ \left(\left(b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1} \left[2+\frac{3}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{3}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - \right. \\ \left. \left(-b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1} \left[2+\frac{3}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{3}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] - \right. \\ \left. \left. 4 a (3+2 n) \operatorname{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{3}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) \right) + \\ \left(4 a b^2 (3+n) x^3 \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \operatorname{AppellF1} \left[\frac{3}{n}, \frac{1}{2}, \frac{1}{2}, \frac{3+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}} \right] \right) /$$

$$n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{3+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \left(b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{3+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{3}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right)$$

Problem 591: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{(a + b x^n + c x^{2n})^{3/2}} dx$$

Optimal (type 6, 151 leaves, 2 steps):

$$\left(x^2 \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \text{AppellF1} \left[\frac{2}{n}, \frac{3}{2}, \frac{3}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(2 a \sqrt{a + b x^n + c x^{2n}} \right)$$

Result (type 6, 1947 leaves):

$$\frac{1}{a (-b^2 + 4 a c) (a + x^n (b + c x^n))^{3/2}} 2 x^2 \left(-\frac{(b^2 - 2 a c + b c x^n) (a + x^n (b + c x^n))}{n} + \left(16 a^2 b c (1+n) x^n (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \text{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] / \left((-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c}) n (2+n) \left((b + \sqrt{b^2 - 4 a c}) n x^n \text{AppellF1} \left[2 + \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - (-b + \sqrt{b^2 - 4 a c}) n x^n \text{AppellF1} \left[2 + \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - 8 a (1+n) \text{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \left(a^2 (2+n) (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \text{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] / \left(4 a (2+n) \text{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - n x^n \left((b + \sqrt{b^2 - 4 a c}) \text{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{2}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \right.$$

$$\begin{aligned}
 & \left((b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) - \\
 & \left(a b^2 (2+n) (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(4c \left(4a (2+n) \operatorname{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left((b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{2}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + (b - \sqrt{b^2 - 4ac}) \right. \right. \\
 & \quad \quad \left. \left. \left. \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right] \right) \right) \right) - \\
 & \left(2a^2 (2+n) (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(n \left(4a (2+n) \operatorname{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left((b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{2}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + (b - \sqrt{b^2 - 4ac}) \right. \right. \\
 & \quad \quad \left. \left. \left. \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right] \right) \right) \right) + \\
 & \left(a b^2 (2+n) (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(c n \left(4a (2+n) \operatorname{AppellF1} \left[\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left((b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{2}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + (b - \sqrt{b^2 - 4ac}) \right. \right. \\
 & \quad \quad \left. \left. \left. \left. \operatorname{AppellF1} \left[\frac{2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 592: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(a+b x^n+c x^{2 n})^{3/2}} dx$$

Optimal (type 6, 142 leaves, 2 steps):

$$\left(x \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right. \\ \left. \text{AppellF1}\left[\frac{1}{n}, \frac{3}{2}, \frac{3}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] \right) / \left(a \sqrt{a + b x^n + c x^{2 n}} \right)$$

Result (type 6, 1876 leaves):

$$\frac{1}{a (-b^2 + 4 a c) (a + x^n (b + c x^n))^{3/2}} \\ 2 x \left(-\frac{(b^2 - 2 a c + b c x^n) (a + x^n (b + c x^n))}{n} + \left(4 a^2 b c (1 + 2 n) x^n (b - \sqrt{b^2 - 4 a c} + 2 c x^n) \right. \right. \\ \left. \left. (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \right. \right. \right. \\ \left. \left. \left. \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \left((-b + \sqrt{b^2 - 4 a c}) (b + \sqrt{b^2 - 4 a c}) n (1 + n) \right) \right. \\ \left. \left(-4 (a + 2 a n) \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \right. \\ \left. \left. n x^n \left((b + \sqrt{b^2 - 4 a c}) \text{AppellF1}\left[2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, \right. \right. \right. \right. \\ \left. \left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + (b - \sqrt{b^2 - 4 a c}) \right. \right. \\ \left. \left. \left. \left. \left. \text{AppellF1}\left[2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) \right) - \\ \left(2 a^2 (1 + n) (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \right. \\ \left. \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ \left((b + \sqrt{b^2 - 4 a c}) n x^n \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] - \right. \\ \left. (-b + \sqrt{b^2 - 4 a c}) n x^n \text{AppellF1}\left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] - \right. \\ \left. 4 a (1 + n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) + \\ \left(a b^2 (1 + n) (b - \sqrt{b^2 - 4 a c} + 2 c x^n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \\
 & \left(2 c \left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right], \right. \\
 & \quad \left. \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right) - \left(-b+\sqrt{b^2-4 a c}\right) n x^n \\
 & \quad \text{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \\
 & \quad 4 a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \Big) + \\
 & \left(2 a^2(1+n)\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \quad \left. \left(n\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right], \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right) - \right. \\
 & \quad \left. \left(-b+\sqrt{b^2-4 a c}\right) n x^n \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. 4 a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \Big) \right) - \\
 & \left(a b^2(1+n)\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \quad \left. \left(c n\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right], \right. \right. \\
 & \quad \left. \left. \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right) - \left(-b+\sqrt{b^2-4 a c}\right) n x^n \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. 4 a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \Big) \Big) \right)
 \end{aligned}$$

Problem 594: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^2 (a+b x^n+c x^{2 n})^{3/2}} dx$$

Optimal (type 6, 152 leaves, 2 steps):

$$- \left(\left(\sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{3}{2}, \frac{3}{2}, -\frac{1-n}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left(a x \sqrt{a + b x^n + c x^{2 n}} \right) \right)$$

Result (type 6, 2225 leaves):

$$\begin{aligned} & \frac{2(-b^2 + 2ac - bcx^n)}{a(-b^2 + 4ac)nx\sqrt{a + bx^n + cx^{2n}}} + \\ & \left(8abc(-1 + 2n)x^{-1+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \left. \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (-1+n)n(a + x^n(b + cx^n))^{3/2} \right. \\ & \left(\left(b + \sqrt{b^2 - 4ac} \right) nx^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\ & \left. \left(-b + \sqrt{b^2 - 4ac} \right) nx^n \operatorname{AppellF1} \left[2 - \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\ & \left. \left. 4a(1 - 2n) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\ & \left(4ab^2(-1+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \left. \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) x(a + x^n(b + cx^n))^{3/2} \right. \\ & \left(-4a(-1+n) \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\ & nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\ & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\ & \left. \left. 2 - \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\ & \left(16a^2c(-1+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \left. \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \end{aligned}$$

$$\begin{aligned}
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) x \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \left(-4a(-1+n) \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. 2 - \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) + \\
 & \left(8ab^2(-1+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) nx \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \left(-4a(-1+n) \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. 2 - \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) - \\
 & \left(16a^2c(-1+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) nx \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \left(-4a(-1+n) \operatorname{AppellF1} \left[-\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-1+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-1+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 595: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x^3 (a + bx^n + cx^{2n})^{3/2}} dx$$

Optimal (type 6, 154 leaves, 2 steps):

$$-\left(\left(\sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \operatorname{AppellF1}\left[-\frac{2}{n}, \frac{3}{2}, \frac{3}{2}, -\frac{2-n}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}\right] \right) / \left(2ax^2 \sqrt{a + bx^n + cx^{2n}} \right) \right)$$

Result (type 6, 2221 leaves):

$$\begin{aligned} & \frac{2(-b^2 + 2ac - bcx^n)}{a(-b^2 + 4ac)nx^2\sqrt{a + bx^n + cx^{2n}}} + \\ & \left(32abc(-1+n)x^{-2+n} \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \quad \left. \operatorname{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] \right) / \\ & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (-2+n)n(a+x^n(b+cx^n))^{3/2} \right. \\ & \quad \left(\left(b + \sqrt{b^2 - 4ac} \right) nx^n \operatorname{AppellF1}\left[2 - \frac{2}{n}, \frac{1}{2}, \frac{3}{2}, 3 - \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] - \right. \\ & \quad \left. \left(-b + \sqrt{b^2 - 4ac} \right) nx^n \operatorname{AppellF1}\left[2 - \frac{2}{n}, \frac{3}{2}, \frac{1}{2}, 3 - \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] - \right. \\ & \quad \left. \left. 8a(-1+n) \operatorname{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] \right) \right) + \\ & \left(2ab^2(-2+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \quad \left. \operatorname{AppellF1}\left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] \right) / \\ & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) x^2 (a+x^n(b+cx^n))^{3/2} \right. \\ & \quad \left(-4a(-2+n) \operatorname{AppellF1}\left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] + \right. \\ & \quad nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1}\left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] + \right. \\ & \quad \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1}\left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] \right) \right) - \\ & \left(8a^2c(-2+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \quad \left. \operatorname{AppellF1}\left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}}\right] \right) / \end{aligned}$$

$$\begin{aligned}
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) x^2 (a + x^n (b + cx^n))^{3/2} \right. \\
 & \left(-4a(-2+n) \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. 2 - \frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) + \\
 & \left(8a^2 b^2 (-2+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) nx^2 (a + x^n (b + cx^n))^{3/2} \right. \\
 & \left(-4a(-2+n) \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. 2 - \frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) - \\
 & \left(16a^2 c (-2+n) \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) nx^2 (a + x^n (b + cx^n))^{3/2} \right. \\
 & \left(-4a(-2+n) \operatorname{AppellF1} \left[-\frac{2}{n}, \frac{1}{2}, \frac{1}{2}, \frac{-2+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. nx^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{1}{2}, \frac{3}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \right. \\
 & \left. \left(b - \sqrt{b^2 - 4ac} \right) \operatorname{AppellF1} \left[\frac{-2+n}{n}, \frac{3}{2}, \frac{1}{2}, 2 - \frac{2}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 600: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx)^m}{(a+bx^n+cx^{2n})^2} dx$$

Optimal (type 5, 328 leaves, 5 steps):

$$\frac{(dx)^{1+m} (b^2 - 2ac + bcx^n)}{a (b^2 - 4ac) dn (a + bx^n + cx^{2n})} +$$

$$\left(c \left(\frac{4ac(1+m-2n) - b^2(1+m-n)}{\sqrt{b^2 - 4ac}} - b(1+m-n) \right) (dx)^{1+m} \text{Hypergeometric2F1} \left[1, \right.$$

$$\left. \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}} \right] \right) / \left(a (b^2 - 4ac) (b - \sqrt{b^2 - 4ac}) d (1+m) n \right) -$$

$$\left(c \left(4ac(1+m-2n) - b^2(1+m-n) + b\sqrt{b^2 - 4ac} (1+m-n) \right) (dx)^{1+m} \right.$$

$$\left. \text{Hypergeometric2F1} \left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) /$$

$$\left(a (b^2 - 4ac)^{3/2} (b + \sqrt{b^2 - 4ac}) d (1+m) n \right)$$

Result (type 5, 3515 leaves):

$$\frac{x (dx)^m (-b^2 + 2ac - bcx^n)}{a (-b^2 + 4ac) n (a + bx^n + cx^{2n})} -$$

$$\left(bcx^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m+n}{n}} \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, \right. \right. \right.$$

$$\left. \left. -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) /$$

$$\left(a (-b^2 + 4ac) (1+m) \right) + \left(bcx^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m+n}{n}} \right.$$

$$\left. \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right.$$

$$\begin{aligned}
 & \left. 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \right] + \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \\
 & \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c} \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \Bigg/ \\
 & (a(-b^2+4ac)(1+m)n) + \left(b c m x^{1+n} (d x)^m (x^n)^{\frac{1-m}{n} - \frac{1-m-n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right) \right] + \right. \right. \\
 & \left. \left. \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c} \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \right) \Bigg/ (a(-b^2+4ac)(1+m)n) + \\
 & \left(b^2 x (d x)^m \left(\left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c} \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \right) \Bigg/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \\
 & \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.
 \end{aligned}$$

$$\left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \left/ \left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \left/ \right.$$

$$(a(-b^2 + 4ac)(1+m)) - \left(4cx(dx)^m \left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right.$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}}$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \left/ \right. \left((-b^2 + 4ac)(1+m) \right) -$$

$$\left(b^2 x(dx)^m \left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\left. \left. - \frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \right.$$

$$\left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right.$$

$$\left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Big/$$

$$(a(-b^2+4ac)(1+m)n) + \left(2cx(dx)^m \left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right.$$

$$\left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right/ \right. \right.$$

$$\left. \left. \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right. \right.$$

$$\left. \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right/ \right. \right. \right.$$

$$\left. \left. \left. \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \Big/ ((-b^2+4ac)(1+m)n) -$$

$$\left(b^2 m x (dx)^m \left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left. \left. \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right) \left/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \right. \\
 & \left((-b^2+4ac)(1+m)n \right) + \left(2cmx(dx)^m \left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n}-\frac{m}{n}} \right) \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n\right)} \right] \right) \right) \left/ \right. \\
 & \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n}-\frac{m}{n}} \right) \\
 & \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n\right)} \right] \right) \right) \left/ \right. \\
 & \left. \left. \left. \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \right) \left/ \left((-b^2+4ac)(1+m)n \right) \right)
 \end{aligned}$$

Problem 601: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx)^m}{(a+bx^n+cx^{2n})^3} dx$$

Optimal (type 5, 615 leaves, 6 steps):

$$\frac{(dx)^{1+m} (b^2 - 2ac + bcx^n)}{2a(b^2 - 4ac)dn(a+bx^n+cx^{2n})^2} -$$

$$\left((dx)^{1+m} (4a^2c^2(1+m-4n) - 5ab^2c(1+m-3n) + b^4(1+m-2n) - \right.$$

$$\left. bc(2ac(2+2m-7n) - b^2(1+m-2n))x^n \right) / \left(2a^2(b^2 - 4ac)^2 dn^2(a+bx^n+cx^{2n}) \right) -$$

$$\left(c \left(b\sqrt{b^2 - 4ac} (2ac(2+2m-7n) - b^2(1+m-2n)) (1+m-n) - \right. \right.$$

$$\left. b^4(1+m^2+m(2-3n) - 3n+2n^2) + 6ab^2c(1+m^2+m(2-4n) - 4n+3n^2) - \right.$$

$$\left. 8a^2c^2(1+m^2+m(2-6n) - 6n+8n^2) \right)$$

$$(dx)^{1+m} \text{Hypergeometric2F1} \left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}} \right] /$$

$$\left(2a^2(b^2 - 4ac)^{5/2} (b - \sqrt{b^2 - 4ac}) d(1+m)n^2 \right) -$$

$$\left(c \left(b\sqrt{b^2 - 4ac} (2ac(2+2m-7n) - b^2(1+m-2n)) (1+m-n) + \right. \right.$$

$$\left. b^4(1+m^2+m(2-3n) - 3n+2n^2) - 6ab^2c(1+m^2+m(2-4n) - 4n+3n^2) + \right.$$

$$\left. 8a^2c^2(1+m^2+m(2-6n) - 6n+8n^2) \right)$$

$$(dx)^{1+m} \text{Hypergeometric2F1} \left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}} \right] /$$

$$\left(2a^2(b^2 - 4ac)^{5/2} (b + \sqrt{b^2 - 4ac}) d(1+m)n^2 \right)$$

Result (type 5, 12289 leaves):

$$\frac{1}{1+m}$$

$$\left(-\frac{b^4}{a^3(-b^2+4ac)^2} + \frac{8b^2c}{a^2(-b^2+4ac)^2} - \frac{16c^2}{a(-b^2+4ac)^2} - \frac{b^4m}{a^3(-b^2+4ac)^2n^2} + \frac{5b^2cm}{a^2(-b^2+4ac)^2n^2} - \right.$$

$$\frac{2c^2(1+m)^2}{a(-b^2+4ac)^2n^2} + \frac{b^4(-1-m^2)}{2a^3(-b^2+4ac)^2n^2} + \frac{5b^2c(1+m^2)}{2a^2(-b^2+4ac)^2n^2} +$$

$$\left. \frac{3b^4(1+m)}{2a^3(-b^2+4ac)^2n} - \frac{21b^2c(1+m)}{2a^2(-b^2+4ac)^2n} + \frac{12c^2(1+m)}{a(-b^2+4ac)^2n} \right) x(dx)^m +$$

$$\left((b^4 - 5ab^2c + 4a^2c^2 + 2b^4m - 10ab^2cm + 8a^2c^2m + b^4m^2 - 5ab^2cm^2 + 4a^2c^2m^2 - 3b^4n + 21ab^2cn \right.$$

$$\left. - 24a^2c^2n - 3b^4mn + 21ab^2cmn - 24a^2c^2mn + 2b^4n^2 - 16ab^2cn^2 + 32a^2c^2n^2) x(dx)^m \right) /$$

$$\left(2a^3(-b^2+4ac)^2(1+m)n^2 \right) + \frac{x(dx)^m(-b^2+2ac-bcx^n)}{2a(-b^2+4ac)n(a+bx^n+cx^{2n})^2} +$$

$$(x^{-m}(dx)^m(-b^4x^{1+m} + 5ab^2cx^{1+m} - 4a^2c^2x^{1+m} - b^4mx^{1+m} + 5ab^2cmx^{1+m} - 4a^2c^2mx^{1+m} + 2b^4nx^{1+m} -$$

$$15ab^2cnx^{1+m} + 16a^2c^2nx^{1+m} - b^3cx^{1+m+n} + 4ab^2c^2x^{1+m+n} - b^3cmx^{1+m+n} + 4ab^2c^2mx^{1+m+n} +$$

$$2b^3cnx^{1+m+n} - 14ab^2c^2nx^{1+m+n})) / \left(2a^2(-b^2+4ac)^2n^2(a+bx^n+cx^{2n}) \right) +$$

$$\left(b^3 c x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m+n}{n}} \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, \right. \right. \right. \\ \left. \left. \left. -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right. \right. \\ \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right) \right) /$$

$$\left(a^2 (-b^2 + 4ac)^2 (1+m) \right) - \left(7bc^2 x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m+n}{n}} \right)$$

$$\left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right. \\ \left. \left. -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[\right. \right. \\ \left. \left. -\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) / \left(a (-b^2 + 4ac)^2 (1+m) \right) +$$

$$\left(b^3 c x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m+n}{n}} \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[\right. \right. \right. \\ \left. \left. \left. -\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right. \right. \\ \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right) \right) /$$

$$\left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \right) /$$

$$\left(2a^2 (-b^2+4ac)^2 (1+m)n^2 \right) - \left(2bc^2 x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n}-\frac{1+m-n}{n}} \right.$$

$$\left. \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n}-\frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right.$$

$$\left. \left. \left. 1-\frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n}-\frac{m}{n}} \right) \right) \right) /$$

$$\left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \right) /$$

$$\left(a (-b^2+4ac)^2 (1+m)n^2 \right) + \left(b^3 cm x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n}-\frac{1+m-n}{n}} \right.$$

$$\left. \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n}-\frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right.$$

$$\left. \left. \left. 1-\frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1}{n}-\frac{m}{n}} \right) \right) \right) /$$

$$\left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \right) /$$

$$\begin{aligned}
 & \left(a^2 (-b^2 + 4ac)^2 (1+m)n^2 \right) - \left(4bc^2 m x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m-n}{n}} \right. \\
 & \left. \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right. \right. \\
 & \left. \left. \left. \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right) / \\
 & \left(a (-b^2 + 4ac)^2 (1+m)n^2 \right) + \left(b^3 c m^2 x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m-n}{n}} \right. \\
 & \left. \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right. \right. \\
 & \left. \left. \left. \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right) / \\
 & \left(2a^2 (-b^2 + 4ac)^2 (1+m)n^2 \right) - \left(2bc^2 m^2 x^{1+n} (dx)^m (x^n)^{\frac{1+m}{n} - \frac{1+m-n}{n}} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1-m}{n}} \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \\
 & \quad \left. \left. 1-\frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right) \right] + \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1-m}{n}} \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c} \left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right) \right] \right) \Bigg/ \\
 & \left(a(-b^2+4ac)^2(1+m)n^2 \right) - \left(3b^3cx^{1+n}(dx)^m(x^n)^{\frac{1-m}{n}-\frac{1+m-n}{n}} \right. \\
 & \quad \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1-m}{n}} \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \\
 & \quad \left. \left. 1-\frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right) \right] + \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1-m}{n}} \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c} \left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right) \right] \right) \Bigg/ \\
 & \left(2a^2(-b^2+4ac)^2(1+m)n \right) + \left(9b^2cx^{1+n}(dx)^m(x^n)^{\frac{1-m}{n}-\frac{1+m-n}{n}} \right. \\
 & \quad \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1-m}{n}} \operatorname{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. \left. 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1-m}{n} \frac{m}{n}} \right. \right. \right. \\
& \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right) \right) / \\
& \left(a(-b^2 + 4ac)^2 (1+m)n \right) - \left(3b^3 cm x^{1+n} (dx)^m (x^n)^{\frac{1-m}{n} - \frac{1+m+n}{n}} \right. \\
& \left. \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1-m}{n} \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right. \\
& \left. \left. \left. 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1-m}{n} \frac{m}{n}} \right) \right) \\
& \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right) \right) / \\
& \left(2a^2 (-b^2 + 4ac)^2 (1+m)n \right) + \left(9b^3 c^2 m x^{1+n} (dx)^m (x^n)^{\frac{1-m}{n} - \frac{1+m+n}{n}} \right. \\
& \left. \left(-\frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1-m}{n} \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, \right. \right. \right. \\
& \left. \left. \left. 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \left(\frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{\frac{1-m}{n} \frac{m}{n}} \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right) \Big/ \\
 & \left(a(-b^2+4ac)^2(1+m)n - \left(b^4 x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1+m}{n}} \right) \right) \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right) \Big/ \\
 & \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1+m}{n}} \\
 & \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right) \Big/ \\
 & \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \Big) \Big/ \left(a^2(-b^2+4ac)^2(1+m) + \right. \\
 & \left. \left(8b^2cx(dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1}\left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right) \Big/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right. \\
 & \left. \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1}\left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right) \Big/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) +
 \end{aligned}$$

$$\left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \left/ \left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \left/ \right.$$

$$\left(a(-b^2 + 4ac)^2(1+m) \right) - \left(16c^2 x(dx)^m \left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \right.$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}}$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \left/ \left((-b^2 + 4ac)^2(1+m) \right) - \right.$$

$$\left(b^4 x(dx)^m \left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\left. \left. -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \right.$$

$$\left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1}{n} - \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right.$$

$$\left. \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \right.$$

$$\left(2a^2(-b^2+4ac)^2(1+m)n^2 \right) + \left(5b^2cx(dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right) \right.$$

$$\left. \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right/ \right.$$

$$\left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}}$$

$$\left. \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right/ \right.$$

$$\left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \left(2a(-b^2+4ac)^2(1+m)n^2 \right) - \right.$$

$$\left(2c^2x(dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right.$$

$$\left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \left/ \left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \left/ \right.$$

$$\left((-b^2 + 4ac)^2 (1+m)n^2 - b^4 m x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right) \right.$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}}$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \left) \left/ \left(a^2 (-b^2 + 4ac)^2 (1+m)n^2 + \right. \right.$$

$$\left. \left(5b^2 c m x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \left/ \left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \right.$$

$$\left. \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \left/ \left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \left/ \right.$$

$$\left(a(-b^2 + 4ac)^2(1+m)n^2 - 4c^2m \times (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right/$$

$$\left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}}$$

$$\left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right/$$

$$\left(\frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \left/ \left((-b^2 + 4ac)^2(1+m)n^2 - \right. \right.$$

$$\left. \left. b^4 m^2 \times (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left(-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \left/ \left(\frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \right.$$

$$\left. \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right.$$

$$\begin{aligned}
 & \left. - \frac{-b + \sqrt{b^2 - 4 a c}}{2 c} \right] \left/ \left(\frac{b (-b + \sqrt{b^2 - 4 a c})}{2 c} + \frac{(-b + \sqrt{b^2 - 4 a c})^2}{2 c} \right) \right) \left/ \right. \\
 & \left(2 a^2 (-b^2 + 4 a c)^2 (1 + m) n^2 \right) + \left(5 b^2 c m^2 x (d x)^m \left(\left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1} \left[-\frac{1 + m}{n}, -\frac{1 + m}{n}, 1 - \frac{1 + m}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left(-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) \right/ \\
 & \left(\frac{b (-b - \sqrt{b^2 - 4 a c})}{2 c} + \frac{(-b - \sqrt{b^2 - 4 a c})^2}{2 c} \right) + \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \\
 & \left. \text{Hypergeometric2F1} \left[-\frac{1 + m}{n}, -\frac{1 + m}{n}, 1 - \frac{1 + m}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left(-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) \left/ \right. \\
 & \left. \left(\frac{b (-b + \sqrt{b^2 - 4 a c})}{2 c} + \frac{(-b + \sqrt{b^2 - 4 a c})^2}{2 c} \right) \right) \left/ \left(2 a (-b^2 + 4 a c)^2 (1 + m) n^2 \right) - \right. \\
 & \left(2 c^2 m^2 x (d x)^m \left(\left(1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1} \left[-\frac{1 + m}{n}, -\frac{1 + m}{n}, 1 - \frac{1 + m}{n}, \right. \right. \right. \\
 & \left. \left. - \frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left(-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) \left/ \left(\frac{b (-b - \sqrt{b^2 - 4 a c})}{2 c} + \frac{(-b - \sqrt{b^2 - 4 a c})^2}{2 c} \right) \right) + \\
 & \left(1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-\frac{1}{n} \frac{m}{n}} \text{Hypergeometric2F1} \left[-\frac{1 + m}{n}, -\frac{1 + m}{n}, 1 - \frac{1 + m}{n}, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Bigg/ \\
 & \left((-b^2+4ac)^2 (1+m)n^2 \right) + \left(3b^4 x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1-m}{n}} \right. \right. \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \right/ \\
 & \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1-m}{n}} \\
 & \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \right/ \\
 & \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \Bigg) \Bigg/ \left(2a^2 (-b^2+4ac)^2 (1+m)n \right) - \\
 & \left(21b^2 c x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1-m}{n}} \right. \right. \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \right/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \\
 & \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1-m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right.
 \end{aligned}$$

$$\left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \left/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \left/ \right.$$

$$(2a(-b^2+4ac)^2(1+m)n) + \left(12c^2 x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right) \right.$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}}$$

$$\left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \left/ \right.$$

$$\left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \left) \left/ \left((-b^2+4ac)^2(1+m)n) + \right. \right.$$

$$\left(3b^4 m x (dx)^m \left(\left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \left/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, \right.$$

$$\begin{aligned}
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right) \right) \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Bigg/ \\
 & \left(2a^2(-b^2+4ac)^2(1+m)n - 21b^2cmx(dx)^m \left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \right. \\
 & \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \\
 & \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \\
 & \left. \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \\
 & \left. \left. \left. \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \right) \Bigg/ \left(2a(-b^2+4ac)^2(1+m)n + \right. \\
 & \left. \left(12c^2mx(dx)^m \left(1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left(-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \Bigg/ \\
 & \left. \left. \left. \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \right) \Bigg/ \left(2a(-b^2+4ac)^2(1+m)n + \right. \\
 & \left. \left(12c^2mx(dx)^m \left(1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-\frac{1+m}{n}} \text{Hypergeometric2F1} \left[-\frac{1+m}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1+m}{n}, 1 - \frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left(-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \Bigg/
 \end{aligned}$$

$$\left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1+m}{n}, -\frac{1+m}{n}, 1-\frac{1+m}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right.\right.\right. /$$

$$\left. \left. \left. \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c}\right)\right)\right)\right) / \left((-b^2+4ac)^2(1+m)n\right)$$

Problem 602: Result more than twice size of optimal antiderivative.

$$\int (d x)^m (a+b x^n+c x^{2 n})^{3/2} d x$$

Optimal (type 6, 161 leaves, 2 steps):

$$\left(a(d x)^{1+m} \sqrt{a+b x^n+c x^{2 n}}\right.$$

$$\left. \text{AppellF1}\left[\frac{1+m}{n}, -\frac{3}{2}, -\frac{3}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right]\right) /$$

$$\left(d(1+m) \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}}\right)$$

Result (type 6, 5259 leaves):

$$x^{-m}(d x)^m \sqrt{a+b x^n+c x^{2 n}}\left(\frac{(4 a c+8 a c m+4 a c m^2+24 a c n+24 a c m n+3 b^2 n^2+32 a c n^2) x^{1+m}}{4 c(1+m+n)(1+m+2 n)(1+m+3 n)}+\right.$$

$$\left.\frac{b(2+2 m+7 n) x^{1+m+n}}{2(1+m+2 n)(1+m+3 n)}+\frac{c x^{1+m+2 n}}{1+m+3 n}\right)+$$

$$\left(12 a^4 n^2 x(d x)^m\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right.$$

$$\left.\text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) /$$

$$\left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+m)(1+m+2 n)(1+m+3 n)\left(a+x^n(b+c x^n)\right)^{3/2}\right.$$

$$\left.4 a(1+m+n) \text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right.$$

$$n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2 n}{n},\right.\right.$$

$$\left.\left.-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right)\right.$$

$$\left.\left.\left.\left.\text{AppellF1}\left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right)\right)\right)$$

$$\begin{aligned}
 & \left(3 a^3 b^2 n^2 x (d x)^m \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(c \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+m) (1+m+2 n) (1+m+3 n) \left(a + x^n (b + c x^n) \right)^{3/2} \right. \\
 & \quad \left(4 a (1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2 n}{n}, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \left(b - \sqrt{b^2 - 4 a c} \right) \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) + \\
 & \left(12 a^4 m n^2 x (d x)^m \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+m) (1+m+2 n) (1+m+3 n) \left(a + x^n (b + c x^n) \right)^{3/2} \right. \\
 & \quad \left(4 a (1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2 n}{n}, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \left(b - \sqrt{b^2 - 4 a c} \right) \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) - \\
 & \left(3 a^3 b^2 m n^2 x (d x)^m \left(b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left(c \left(b - \sqrt{b^2 - 4 a c} \right) \left(b + \sqrt{b^2 - 4 a c} \right) (1+m) (1+m+2 n) (1+m+3 n) \left(a + x^n (b + c x^n) \right)^{3/2} \right. \\
 & \quad \left(4 a (1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2 n}{n}, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \left(b - \sqrt{b^2 - 4 a c} \right) \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\
 & \left(24 a^4 n^3 x (dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m) (1+m+2n) (1+m+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left. \left(4a (1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\
 & \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right) + \\
 & \left(12 a^3 b n^2 x^{1+n} (dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) / \\
 & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m+n)^2 (1+m+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left. \left(4a (1+m+2n) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\
 & \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right) - \\
 & \left(3 a^2 b^3 n^2 x^{1+n} (dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) / \\
 & \left(c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m+n)^2 (1+m+3n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \left. \left(4a (1+m+2n) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right. \right. \\
 & \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \left. \left. \left. \left. \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}] + \left(b - \sqrt{b^2-4 a c} \right) \\
 & \text{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \Big) \Big) + \\
 & \left(12 a^3 b m n^2 x^{1+n} (d x)^m \left(b - \sqrt{b^2-4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2-4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(\left(b - \sqrt{b^2-4 a c} \right) \left(b + \sqrt{b^2-4 a c} \right) (1+m+n)^2 (1+m+3 n) \left(a + x^n (b+c x^n) \right)^{3/2} \right. \\
 & \quad \left. \left[4 a (1+m+2 n) \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \right. \\
 & \quad \left. \left. n x^n \left(\left(b + \sqrt{b^2-4 a c} \right) \text{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3 n}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \left(b - \sqrt{b^2-4 a c} \right) \right. \right. \\
 & \quad \left. \left. \left. \left. \text{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right] \right] \right] \right) - \\
 & \left(3 a^2 b^3 m n^2 x^{1+n} (d x)^m \left(b - \sqrt{b^2-4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2-4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(c \left(b - \sqrt{b^2-4 a c} \right) \left(b + \sqrt{b^2-4 a c} \right) (1+m+n)^2 (1+m+3 n) \left(a + x^n (b+c x^n) \right)^{3/2} \right. \\
 & \quad \left. \left[4 a (1+m+2 n) \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \right. \\
 & \quad \left. \left. n x^n \left(\left(b + \sqrt{b^2-4 a c} \right) \text{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3 n}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \left(b - \sqrt{b^2-4 a c} \right) \right. \right. \\
 & \quad \left. \left. \left. \left. \text{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right] \right] \right] \right) + \\
 & \left(18 a^3 b n^3 x^{1+n} (d x)^m \left(b - \sqrt{b^2-4 a c} + 2 c x^n \right) \left(b + \sqrt{b^2-4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left(\left(b - \sqrt{b^2-4 a c} \right) \left(b + \sqrt{b^2-4 a c} \right) (1+m+n)^2 (1+m+3 n) \left(a + x^n (b+c x^n) \right)^{3/2} \right. \\
 & \quad \left. \left[4 a (1+m+2 n) \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3n}{n}, \right. \right. \\
 & \quad \left. \left. - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\
 & \left(3 a^2 b^3 n^3 x^{1+n} (dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(2c \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m+n)^2 (1+m+3n) (a+x^n(b+cx^n))^{3/2} \right. \\
 & \quad \left. \left(4a(1+m+2n) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3n}{n}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right)
 \end{aligned}$$

Problem 603: Result more than twice size of optimal antiderivative.

$$\int (dx)^m \sqrt{a+bx^n+cx^{2n}} dx$$

Optimal (type 6, 160 leaves, 2 steps):

$$\begin{aligned}
 & \left((dx)^{1+m} \sqrt{a+bx^n+cx^{2n}} \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, -\frac{1}{2}, -\frac{1}{2}, \frac{1+m+n}{n}, - \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(d(1+m) \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \right)
 \end{aligned}$$

Result (type 6, 930 leaves):

$$\begin{aligned}
 & \frac{x (dx)^m \sqrt{a+bx^n+cx^{2n}}}{1+m+n} + \left(4a^3 n x (dx)^m \left(b - \sqrt{b^2-4ac} + 2cx^n \right) \left(b + \sqrt{b^2-4ac} + 2cx^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2-4ac} \right) \left(b + \sqrt{b^2-4ac} \right) (1+m) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \quad \left(4a (1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2-4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2-4ac} \right) \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) + \\
 & \left(2a^2 b n (1+m+2n) x^{1+n} (dx)^m \left(b - \sqrt{b^2-4ac} + 2cx^n \right) \left(b + \sqrt{b^2-4ac} + 2cx^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) / \\
 & \left(\left(b - \sqrt{b^2-4ac} \right) \left(b + \sqrt{b^2-4ac} \right) (1+m+n)^2 (a+x^n (b+cx^n))^{3/2} \right. \\
 & \quad \left(4a (1+m+2n) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] - \right. \\
 & \quad \left. n x^n \left(\left(b + \sqrt{b^2-4ac} \right) \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3n}{n}, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] + \left(b - \sqrt{b^2-4ac} \right) \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+2n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 604: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx)^m}{\sqrt{a+bx^n+cx^{2n}}} dx$$

Optimal (type 6, 160 leaves, 2 steps):

$$\left((dx)^{1+m} \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2-4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2-4ac}}} \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \right. \right. \\
 \left. \left. \frac{1+m+n}{n}, -\frac{2cx^n}{b - \sqrt{b^2-4ac}}, -\frac{2cx^n}{b + \sqrt{b^2-4ac}} \right] \right) / \left(d (1+m) \sqrt{a+bx^n+cx^{2n}} \right)$$

Result (type 6, 440 leaves):

$$\begin{aligned} & \left(4 a^2 (1+m+n) x (dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left(\left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m) \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\ & \quad \left(4a(1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\ & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \\ & \quad \quad \left. \left. -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \\ & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) \end{aligned}$$

Problem 605: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx)^m}{(a + bx^n + cx^{2n})^{3/2}} dx$$

Optimal (type 6, 163 leaves, 2 steps):

$$\begin{aligned} & \left((dx)^{1+m} \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \text{AppellF1} \left[\frac{1+m}{n}, \frac{3}{2}, \frac{3}{2}, \right. \right. \\ & \quad \left. \left. \frac{1+m+n}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(ad(1+m) \sqrt{a + bx^n + cx^{2n}} \right) \end{aligned}$$

Result (type 6, 3743 leaves):

$$\begin{aligned} & \frac{2x(dx)^m(-b^2 + 2ac - bcx^n)}{a(-b^2 + 4ac)n\sqrt{a + bx^n + cx^{2n}}} - \\ & \left(4ab^2(1+m+n)x(dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\ & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m) \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\ & \quad \left(4a(1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\ & \quad \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}] + (b-\sqrt{b^2-4ac}) \\
 & \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \Big) \Big) \Big) + \\
 & \left(16a^2c(1+m+n)x(dx)^m(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right) / \\
 & \left((-b^2+4ac)(b-\sqrt{b^2-4ac})(b+\sqrt{b^2-4ac})(1+m)(a+x^n(b+cx^n))^{3/2} \right. \\
 & \left. \left(4a(1+m+n)\text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \right. \\
 & \left. \left. nx^n\left(\left(b+\sqrt{b^2-4ac}\right)\text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] + (b-\sqrt{b^2-4ac}) \right. \right. \right. \\
 & \left. \left. \left. \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right)\right)\right) \Big) \Big) + \\
 & \left(8a^2b^2(1+m+n)x(dx)^m(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right) / \\
 & \left((-b^2+4ac)(b-\sqrt{b^2-4ac})(b+\sqrt{b^2-4ac})(1+m)n(a+x^n(b+cx^n))^{3/2} \right. \\
 & \left. \left(4a(1+m+n)\text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \right. \\
 & \left. \left. nx^n\left(\left(b+\sqrt{b^2-4ac}\right)\text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] + (b-\sqrt{b^2-4ac}) \right. \right. \right. \\
 & \left. \left. \left. \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right)\right)\right) \Big) \Big) - \\
 & \left(16a^2c(1+m+n)x(dx)^m(b-\sqrt{b^2-4ac}+2cx^n)(b+\sqrt{b^2-4ac}+2cx^n) \right. \\
 & \left. \text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right) / \\
 & \left((-b^2+4ac)(b-\sqrt{b^2-4ac})(b+\sqrt{b^2-4ac})(1+m)n(a+x^n(b+cx^n))^{3/2} \right. \\
 & \left. \left(4a(1+m+n)\text{AppellF1}\left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] - \right. \right. \\
 & \left. \left. nx^n\left(\left(b+\sqrt{b^2-4ac}\right)\text{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] + (b-\sqrt{b^2-4ac}) \right. \right. \right. \\
 & \left. \left. \left. \text{AppellF1}\left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}, \frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right)\right)\right) \Big) \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \\
 & \quad \left. \left. - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
 & \left(8ab^2m(1+m+n)x(dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m)n \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left. \left(4a(1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) - \\
 & \left(16a^2cm(1+m+n)x(dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) (1+m)n \left(a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left. \left(4a(1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \right. \\
 & \quad \left. \left. n x^n \left(\left(b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \left(b - \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) + \\
 & \left(8abc(1+m+2n)x^{1+n}(dx)^m \left(b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2n}{n}, - \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left((-b^2 + 4ac) \left(b - \sqrt{b^2 - 4ac} \right) \left(b + \sqrt{b^2 - 4ac} \right) n(1+m+n) \left(a + x^n (b + cx^n) \right)^{3/2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(4 a (1+m+2 n) \operatorname{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3 n}{n}, \right. \right. \\
 & \quad \quad \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \left(b-\sqrt{b^2-4 a c} \right) \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) + \\
 & \left(8 a b c m (1+m+2 n) x^{1+n} (d x)^m \left(b-\sqrt{b^2-4 a c}+2 c x^n \right) \left(b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left((-b^2+4 a c) \left(b-\sqrt{b^2-4 a c} \right) \left(b+\sqrt{b^2-4 a c} \right) n (1+m+n) \left(a+x^n \left(b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left(4 a (1+m+2 n) \operatorname{AppellF1}\left[\frac{1+m+n}{n}, \frac{1}{2}, \frac{1}{2}, \frac{1+m+2 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \quad n x^n \left(\left(b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{1}{2}, \frac{3}{2}, \frac{1+m+3 n}{n}, \right. \right. \\
 & \quad \quad \quad \left. \left. -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \left(b-\sqrt{b^2-4 a c} \right) \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1}\left[\frac{1+m+2 n}{n}, \frac{3}{2}, \frac{1}{2}, \frac{1+m+3 n}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 606: Result more than twice size of optimal antiderivative.

$$\int (d x)^m (a+b x^n+c x^{2 n})^p d x$$

Optimal (type 6, 158 leaves, 2 steps):

$$\begin{aligned}
 & \frac{1}{d (1+m)} (d x)^{1+m} \left(1 + \frac{2 c x^n}{b-\sqrt{b^2-4 a c}} \right)^{-p} \left(1 + \frac{2 c x^n}{b+\sqrt{b^2-4 a c}} \right)^{-p} (a+b x^n+c x^{2 n})^p \\
 & \operatorname{AppellF1}\left[\frac{1+m}{n}, -p, -p, \frac{1+m+n}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right]
 \end{aligned}$$

Result (type 6, 534 leaves):

$$\begin{aligned}
 & - \left(\left(2^{-1-p} \left(b + \sqrt{b^2 - 4ac} \right) (1+m+n) x (dx)^m \left(\frac{b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)^{-p} \left(-b + \sqrt{b^2 - 4ac} - 2cx^n \right) \right. \right. \\
 & \quad \left. \left(\frac{b - \sqrt{b^2 - 4ac} + 2cx^n}{c} \right)^p \left(-2a + \left(-b + \sqrt{b^2 - 4ac} \right) x^n \right)^2 (a + x^n (b + cx^n))^{-1+p} \right. \\
 & \quad \left. \text{AppellF1} \left[\frac{1+m}{n}, -p, -p, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left(\left(-b + \sqrt{b^2 - 4ac} \right) (1+m) \left(b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \left(-2a(1+m+n) \text{AppellF1} \left[\frac{1+m}{n}, -p, -p, \frac{1+m+n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left. np x^n \left(\left(-b + \sqrt{b^2 - 4ac} \right) \text{AppellF1} \left[\frac{1+m+n}{n}, 1-p, -p, \frac{1+m+2n}{n}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \left(b + \sqrt{b^2 - 4ac} \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{1+m+n}{n}, -p, 1-p, \frac{1+m+2n}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 607: Result more than twice size of optimal antiderivative.

$$\int (d+ex)^3 (a+b(d+ex)^2+c(d+ex)^4) dx$$

Optimal (type 1, 46 leaves, 3 steps):

$$\frac{a(d+ex)^4}{4e} + \frac{b(d+ex)^6}{6e} + \frac{c(d+ex)^8}{8e}$$

Result (type 1, 150 leaves):

$$\begin{aligned}
 & d^3 (a + b d^2 + c d^4) x + \frac{1}{2} d^2 (3 a + 5 b d^2 + 7 c d^4) e x^2 + \frac{1}{3} d (3 a + 10 b d^2 + 21 c d^4) e^2 x^3 + \\
 & \frac{1}{4} (a + 10 b d^2 + 35 c d^4) e^3 x^4 + d (b + 7 c d^2) e^4 x^5 + \frac{1}{6} (b + 21 c d^2) e^5 x^6 + c d e^6 x^7 + \frac{1}{8} c e^7 x^8
 \end{aligned}$$

Problem 608: Result more than twice size of optimal antiderivative.

$$\int (d+ex)^3 (a+b(d+ex)^2+c(d+ex)^4)^2 dx$$

Optimal (type 1, 89 leaves, 4 steps):

$$\frac{a^2(d+ex)^4}{4e} + \frac{ab(d+ex)^6}{3e} + \frac{(b^2+2ac)(d+ex)^8}{8e} + \frac{bc(d+ex)^{10}}{5e} + \frac{c^2(d+ex)^{12}}{12e}$$

Result (type 1, 401 leaves):

$$\begin{aligned}
 & d^3 (a+b d^2+c d^4)^2 x + \frac{1}{2} d^2 (3 a^2+10 a b d^2+7 b^2 d^4+14 a c d^4+18 b c d^6+11 c^2 d^8) e x^2 + \\
 & \frac{1}{3} d (3 a^2+20 a b d^2+21 b^2 d^4+42 a c d^4+72 b c d^6+55 c^2 d^8) e^2 x^3 + \\
 & \frac{1}{4} (a^2+20 a b d^2+35 b^2 d^4+70 a c d^4+168 b c d^6+165 c^2 d^8) e^3 x^4 + \\
 & \frac{1}{5} d (10 a b+35 b^2 d^2+70 a c d^2+252 b c d^4+330 c^2 d^6) e^4 x^5 + \\
 & \frac{1}{6} (2 a b+21 b^2 d^2+42 a c d^2+252 b c d^4+462 c^2 d^6) e^5 x^6 + \\
 & d (b^2+2 a c+24 b c d^2+66 c^2 d^4) e^6 x^7 + \frac{1}{8} (b^2+2 a c+72 b c d^2+330 c^2 d^4) e^7 x^8 + \\
 & \frac{1}{3} c d (6 b+55 c d^2) e^8 x^9 + \frac{1}{10} c (2 b+55 c d^2) e^9 x^{10} + c^2 d e^{10} x^{11} + \frac{1}{12} c^2 e^{11} x^{12}
 \end{aligned}$$

Problem 609: Result more than twice size of optimal antiderivative.

$$\int (d+e x)^3 (a+b (d+e x)^2+c (d+e x)^4)^3 d x$$

Optimal (type 1, 138 leaves, 4 steps):

$$\begin{aligned}
 & \frac{a^3 (d+e x)^4}{4 e} + \frac{a^2 b (d+e x)^6}{2 e} + \frac{3 a (b^2+a c) (d+e x)^8}{8 e} + \\
 & \frac{b (b^2+6 a c) (d+e x)^{10}}{10 e} + \frac{c (b^2+a c) (d+e x)^{12}}{4 e} + \frac{3 b c^2 (d+e x)^{14}}{14 e} + \frac{c^3 (d+e x)^{16}}{16 e}
 \end{aligned}$$

Result (type 1, 797 leaves):

$$\begin{aligned}
 & d^3 (a+b d^2+c d^4)^3 x + \frac{3}{2} d^2 (a+b d^2+c d^4)^2 (a+3 b d^2+5 c d^4) e x^2 + \\
 & d (a^3+10 a^2 b d^2+21 a b^2 d^4+21 a^2 c d^4+12 b^3 d^6+ \\
 & \quad 72 a b c d^6+55 b^2 c d^8+55 a c^2 d^8+78 b c^2 d^{10}+35 c^3 d^{12}) e^2 x^3 + \\
 & \frac{1}{4} (a^3+30 a^2 b d^2+105 a b^2 d^4+105 a^2 c d^4+84 b^3 d^6+504 a b c d^6+ \\
 & \quad 495 b^2 c d^8+495 a c^2 d^8+858 b c^2 d^{10}+455 c^3 d^{12}) e^3 x^4 + \\
 & \frac{3}{5} d (5 a^2 b+35 a b^2 d^2+35 a^2 c d^2+42 b^3 d^4+252 a b c d^4+330 b^2 c d^6+330 a c^2 d^6+ \\
 & \quad 715 b c^2 d^8+455 c^3 d^{10}) e^4 x^5 + \frac{1}{2} (a^2 b+21 a b^2 d^2+21 a^2 c d^2+42 b^3 d^4+ \\
 & \quad 252 a b c d^4+462 b^2 c d^6+462 a c^2 d^6+1287 b c^2 d^8+1001 c^3 d^{10}) e^5 x^6 + \frac{1}{7} d \\
 & (21 a b^2+21 a^2 c+84 b^3 d^2+504 a b c d^2+1386 b^2 c d^4+1386 a c^2 d^4+5148 b c^2 d^6+5005 c^3 d^8) e^6 x^7 + \\
 & \frac{3}{8} (a b^2+a^2 c+12 b^3 d^2+72 a b c d^2+330 b^2 c d^4+330 a c^2 d^4+1716 b c^2 d^6+2145 c^3 d^8) e^7 x^8 + \\
 & d (b^3+6 a b c+55 b^2 c d^2+55 a c^2 d^2+429 b c^2 d^4+715 c^3 d^6) e^8 x^9 + \\
 & \frac{1}{10} (b^3+6 a b c+165 b^2 c d^2+165 a c^2 d^2+2145 b c^2 d^4+5005 c^3 d^6) e^9 x^{10} + \\
 & 3 c d (b^2+a c+26 b c d^2+91 c^2 d^4) e^{10} x^{11} + \\
 & \frac{1}{4} c (b^2+a c+78 b c d^2+455 c^2 d^4) e^{11} x^{12} + c^2 d (3 b+35 c d^2) e^{12} x^{13} + \\
 & \frac{3}{14} c^2 (b+35 c d^2) e^{13} x^{14} + c^3 d e^{14} x^{15} + \frac{1}{16} c^3 e^{15} x^{16}
 \end{aligned}$$

Problem 610: Result more than twice size of optimal antiderivative.

$$\int (d f + e f x)^3 (a+b (d+e x)^2+c (d+e x)^4) dx$$

Optimal (type 1, 55 leaves, 3 steps):

$$\frac{a f^3 (d+e x)^4}{4 e} + \frac{b f^3 (d+e x)^6}{6 e} + \frac{c f^3 (d+e x)^8}{8 e}$$

Result (type 1, 154 leaves):

$$\begin{aligned}
 & f^3 \left(d^3 (a+b d^2+c d^4) x + \frac{1}{2} d^2 (3 a+5 b d^2+7 c d^4) e x^2 + \frac{1}{3} d (3 a+10 b d^2+21 c d^4) e^2 x^3 + \right. \\
 & \quad \left. \frac{1}{4} (a+10 b d^2+35 c d^4) e^3 x^4 + d (b+7 c d^2) e^4 x^5 + \frac{1}{6} (b+21 c d^2) e^5 x^6 + c d e^6 x^7 + \frac{1}{8} c e^7 x^8 \right)
 \end{aligned}$$

Problem 611: Result more than twice size of optimal antiderivative.

$$\int (d f + e f x)^3 (a+b (d+e x)^2+c (d+e x)^4)^2 dx$$

Optimal (type 1, 104 leaves, 4 steps):

$$\frac{a^2 f^3 (d+e x)^4}{4 e} + \frac{a b f^3 (d+e x)^6}{3 e} + \frac{(b^2+2 a c) f^3 (d+e x)^8}{8 e} + \frac{b c f^3 (d+e x)^{10}}{5 e} + \frac{c^2 f^3 (d+e x)^{12}}{12 e}$$

Result (type 1, 405 leaves):

$$\begin{aligned} & f^3 \left(d^3 (a+b d^2+c d^4)^2 x + \frac{1}{2} d^2 (3 a^2+10 a b d^2+7 b^2 d^4+14 a c d^4+18 b c d^6+11 c^2 d^8) e x^2 + \right. \\ & \quad \frac{1}{3} d (3 a^2+20 a b d^2+21 b^2 d^4+42 a c d^4+72 b c d^6+55 c^2 d^8) e^2 x^3 + \\ & \quad \frac{1}{4} (a^2+20 a b d^2+35 b^2 d^4+70 a c d^4+168 b c d^6+165 c^2 d^8) e^3 x^4 + \\ & \quad \frac{1}{5} d (10 a b+35 b^2 d^2+70 a c d^2+252 b c d^4+330 c^2 d^6) e^4 x^5 + \\ & \quad \frac{1}{6} (2 a b+21 b^2 d^2+42 a c d^2+252 b c d^4+462 c^2 d^6) e^5 x^6 + \\ & \quad d (b^2+2 a c+24 b c d^2+66 c^2 d^4) e^6 x^7 + \frac{1}{8} (b^2+2 a c+72 b c d^2+330 c^2 d^4) e^7 x^8 + \\ & \quad \left. \frac{1}{3} c d (6 b+55 c d^2) e^8 x^9 + \frac{1}{10} c (2 b+55 c d^2) e^9 x^{10} + c^2 d e^{10} x^{11} + \frac{1}{12} c^2 e^{11} x^{12} \right) \end{aligned}$$

Problem 612: Result more than twice size of optimal antiderivative.

$$\int (d f+e f x)^3 (a+b(d+e x)^2+c(d+e x)^4)^3 dx$$

Optimal (type 1, 159 leaves, 4 steps):

$$\begin{aligned} & \frac{a^3 f^3 (d+e x)^4}{4 e} + \frac{a^2 b f^3 (d+e x)^6}{2 e} + \frac{3 a (b^2+a c) f^3 (d+e x)^8}{8 e} + \\ & \frac{b (b^2+6 a c) f^3 (d+e x)^{10}}{10 e} + \frac{c (b^2+a c) f^3 (d+e x)^{12}}{4 e} + \frac{3 b c^2 f^3 (d+e x)^{14}}{14 e} + \frac{c^3 f^3 (d+e x)^{16}}{16 e} \end{aligned}$$

Result (type 1, 801 leaves):

$$\begin{aligned}
 & f^3 \left(d^3 (a+b d^2+c d^4)^3 x + \right. \\
 & \quad \frac{3}{2} d^2 (a+b d^2+c d^4)^2 (a+3 b d^2+5 c d^4) e x^2 + d (a^3+10 a^2 b d^2+21 a b^2 d^4+21 a^2 c d^4+ \\
 & \quad \quad 12 b^3 d^6+72 a b c d^6+55 b^2 c d^8+55 a c^2 d^8+78 b c^2 d^{10}+35 c^3 d^{12}) e^2 x^3 + \\
 & \quad \frac{1}{4} (a^3+30 a^2 b d^2+105 a b^2 d^4+105 a^2 c d^4+84 b^3 d^6+504 a b c d^6+495 b^2 c d^8+ \\
 & \quad \quad 495 a c^2 d^8+858 b c^2 d^{10}+455 c^3 d^{12}) e^3 x^4 + \frac{3}{5} d (5 a^2 b+35 a b^2 d^2+35 a^2 c d^2+ \\
 & \quad \quad 42 b^3 d^4+252 a b c d^4+330 b^2 c d^6+330 a c^2 d^6+715 b c^2 d^8+455 c^3 d^{10}) e^4 x^5 + \\
 & \quad \frac{1}{2} (a^2 b+21 a b^2 d^2+21 a^2 c d^2+42 b^3 d^4+252 a b c d^4+462 b^2 c d^6+ \\
 & \quad \quad 462 a c^2 d^6+1287 b c^2 d^8+1001 c^3 d^{10}) e^5 x^6 + \\
 & \quad \frac{1}{7} d (21 a b^2+21 a^2 c+84 b^3 d^2+504 a b c d^2+1386 b^2 c d^4+1386 a c^2 d^4+5148 b c^2 d^6+5005 c^3 d^8) \\
 & \quad e^6 x^7 + \frac{3}{8} (a b^2+a^2 c+12 b^3 d^2+72 a b c d^2+330 b^2 c d^4+330 a c^2 d^4+1716 b c^2 d^6+2145 c^3 d^8) \\
 & \quad e^7 x^8 + d (b^3+6 a b c+55 b^2 c d^2+55 a c^2 d^2+429 b c^2 d^4+715 c^3 d^6) e^8 x^9 + \\
 & \quad \frac{1}{10} (b^3+6 a b c+165 b^2 c d^2+165 a c^2 d^2+2145 b c^2 d^4+5005 c^3 d^6) e^9 x^{10} + \\
 & \quad 3 c d (b^2+a c+26 b c d^2+91 c^2 d^4) e^{10} x^{11} + \\
 & \quad \frac{1}{4} c (b^2+a c+78 b c d^2+455 c^2 d^4) e^{11} x^{12} + c^2 d (3 b+35 c d^2) e^{12} x^{13} + \\
 & \quad \left. \frac{3}{14} c^2 (b+35 c d^2) e^{13} x^{14} + c^3 d e^{14} x^{15} + \frac{1}{16} c^3 e^{15} x^{16} \right)
 \end{aligned}$$

Problem 661: Unable to integrate problem.

$$\int \frac{x}{\sqrt{a+b(d+ex)^3+c(d+ex)^6}} dx$$

Optimal (type 6, 340 leaves, 7 steps):

$$\begin{aligned}
 & - \left(\left(d(d+ex) \sqrt{1 + \frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}}} \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}, - \frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(e^2 \sqrt{a+b(d+ex)^3+c(d+ex)^6} \right) \right) + \\
 & \left((d+ex)^2 \sqrt{1 + \frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}}} \operatorname{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \right. \right. \\
 & \quad \left. \left. \left. - \frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}, - \frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left(2 e^2 \sqrt{a+b(d+ex)^3+c(d+ex)^6} \right)
 \end{aligned}$$

Result (type 8, 28 leaves):

$$\int \frac{x}{\sqrt{a+b(d+ex)^3+c(d+ex)^6}} dx$$

Problem 662: Unable to integrate problem.

$$\int \frac{x^2}{\sqrt{a+b(d+ex)^3+c(d+ex)^6}} dx$$

Optimal (type 6, 398 leaves, 10 steps):

$$\begin{aligned} & \left(d^2 (d+ex) \sqrt{1 + \frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}}} \right. \\ & \quad \left. \text{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left(e^3 \sqrt{a+b(d+ex)^3+c(d+ex)^6} \right) - \left(d (d+ex)^2 \sqrt{1 + \frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}} \right. \\ & \quad \left. \sqrt{1 + \frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}}} \text{AppellF1} \left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{2c(d+ex)^3}{b - \sqrt{b^2 - 4ac}}, -\frac{2c(d+ex)^3}{b + \sqrt{b^2 - 4ac}} \right] \right) / \\ & \left(e^3 \sqrt{a+b(d+ex)^3+c(d+ex)^6} \right) + \frac{\text{ArcTanh} \left[\frac{b+2c(d+ex)^3}{2\sqrt{c}\sqrt{a+b(d+ex)^3+c(d+ex)^6}} \right]}{3\sqrt{c}e^3} \end{aligned}$$

Result (type 8, 30 leaves):

$$\int \frac{x^2}{\sqrt{a+b(d+ex)^3+c(d+ex)^6}} dx$$

Problem 664: Result more than twice size of optimal antiderivative.

$$\int (2+3x)^6 \left(1 + (2+3x)^7 + (2+3x)^{14} \right)^2 dx$$

Optimal (type 1, 56 leaves, 4 steps):

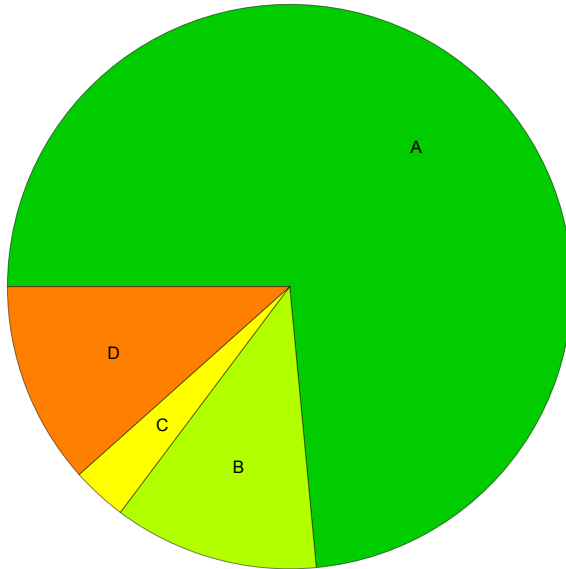
$$\frac{1}{21} (2+3x)^7 + \frac{1}{21} (2+3x)^{14} + \frac{1}{21} (2+3x)^{21} + \frac{1}{42} (2+3x)^{28} + \frac{1}{105} (2+3x)^{35}$$

Result (type 1, 188 leaves):

$$\begin{aligned}
 & 17\,451\,466\,816 x + 443\,569\,828\,128 x^2 + 7\,299\,544\,818\,384 x^3 + 87\,406\,679\,578\,680 x^4 + \\
 & \frac{4\,057\,390\,785\,756\,924 x^5}{5} + 6\,077\,684\,727\,888\,102 x^6 + 37\,727\,143\,432\,895\,007 x^7 + \\
 & 197\,897\,276\,851\,452\,864 x^8 + 889\,942\,562\,270\,387\,136 x^9 + \frac{17\,344\,958\,593\,049\,772\,048 x^{10}}{5} + \\
 & 11\,821\,487\,501\,620\,716\,192 x^{11} + 35\,454\,069\,480\,572\,048\,124 x^{12} + 94\,069\,263\,918\,929\,616\,324 x^{13} + \\
 & 221\,699\,757\,548\,270\,194\,389 x^{14} + 465\,517\,091\,041\,681\,015\,296 x^{15} + 872\,775\,774\,067\,455\,498\,528 x^{16} + \\
 & 1\,463\,104\,032\,160\,519\,033\,200 x^{17} + 2\,194\,577\,166\,014\,752\,240\,080 x^{18} + 2\,945\,285\,062\,308\,448\,290\,360 x^{19} + \\
 & 3\,534\,290\,697\,929\,473\,864\,098 x^{20} + \frac{26\,506\,949\,038\,858\,918\,036\,881 x^{21}}{7} + \\
 & 3\,614\,565\,944\,605\,222\,108\,800 x^{22} + 3\,064\,515\,076\,512\,846\,852\,480 x^{23} + \\
 & 2\,298\,383\,223\,254\,096\,766\,840 x^{24} + \frac{7\,584\,660\,010\,542\,711\,771\,792 x^{25}}{5} + 875\,152\,864\,622\,814\,086\,340 x^{26} + \\
 & 437\,576\,396\,725\,285\,446\,564 x^{27} + \frac{2\,625\,458\,326\,972\,530\,284\,475 x^{28}}{14} + 67\,899\,784\,121\,041\,365\,504 x^{29} + \\
 & \frac{101\,849\,676\,181\,562\,048\,256 x^{30}}{5} + 4\,928\,210\,137\,817\,518\,464 x^{31} + 924\,039\,400\,840\,784\,712 x^{32} + \\
 & 126\,005\,372\,841\,925\,188 x^{33} + 11\,118\,121\,133\,111\,046 x^{34} + \frac{16\,677\,181\,699\,666\,569 x^{35}}{35}
 \end{aligned}$$

Summary of Integration Test Results

664 integration problems



A - 488 optimal antiderivatives

B - 78 more than twice size of optimal antiderivatives

C - 21 unnecessarily complex antiderivatives

D - 77 unable to integrate problems

E - 0 integration timeouts